



Computations of Aerodynamic Performance Databases using Output-Based Refinement

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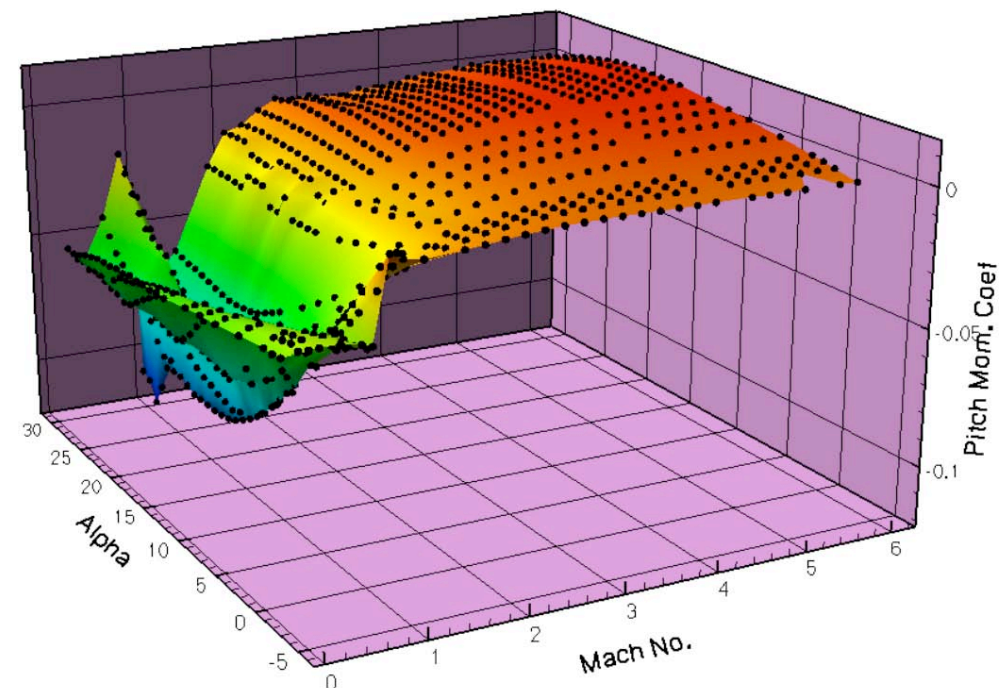
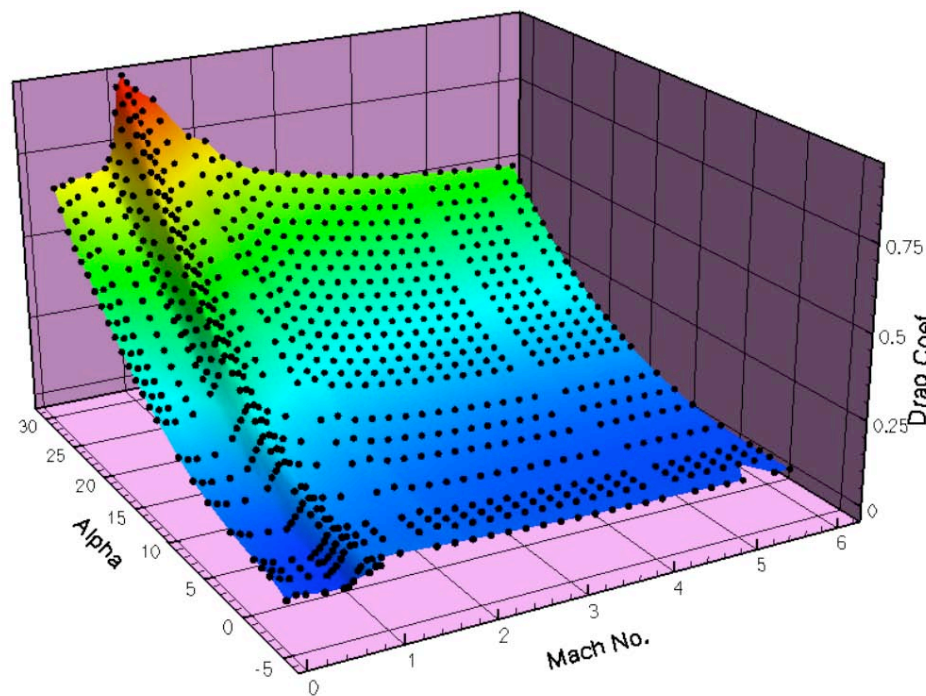
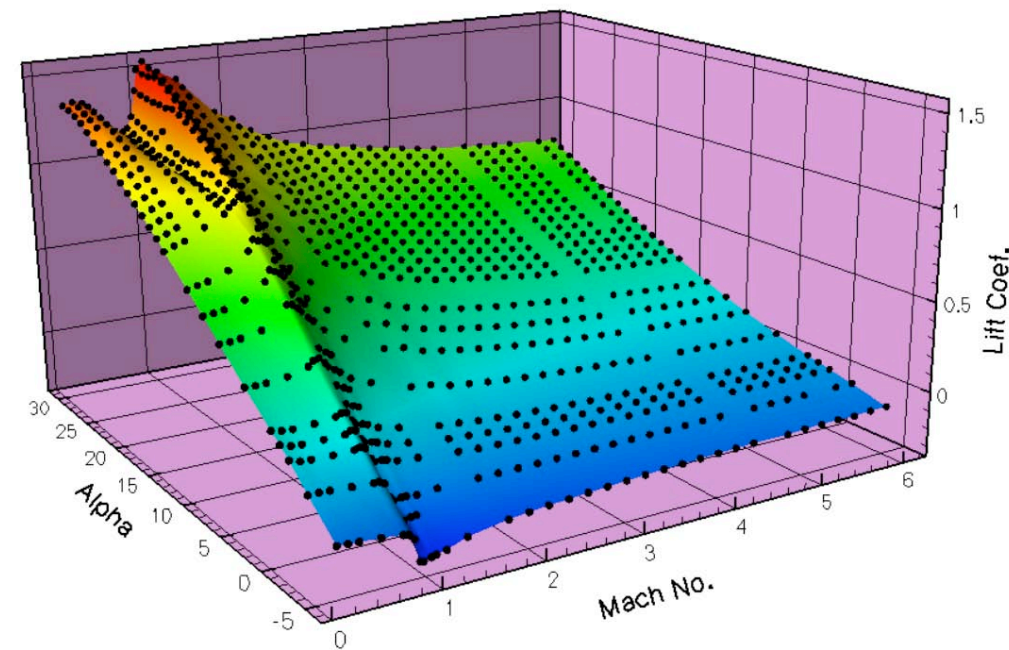
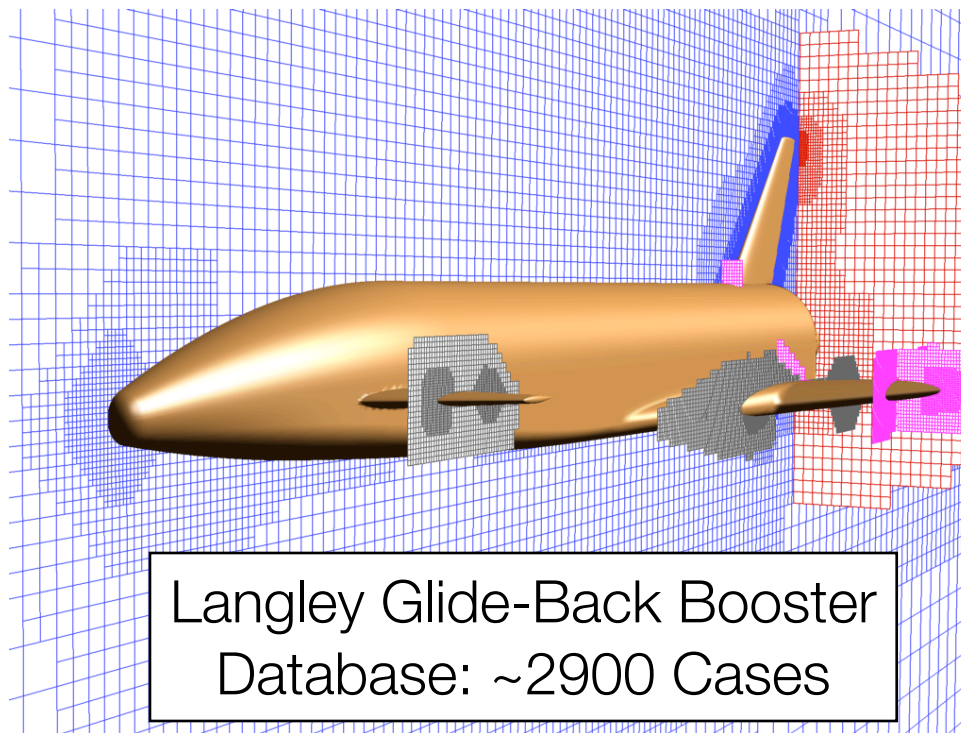
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Oral Presentation Only



Motivation

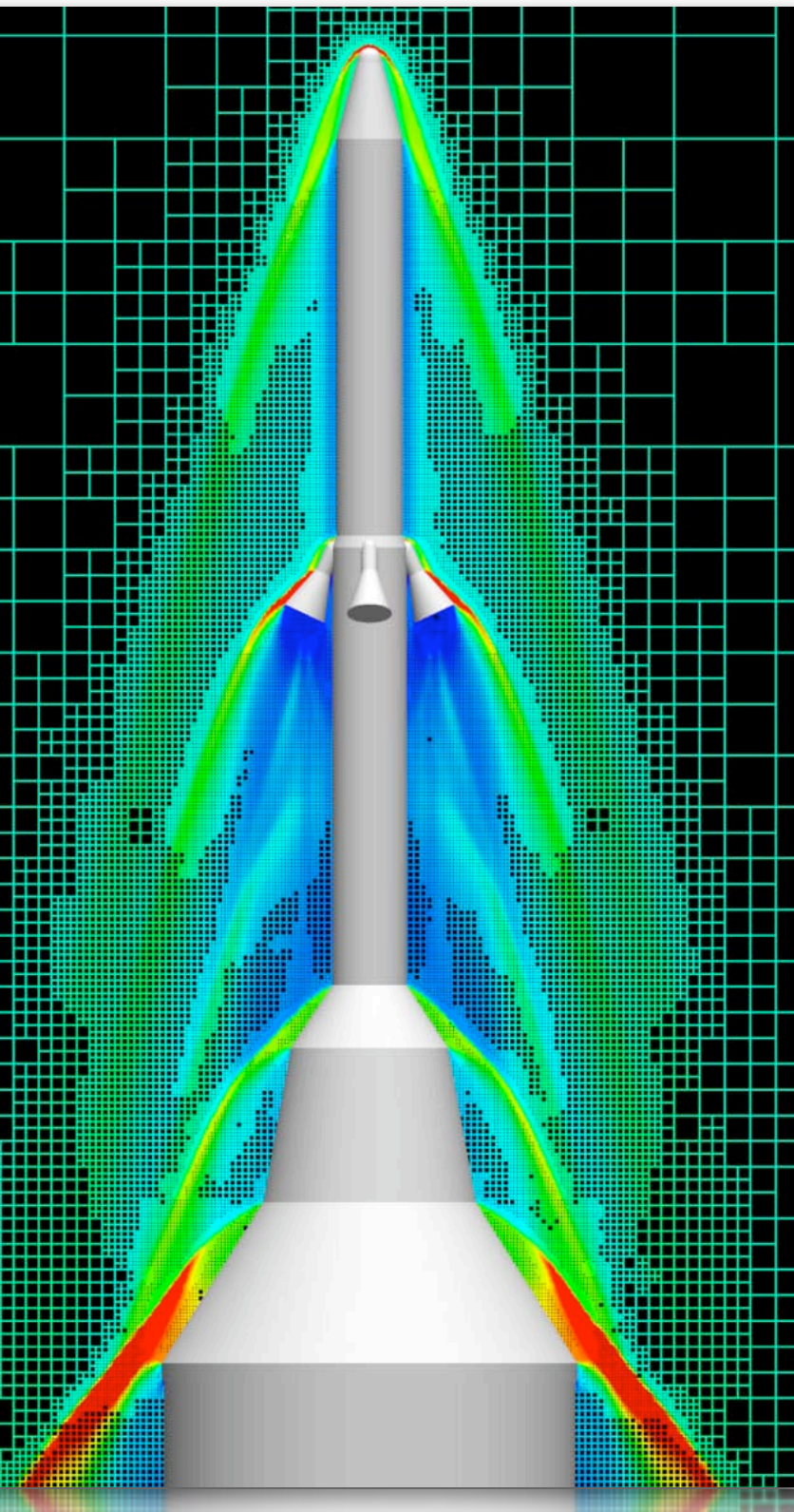


- How well is the vehicle's aerodynamic performance estimated?
- Is the mesh appropriate for every flow condition and vehicle configuration?



Objectives

Toward automation of CFD analysis



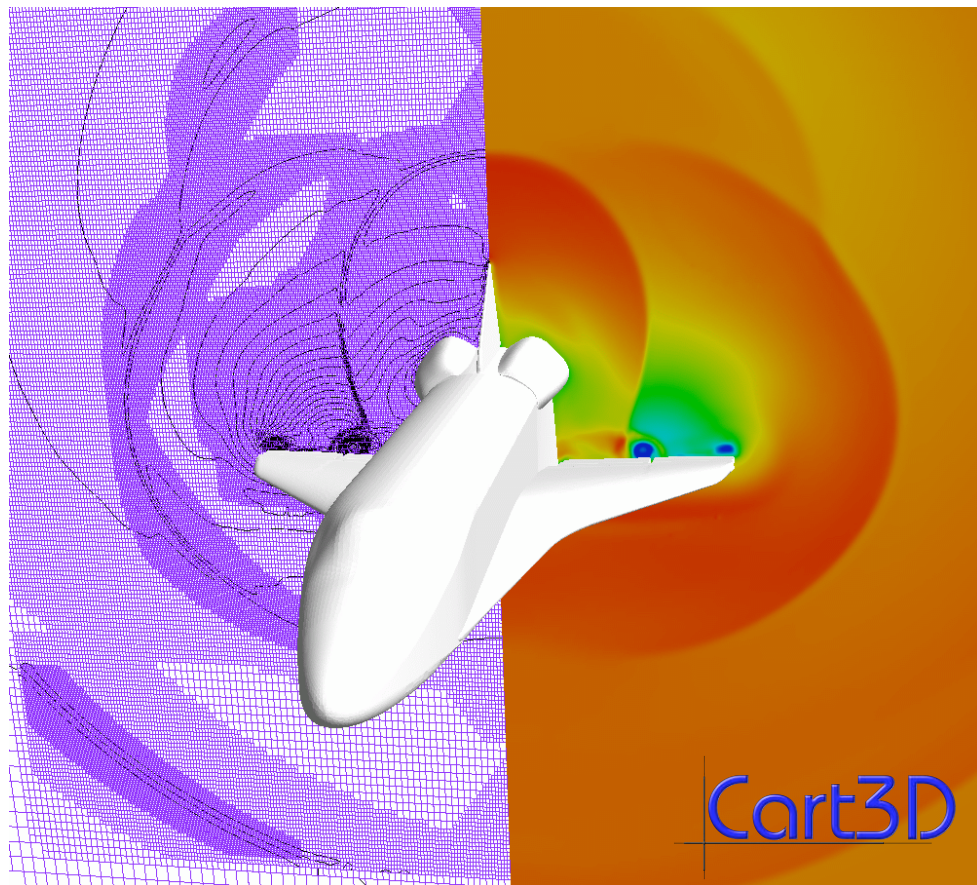
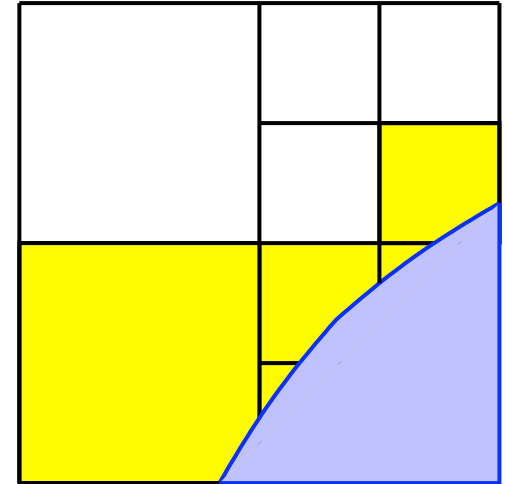
- Handle complex geometry problems
- Control discretization errors via solution-adaptive mesh refinement
- Focus on aerodynamic databases of parametric and optimization studies
 1. **Accuracy**: satisfy prescribed error bounds
 2. **Robustness** and **speed**: may require over 10^5 mesh generations
 3. **Automation**: avoid user supervision
- Obtain “expert meshes” independent of user skill
- Run every case adaptively in production settings



Approach

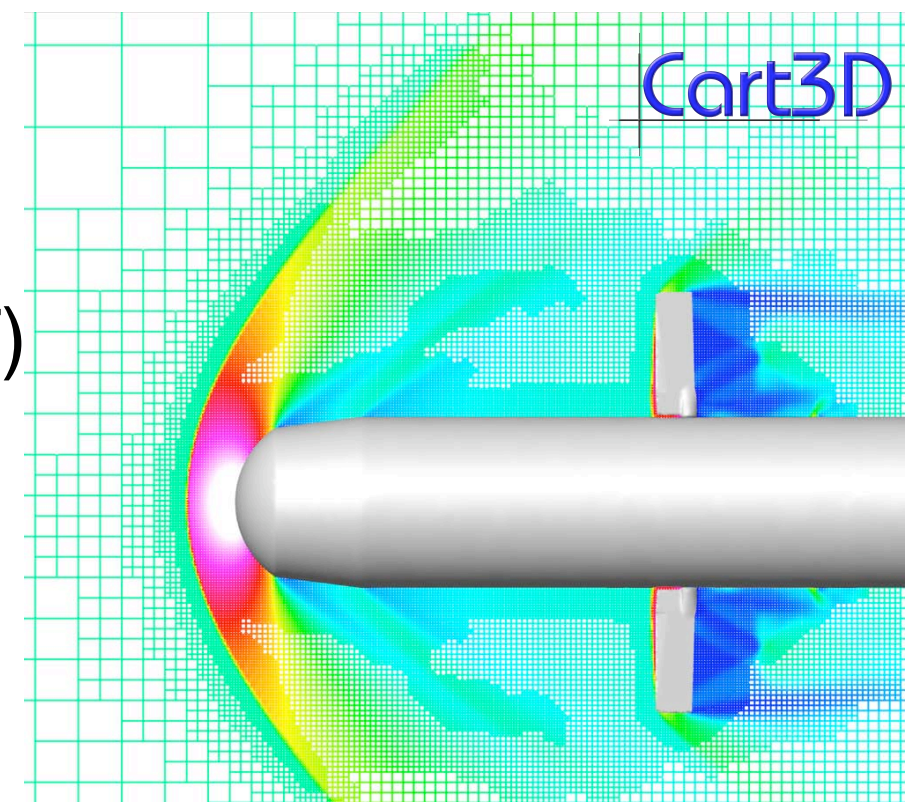
1. Embedded-boundary Cartesian mesh method (1990's)

- Arbitrarily complex domains, efficient and accurate
- Irregularity confined to body intersecting cells



2. Incremental strategy for h-refinement of nested Cartesian meshes (2002)

- Fast local re-meshing of flagged cells
- Guaranteed reliability
- Early work used feature detection and τ -extrapolation



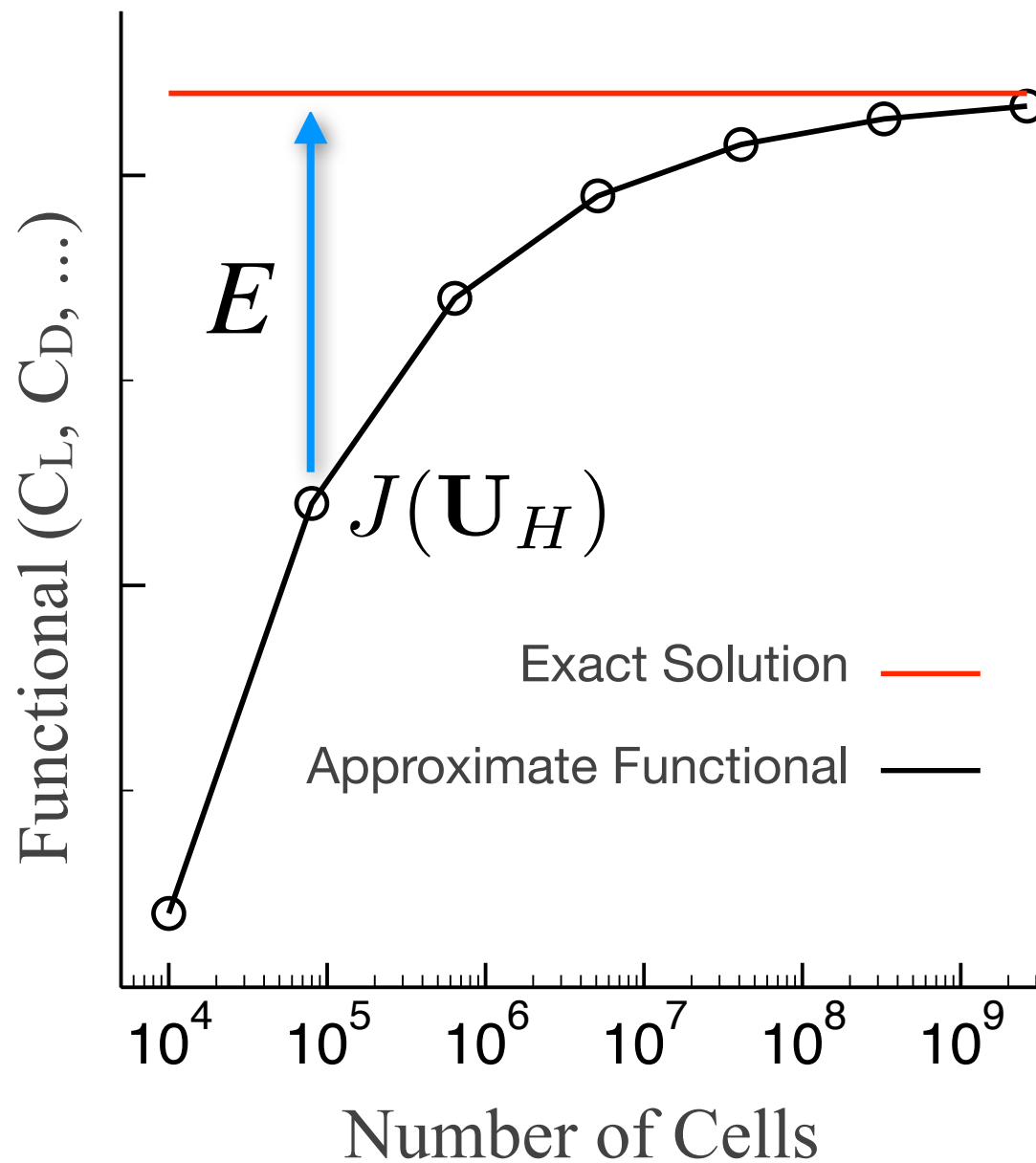
3. Adjoint-weighted residual error estimates (2007)

- Mesh enrichment targets output functionals
- Functional error-bound estimates
- Implementation exploits nesting of Cartesian meshes for fast interpolation



Numerical Error

Uniform Mesh Refinement



➔ Exact Functional: \mathcal{J}

- Numerical solution on a mesh with cell-size H gives approximate functional:

$$J(\mathbf{U}_H)$$

- Goal is to estimate functional error:

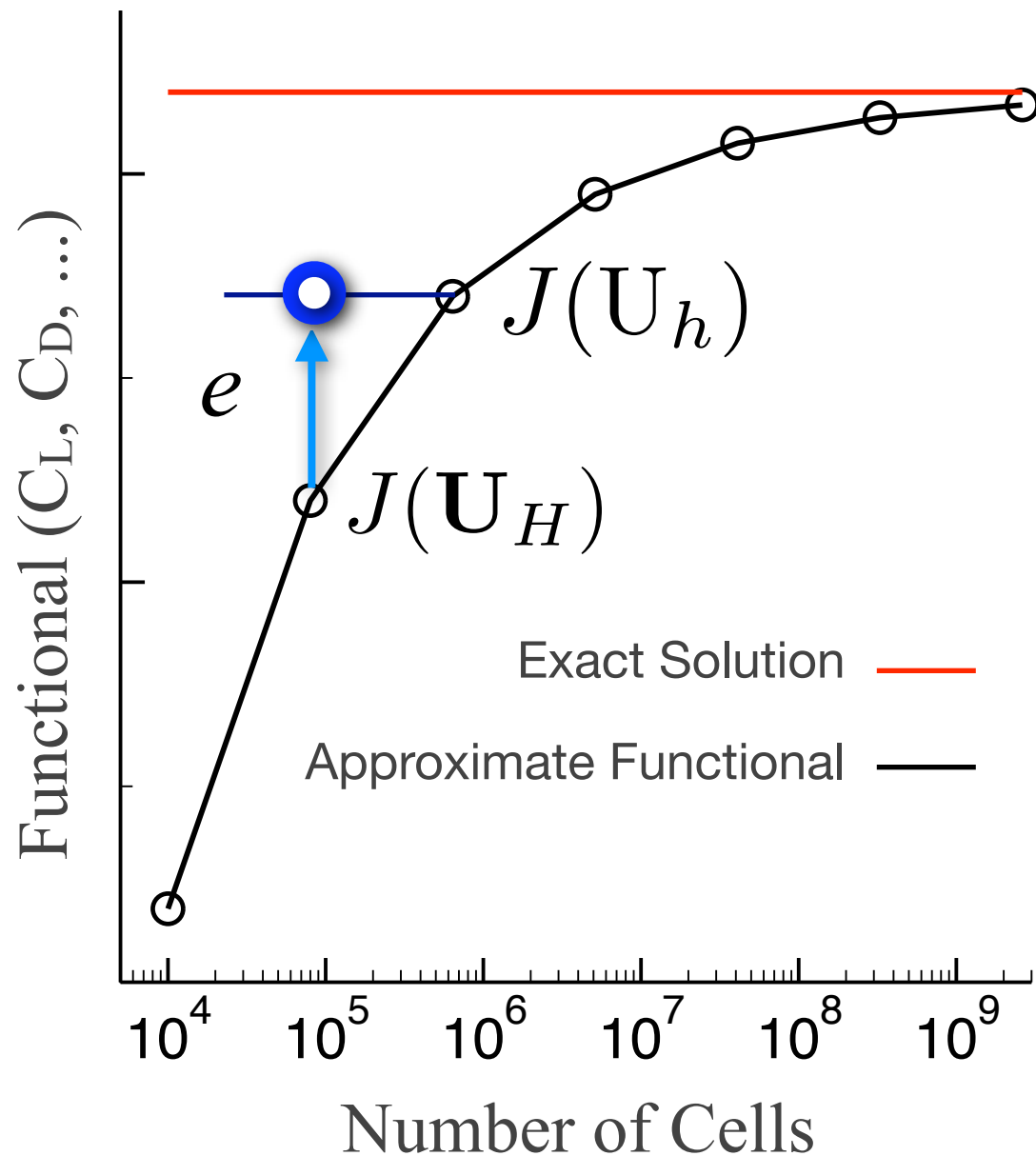
$$\mathcal{J}(\mathbf{U}) = J(\mathbf{U}_H) + E$$

- Express the error as a function of the flow solution

$$E = f(\mathbf{U}_H)$$



Discrete Estimate of Numerical Error



- Consider a simpler problem of computing relative error:

$$J(\mathbf{U}_h) = J(\mathbf{U}_H) + e$$

- For second-order accurate spatial discretization and cell-size in the asymptotic range, the functional error is:

$$\begin{aligned} E &= e + \frac{1}{4}e + \frac{1}{4^2}e + \dots \\ &= \frac{4}{3}e \end{aligned}$$

- We will use an adjoint solution on mesh H to estimate

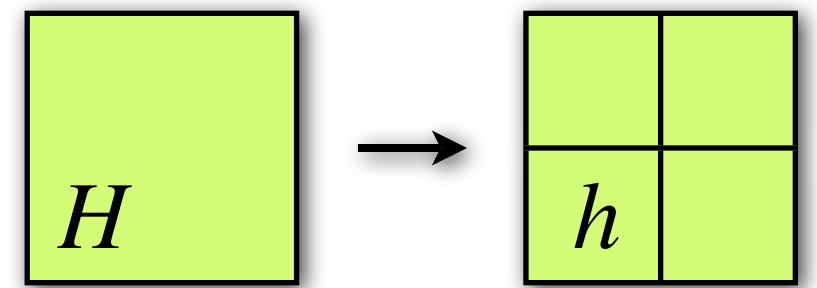
$$e = f(\mathbf{U}_H, \psi_H)$$



Adjoint Error Estimates

- Consider a functional $J(\mathbf{U}_H)$ computed from the solution of Euler equations discretized on an affordable mesh with cell-size H :

$$R(\mathbf{U}_H) = 0$$



- In addition, consider an embedded mesh with cell-size h obtained via uniform refinement of the baseline mesh
- We seek to compute the error relative to the embedded mesh without solving the problem on the fine mesh

$$e = |J(\mathbf{U}_h) - J(\mathbf{U}_h^H)|$$



- Estimate of functional on embedded mesh is obtained from Taylor series expansions about the coarse mesh solution

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) + \frac{\partial J(\mathbf{U}_h^H)}{\partial \mathbf{U}_h} (\mathbf{U}_h - \mathbf{U}_h^H)$$

$$\mathbf{R}(\mathbf{U}_h) = 0 \approx \mathbf{R}(\mathbf{U}_h^H) + \frac{\partial \mathbf{R}(\mathbf{U}_h^H)}{\partial \mathbf{U}_h} (\mathbf{U}_h - \mathbf{U}_h^H)$$

- These equations are combined to give

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - \psi_h^T \mathbf{R}(\mathbf{U}_h^H)$$

where ψ satisfies the adjoint equation

$$\left[\frac{\partial \mathbf{R}(\mathbf{U}_h^H)}{\partial \mathbf{U}_h} \right]^T \psi_h = \frac{\partial J(\mathbf{U}_h^H)}{\partial \mathbf{U}_h}^T$$



- Estimate of functional on embedded mesh is obtained from Taylor series expansions about the coarse mesh solution

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) + \frac{\partial J(\mathbf{U}_h^H)}{\partial \mathbf{U}_h} (\mathbf{U}_h - \mathbf{U}_h^H)$$

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- These equations are combined to give

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - \psi_h^T \mathbf{R}(\mathbf{U}_h^H) \longrightarrow$$

**Adjoint provide
a weighting on
residual errors**

where ψ satisfies the adjoint equation

$$\left[\frac{\partial \mathbf{R}(\mathbf{U}_h^H)}{\partial \mathbf{U}_h} \right]^T \psi_h = \frac{\partial J(\mathbf{U}_h^H)}{\partial \mathbf{U}_h}^T$$



Adjoint Correction and Error Bound

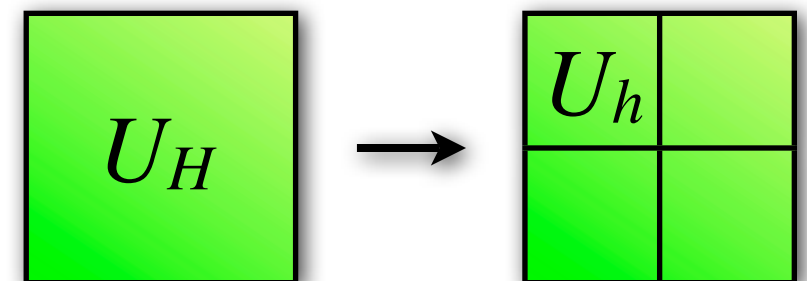
- Since the adjoint solution is not known on the embedded mesh, we use an approximate solution from the coarse mesh to obtain

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - (\psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H) - (\psi_h - \psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H)$$

Adjoint Correction

Remaining Error

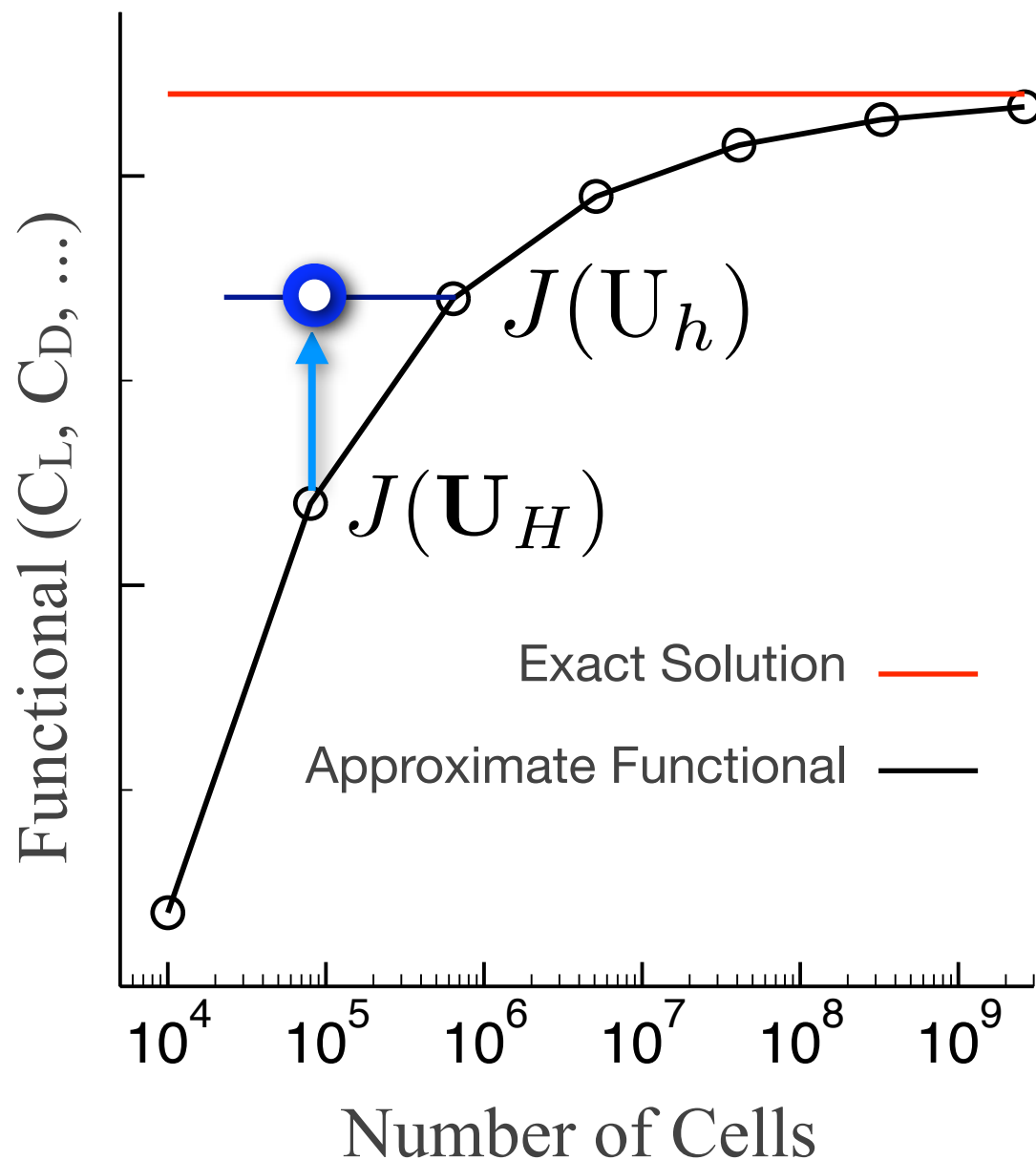
- \mathbf{U}_h^H, ψ_h^H denote reconstructed solutions lifted from coarse mesh to embedded mesh. We use linear interpolation
- ψ_h is unknown. We approximate it with a quadratic interpolant



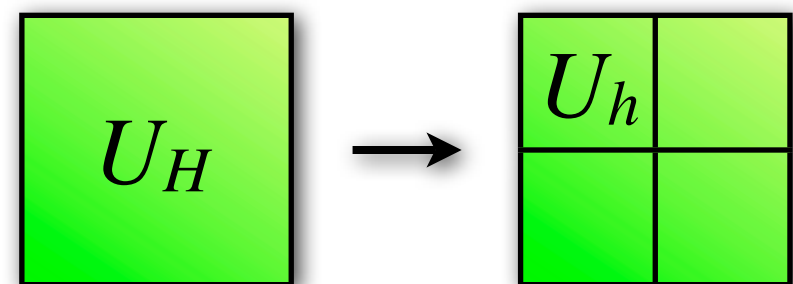


Adjoint Correction

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - (\psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H) - (\psi_h - \psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H)$$



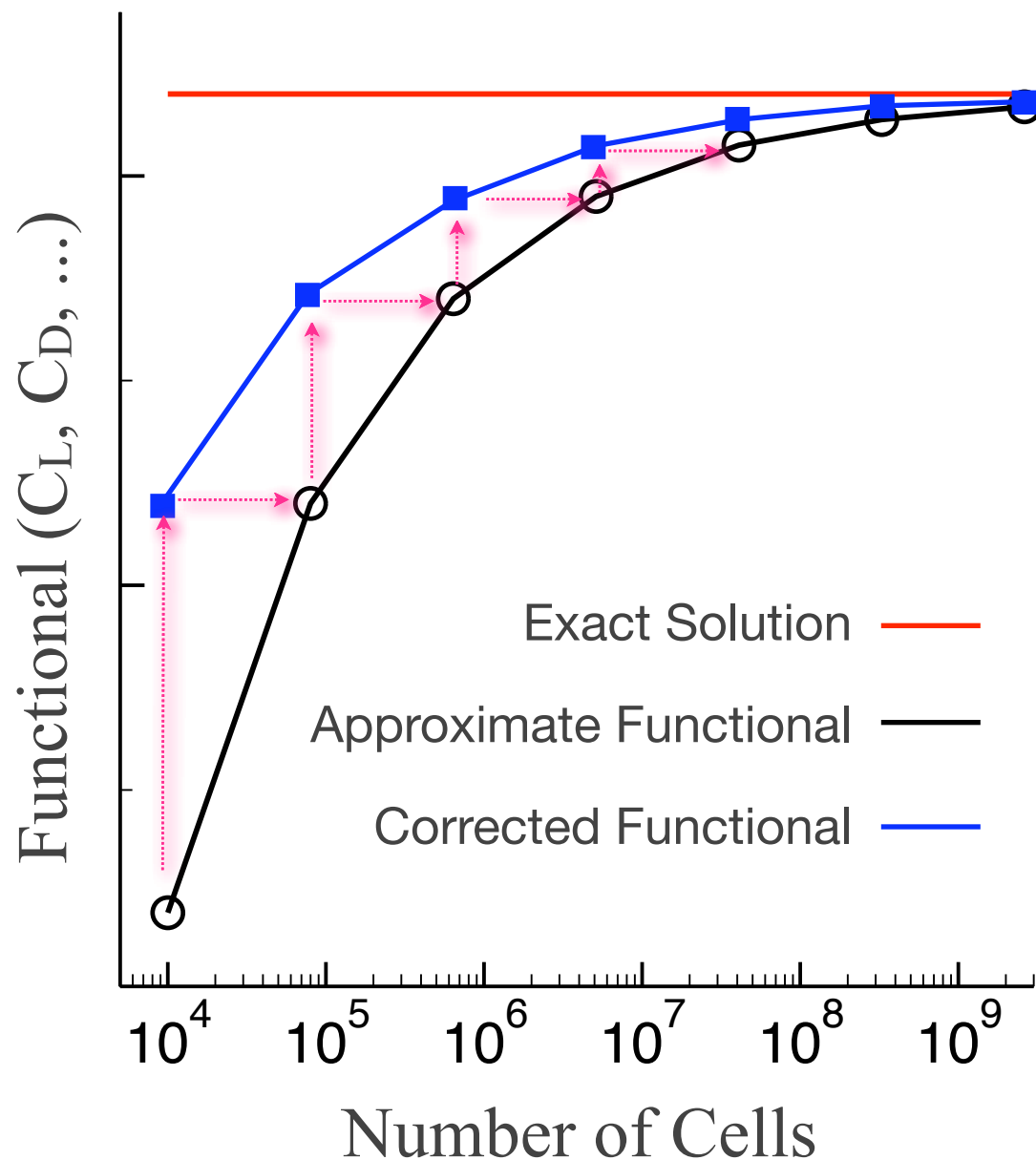
- Predict functional on a fine mesh with cell-size h from a coarse mesh solution with cell size H



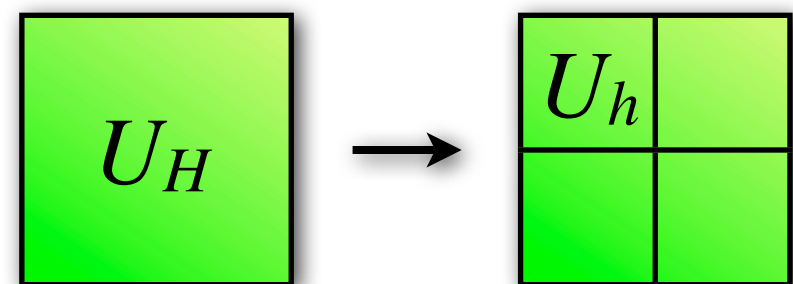


Adjoint Correction

$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - (\psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H) - (\psi_h - \psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H)$$



- Predict functional on a fine mesh with cell-size h from a coarse mesh solution with cell size H





Error Bound Estimate

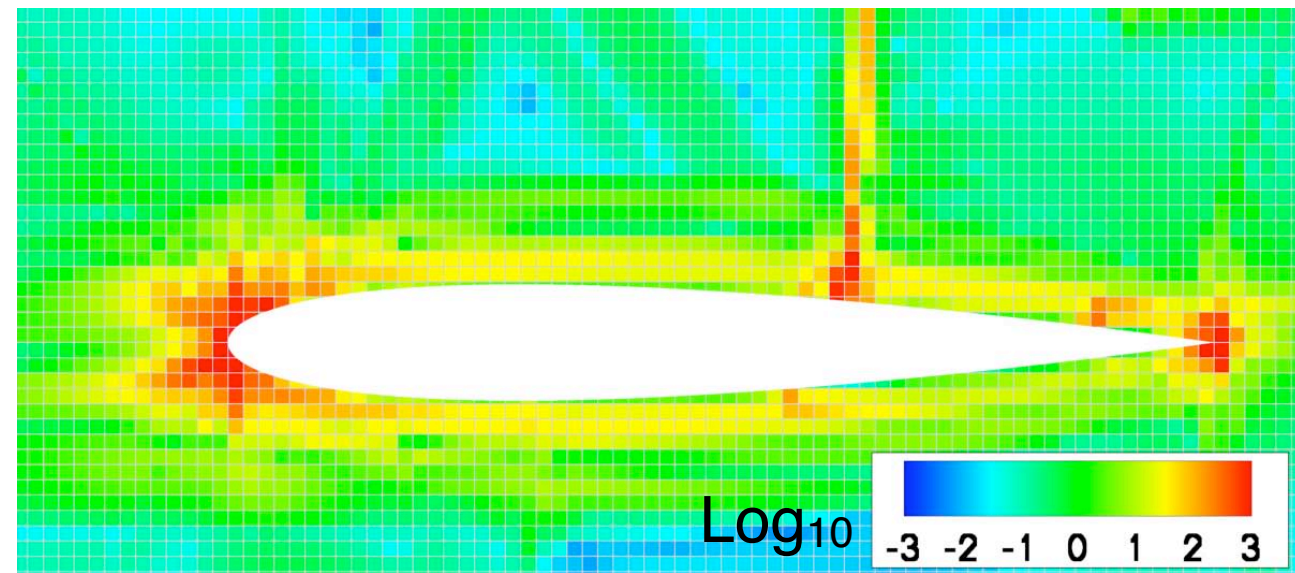
$$J(\mathbf{U}_h) \approx J(\mathbf{U}_h^H) - (\psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H) - (\psi_h - \psi_h^H)^T \mathbf{R}(\mathbf{U}_h^H)$$

- Bound on remaining error in each coarse cell k

$$e_k = \sum \left| (\psi_Q - \psi_L)^T R(\mathbf{U}_L) \right|_k$$

- Net functional error $E = \sum_{k=0}^N e_k$

- Given a user specified tolerance TOL, termination criterion is satisfied when $E < \text{TOL}$

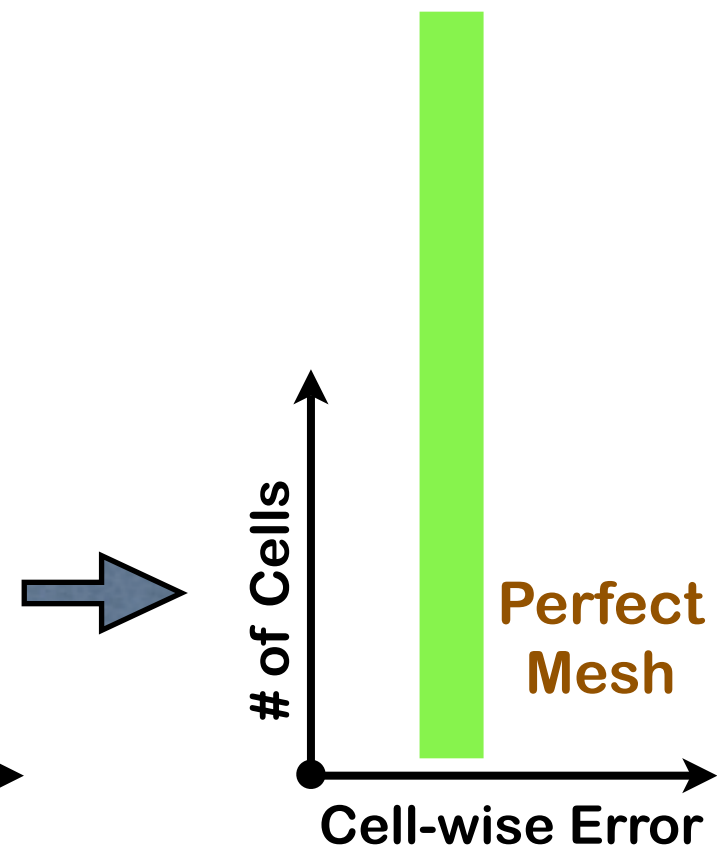
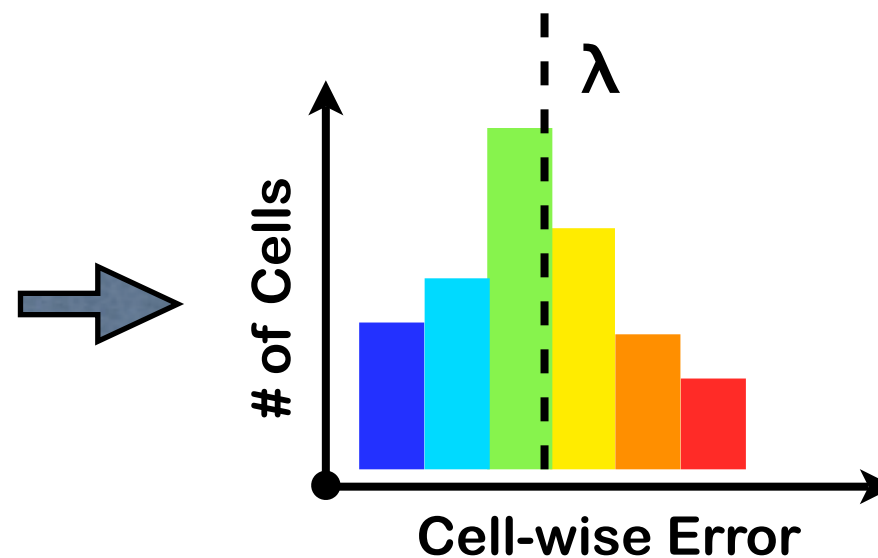
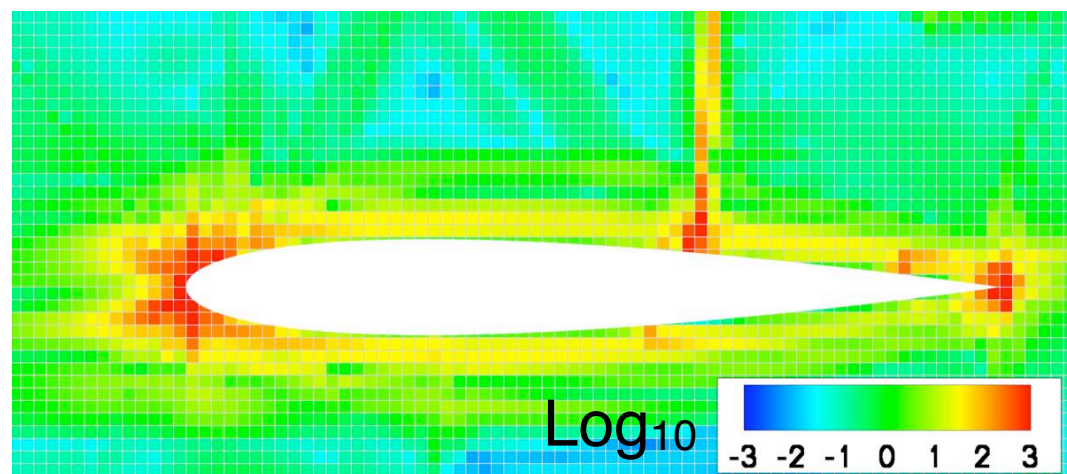




Refinement Parameter

- Define maximum allowable error level in each coarse cell via equidistribution: $t = \text{TOL} / N$
- Refinement parameter in each cell is given by $r_k = \frac{e_k}{t}$
- Refine cells for which $r_k > \lambda$
where $\lambda \geq 1$ is a global threshold factor

Error Histograms



Results

Focus on Applications



Part A. Accuracy

- Launch Abort Vehicle with jets - uniform mesh refinement study

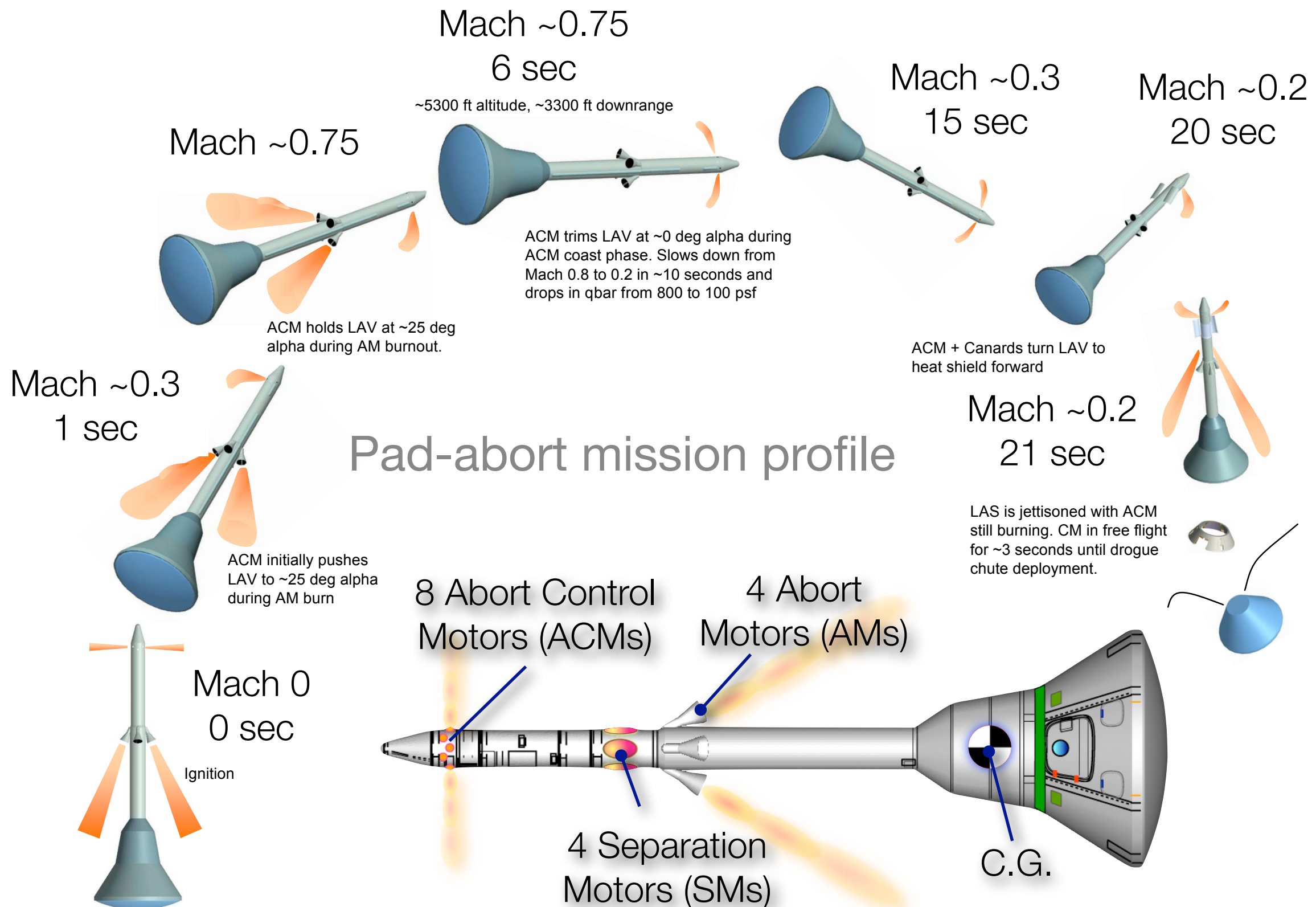
Part B. Efficiency

- Sonic-boom signature test case - computational cost summary

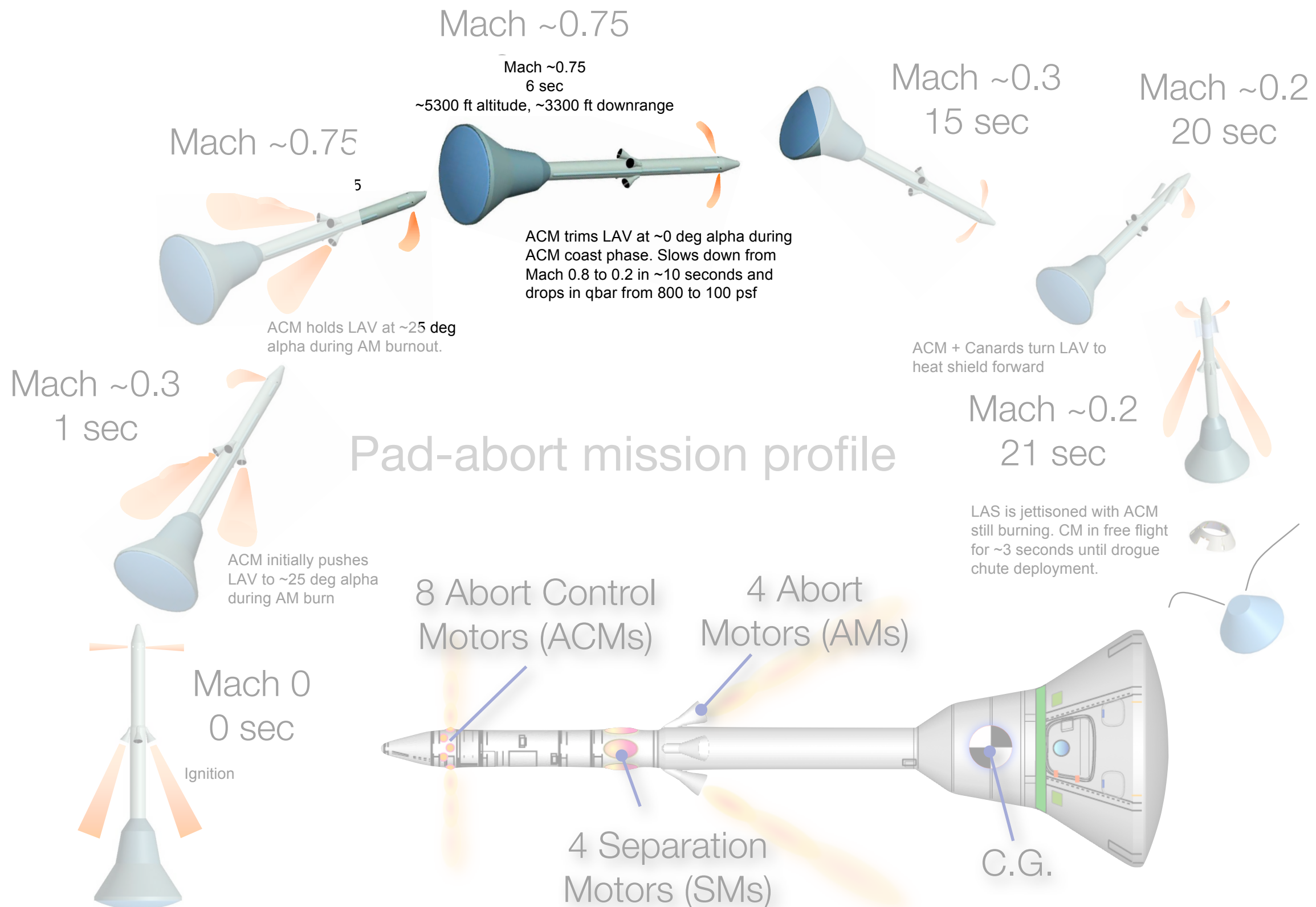
Part C. Databases

- Nozzle-Guide-Vane Missile
- Launch Abort Vehicle with Jettison Motor plumes

Launch Abort Vehicle with ACM Jets



Launch Abort Vehicle with ACM Jets

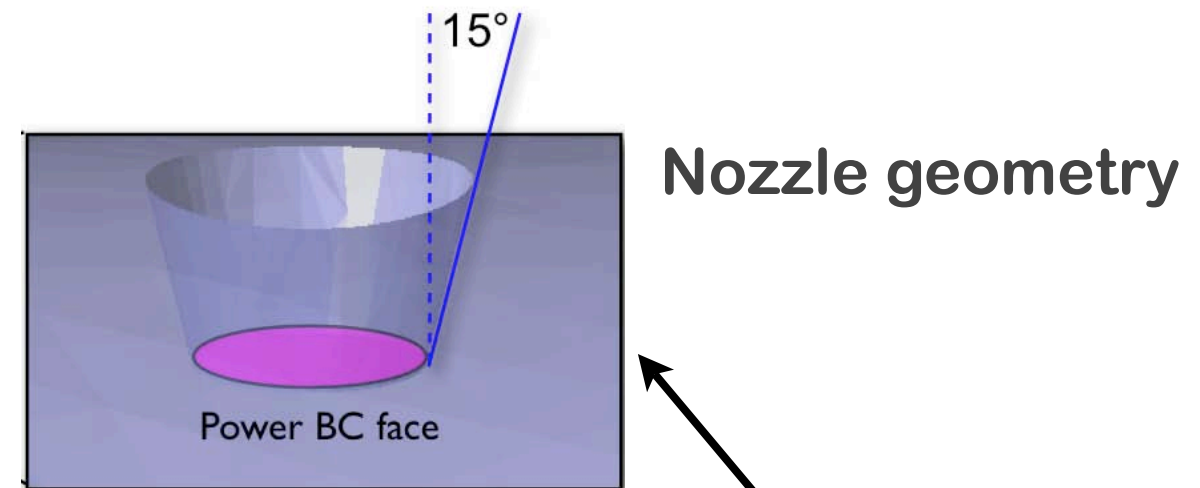


Launch Abort Vehicle with ACM Jets

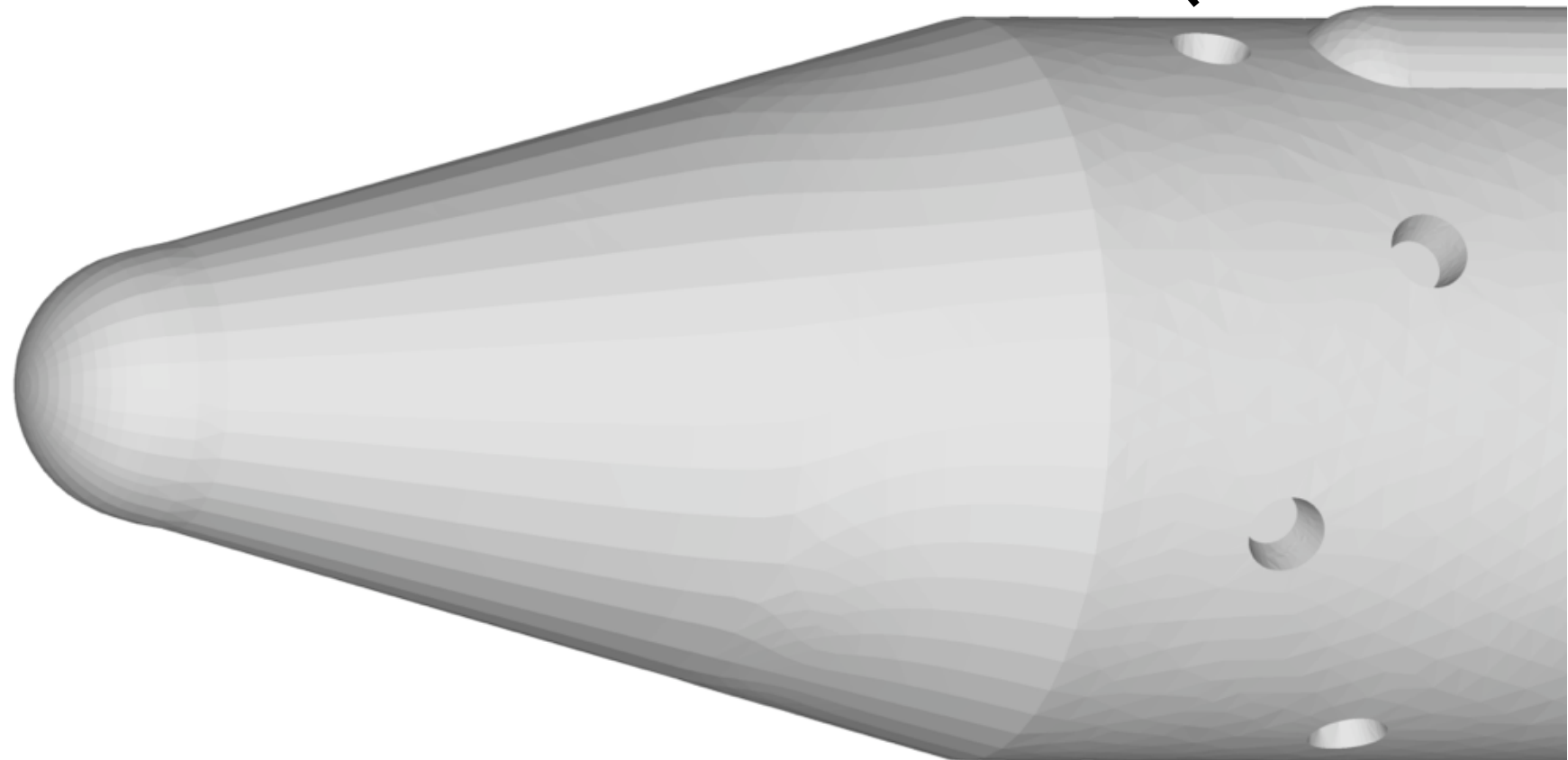
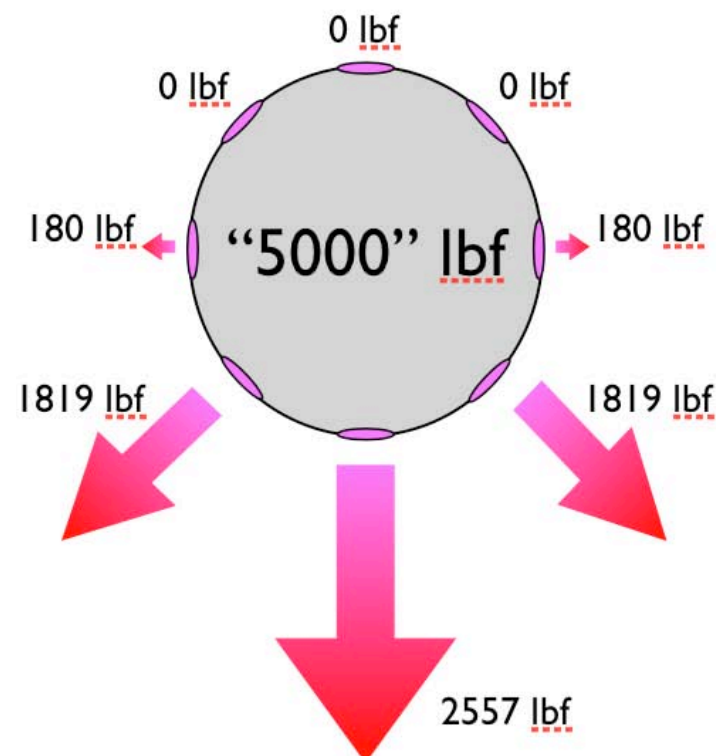
Problem Setup



- Examine aerodynamic performance with ACM jets (AIAA 2008-1281)
- Selected case: $M_\infty = 4$, $\alpha = 20^\circ$, due to significant plume penetration
- Power boundary conditions applied at plenum face (assumes perfect gas)



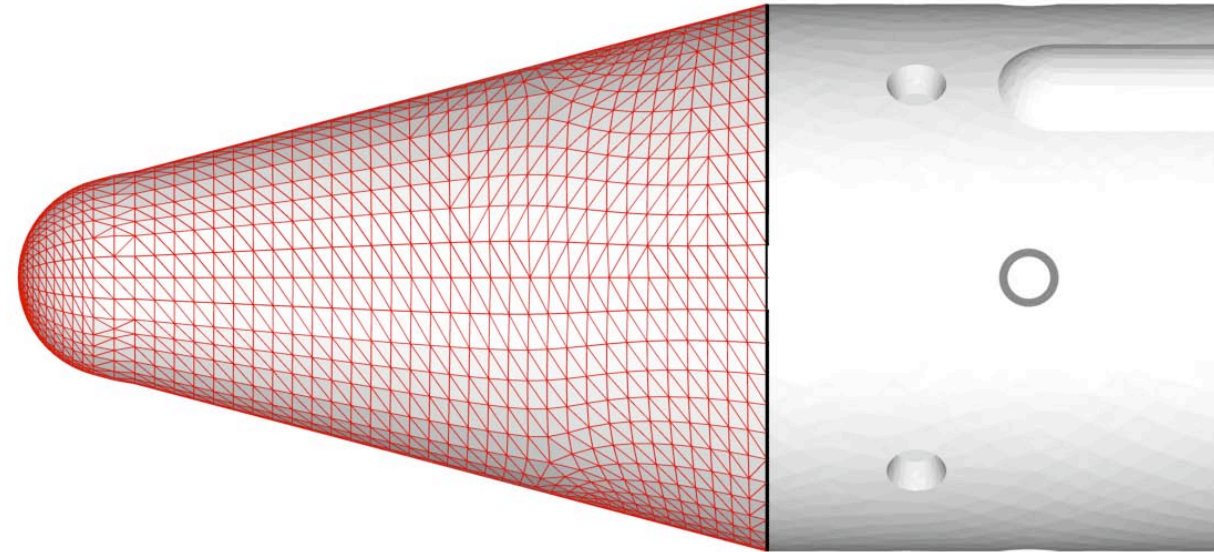
Thrust setting



Launch Abort Vehicle with ACM Jets Functional



- Functional: $C_N + 0.4C_A$
- Consider two cases:
 - ▶ *Case A*: Functional defined over nose-cone surface only, $TOL=0.0005$
 - Accuracy verification: Uniform mesh refinement study
 - Take advantage of supersonic freestream conditions to limit refinement to nose-cone region
 - ▶ *Case B*: Functional defined over entire vehicle, $TOL=0.006$
 - Typical engineering database case

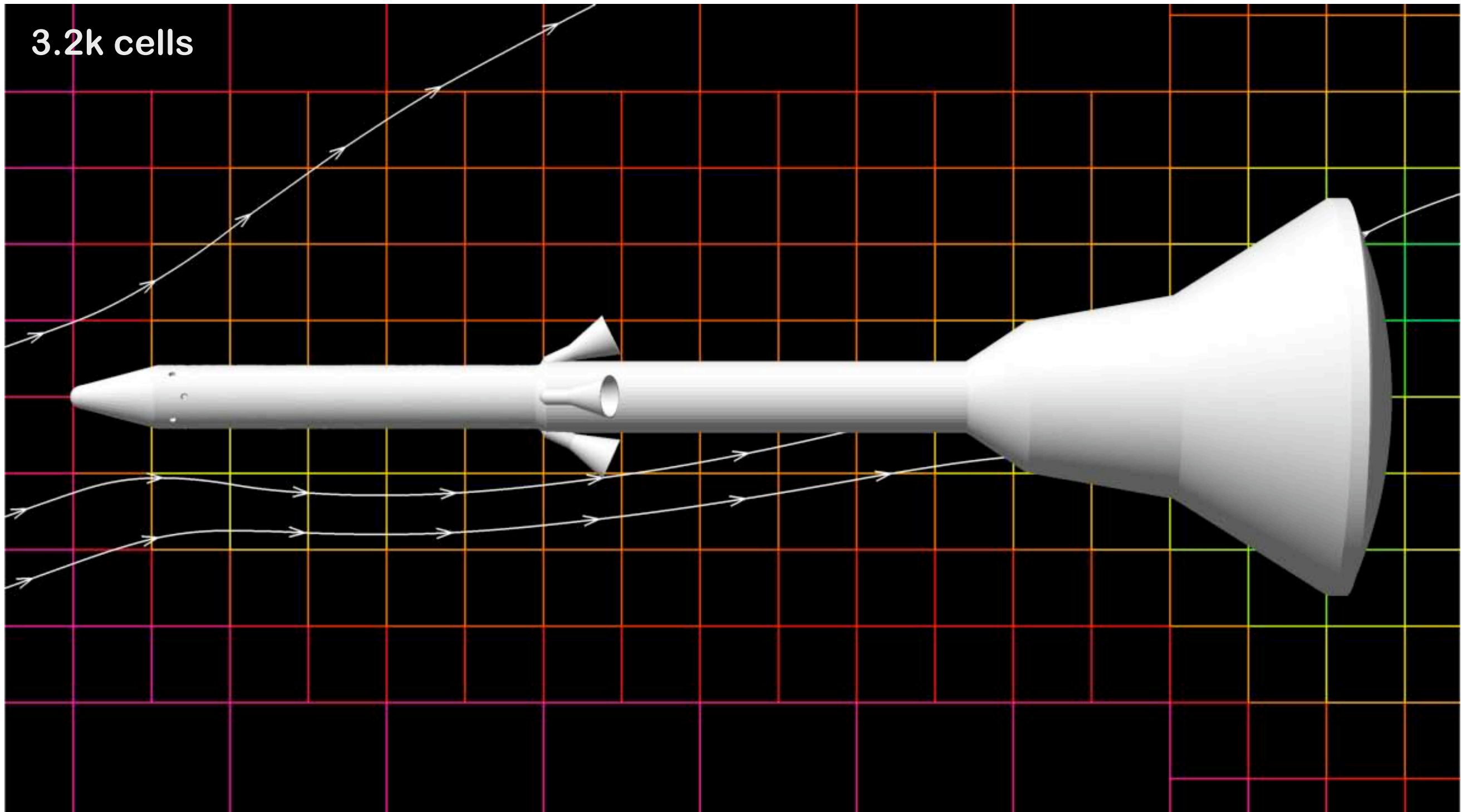


Launch Abort Vehicle

Initial mesh and solution on symmetry plane

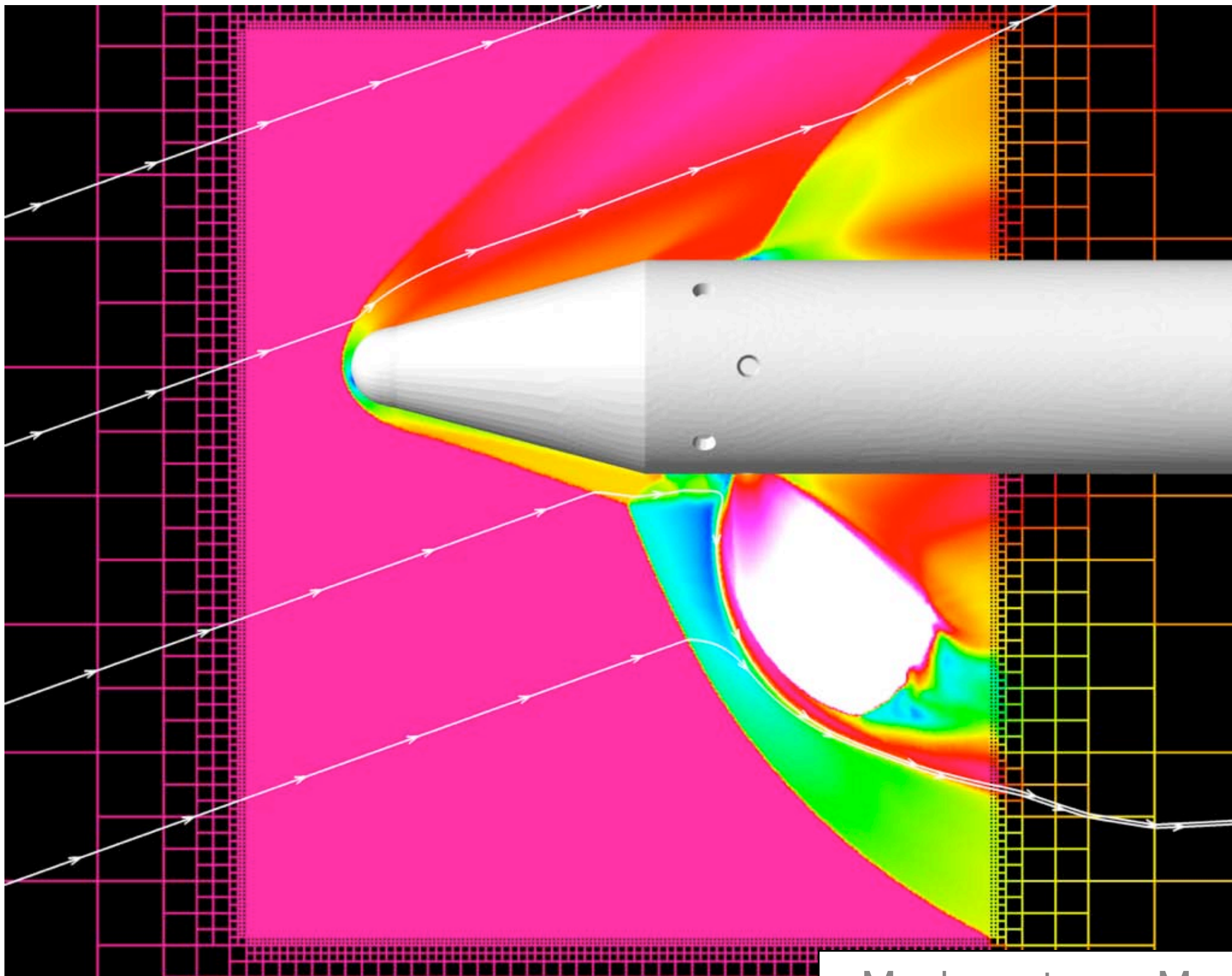


3.2k cells



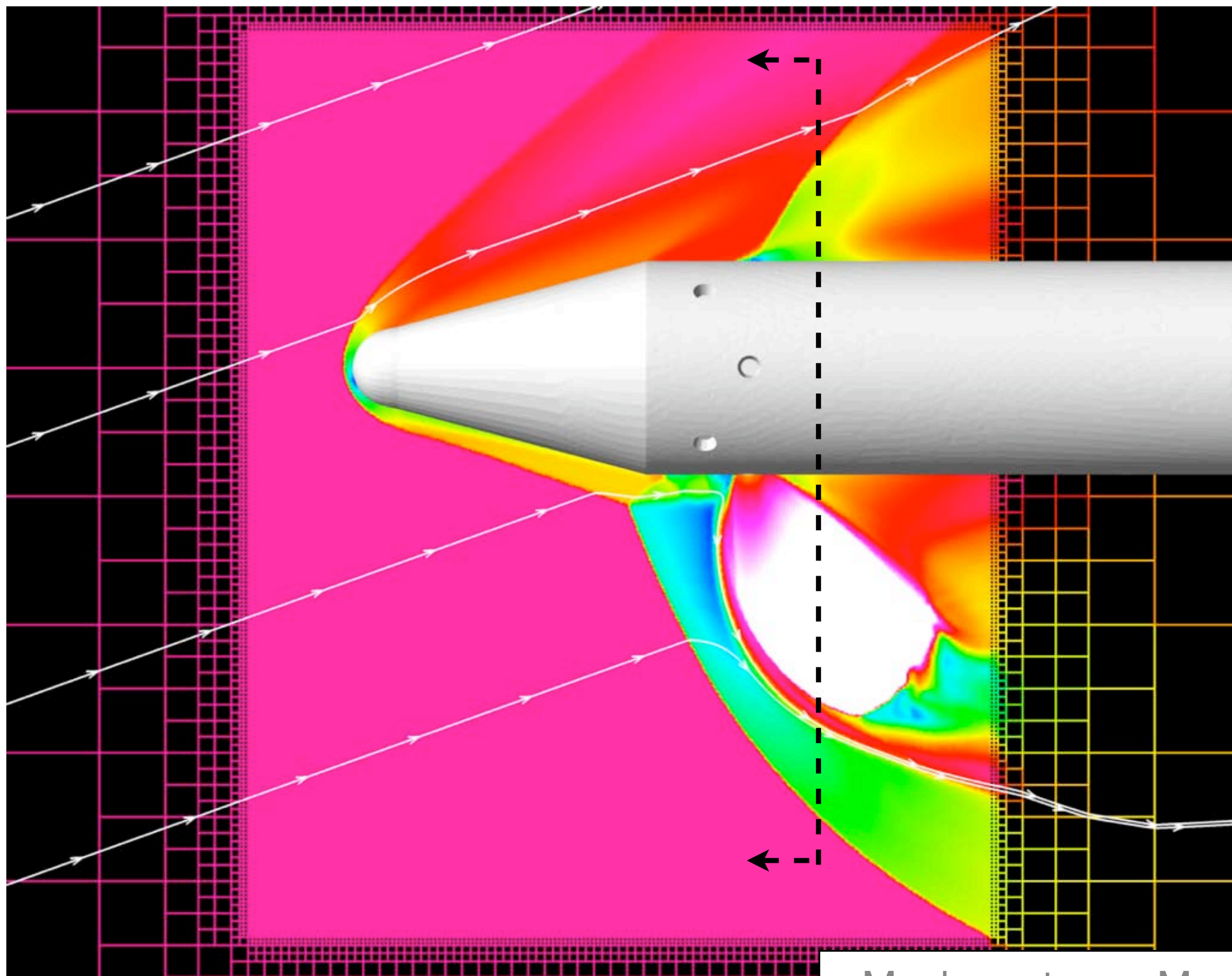
Mach contours, $M_\infty = 4$, $\alpha = 20^\circ$

Case A: Finest Mesh of Uniform Refinement Study (Side-view, 75M Cells)



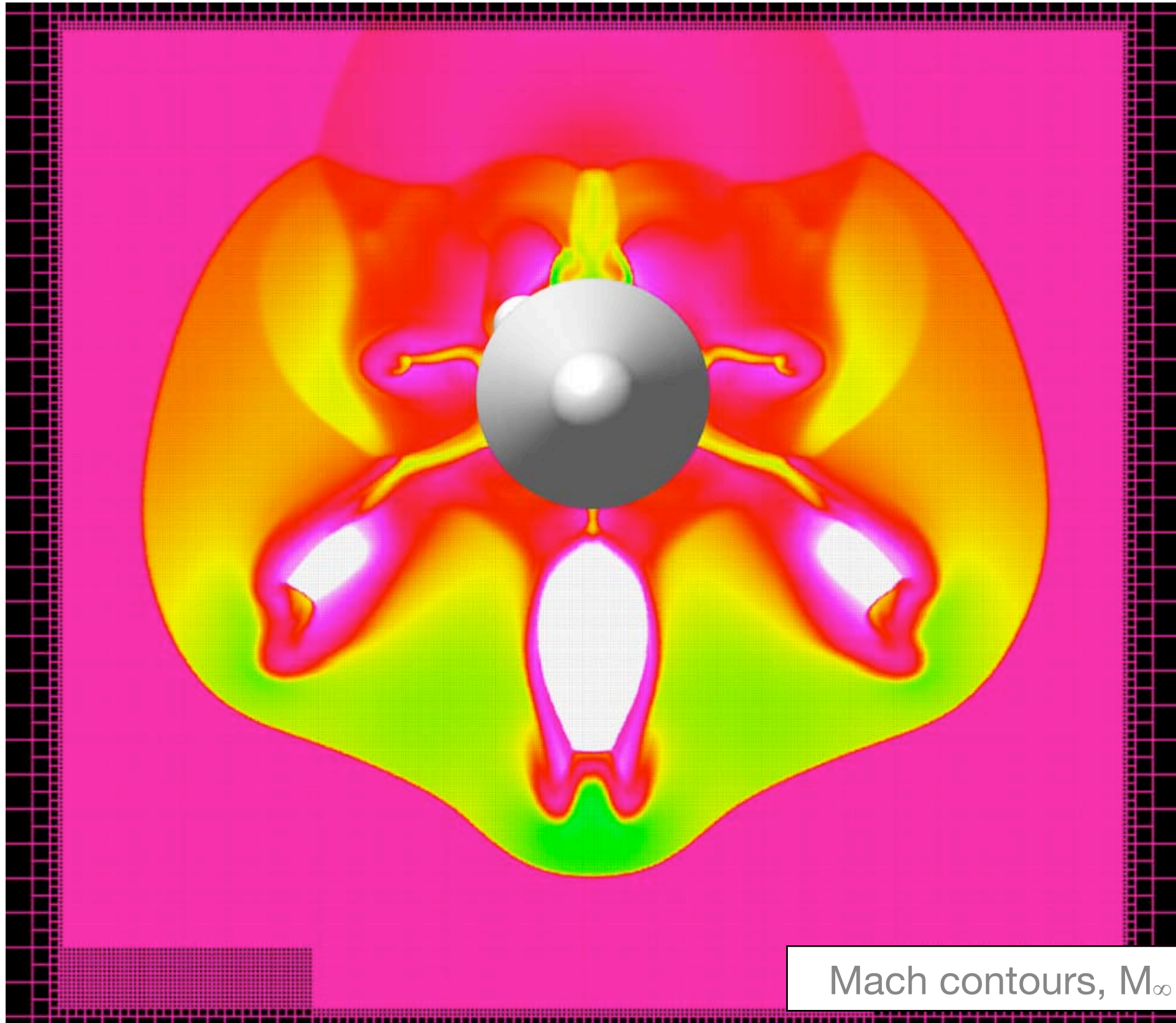
Mach contours, $M_{\infty} = 4$, $\alpha = 20^{\circ}$

Case A: Finest Mesh of Uniform Refinement Study (Side-view, 75M Cells)



Mach contours, $M_\infty = 4$, $\alpha = 20^\circ$

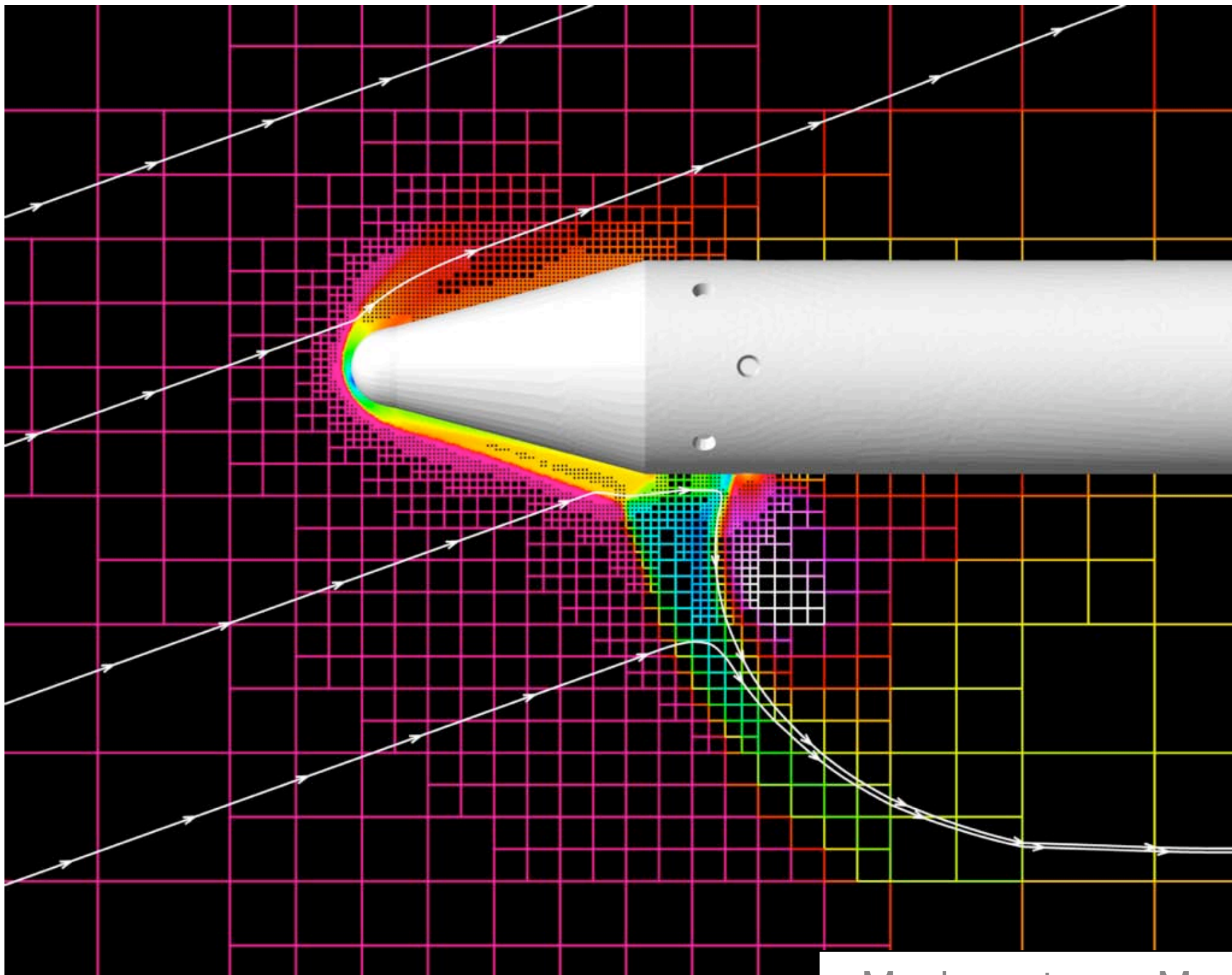
Case A: Finest Mesh of Uniform Refinement Study (Front-view, 75M Cells)



Mach contours, $M_{\infty} = 4$, $\alpha = 20^{\circ}$

Case A: Adapted Mesh (Side-view)

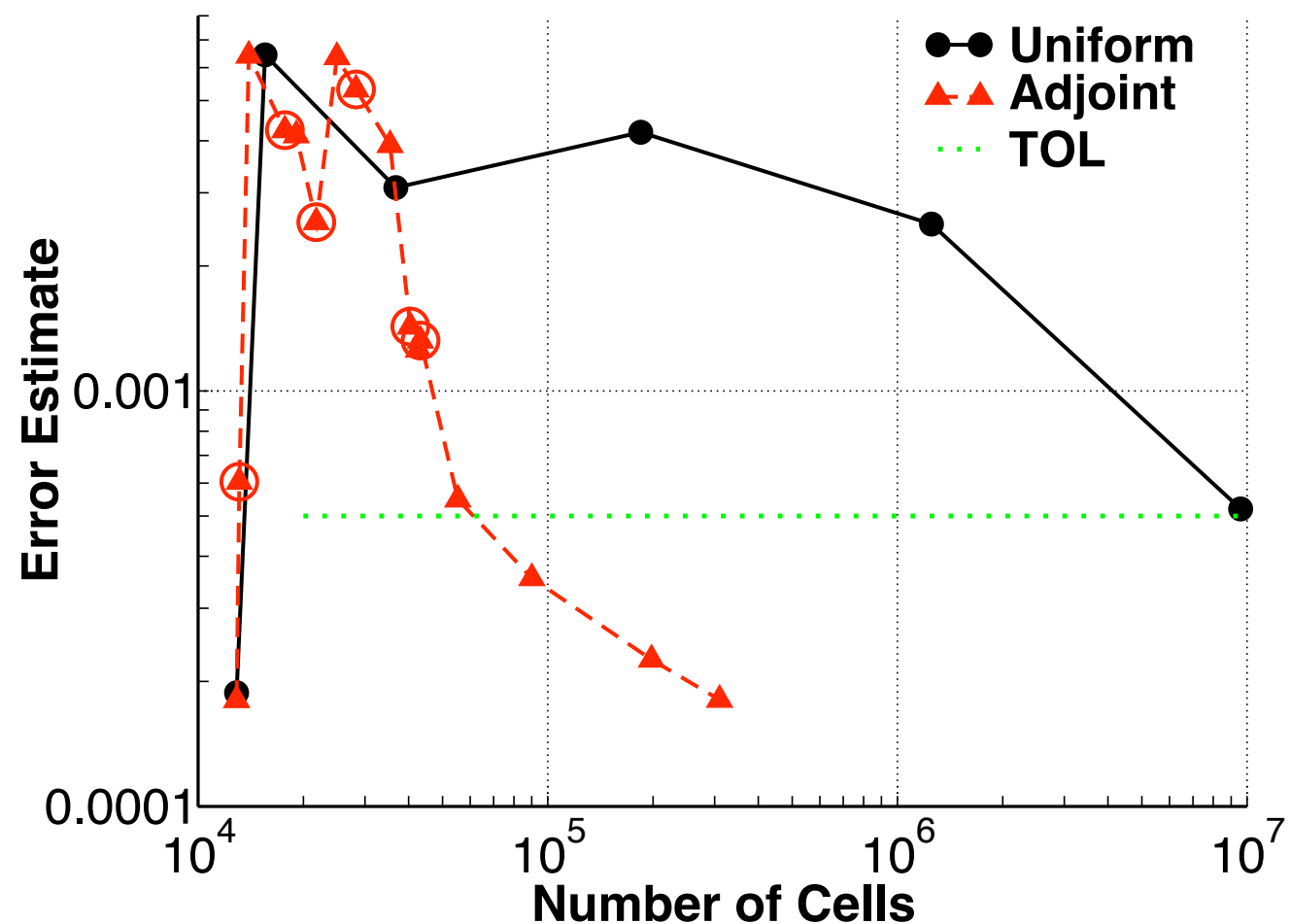
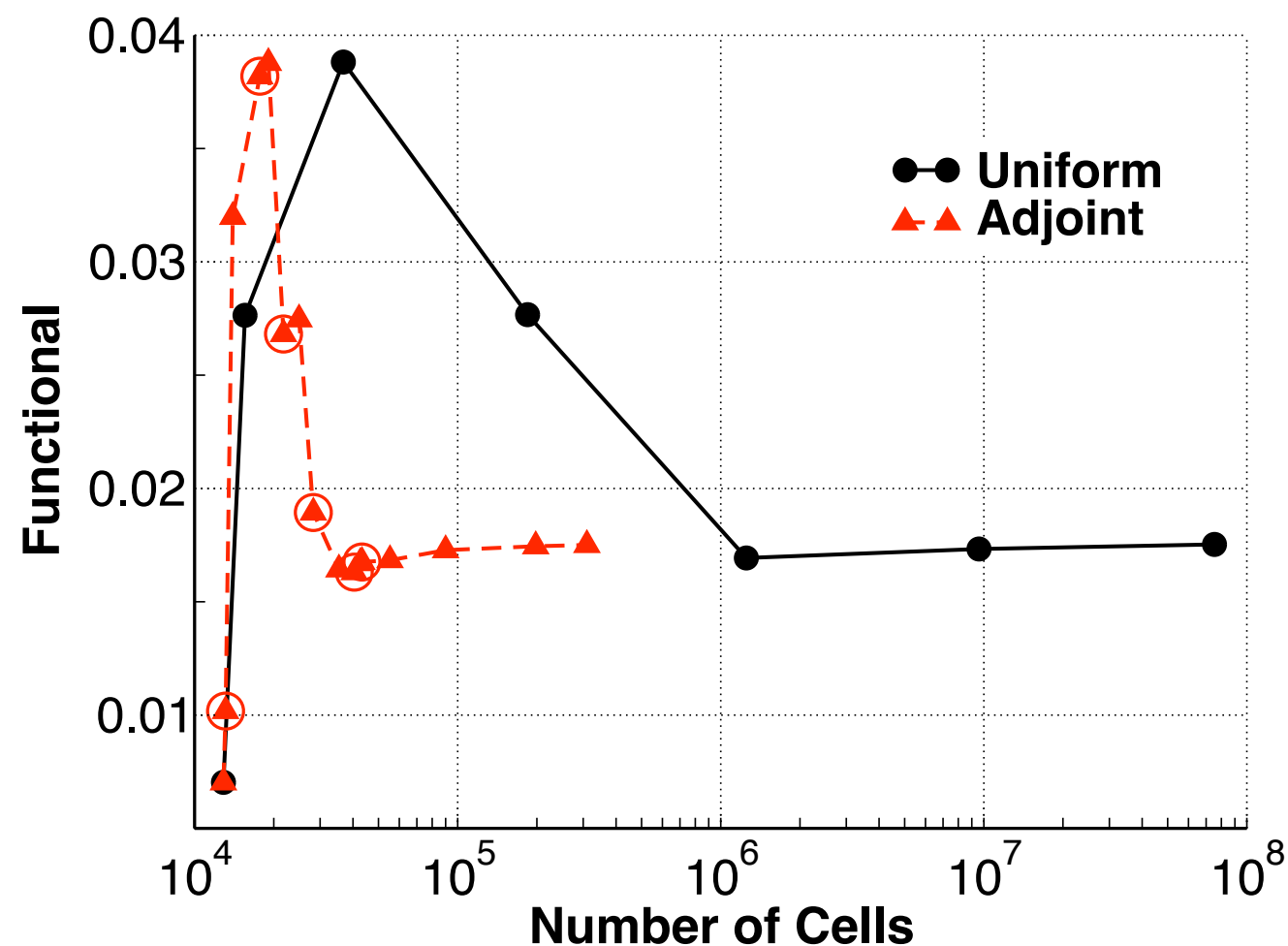
14 Cycles; 310k Cells



Mach contours, $M_{\infty} = 4$, $\alpha = 20^{\circ}$



Case A: Functional and Error Convergence



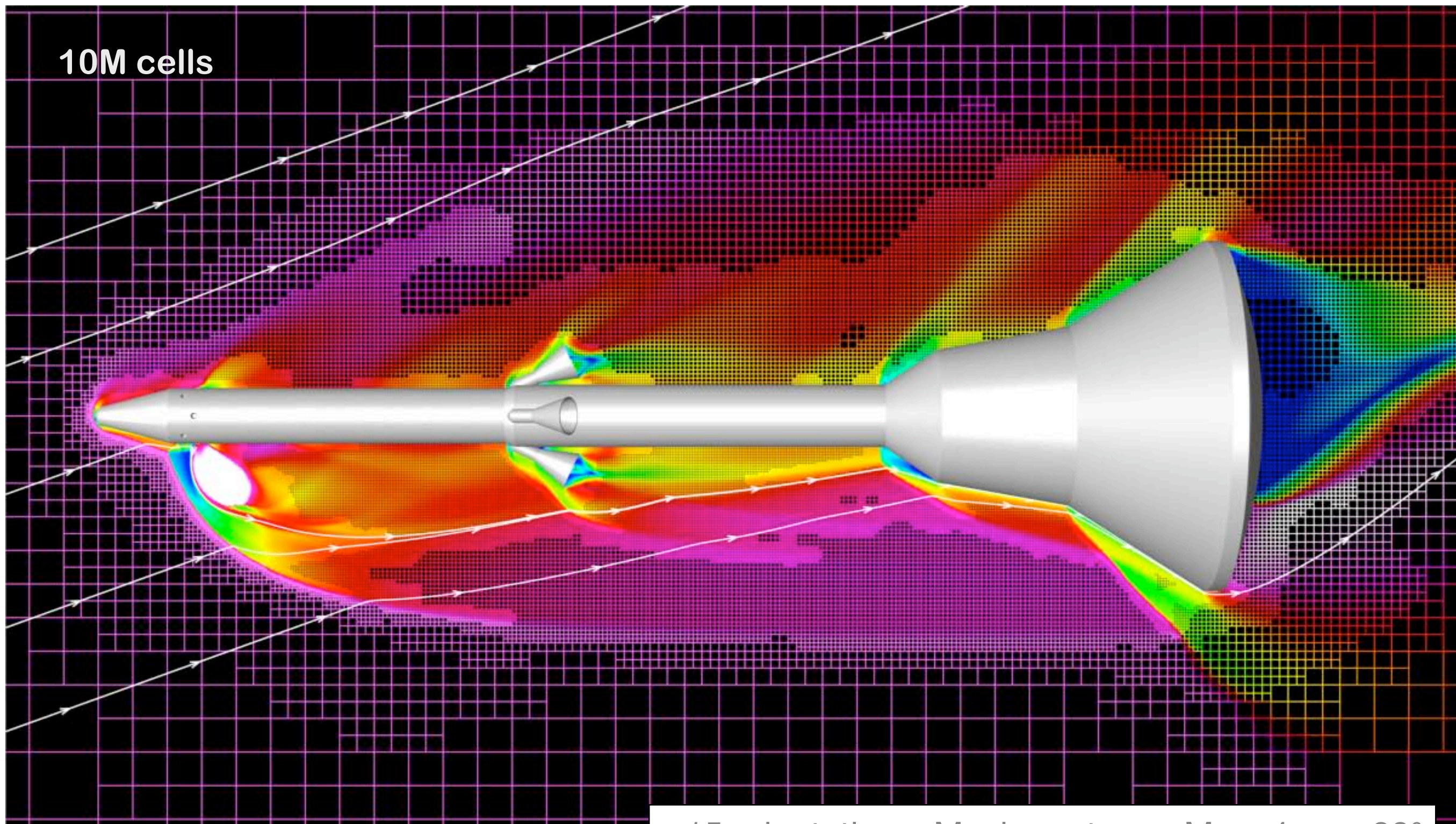
- Difference in functional values is below 0.05% on finest mesh
- Two orders-of magnitude savings in total number of cells
- Adaptive computation required just 9 minutes of wall-clock time on an 8-core Intel Xeon desktop

Case B

Final mesh and solution on symmetry plane



10M cells



15 adaptations, Mach contours, $M_\infty = 4$, $\alpha = 20^\circ$

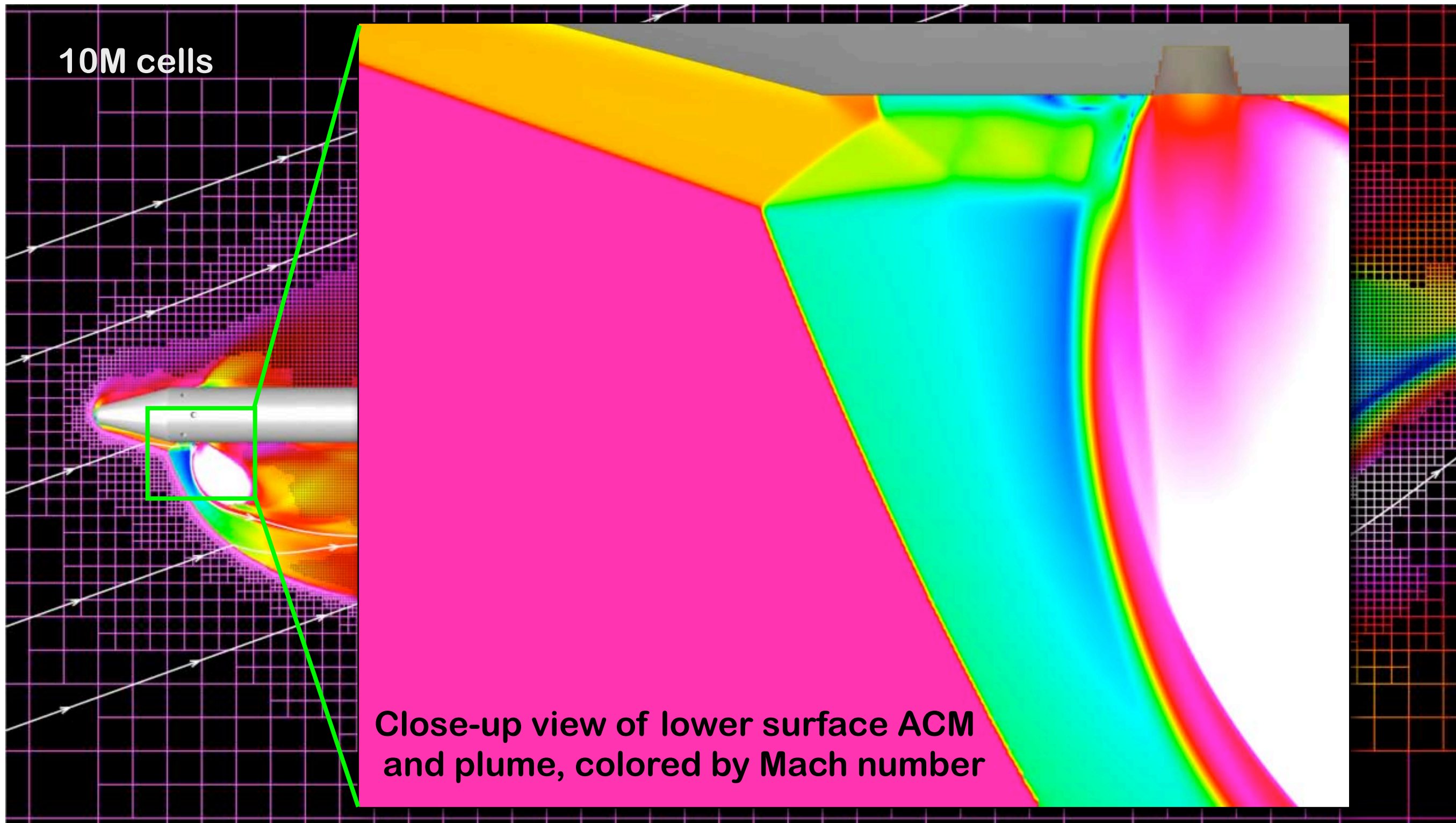
Case B

Type IV Shock-Shock Interference



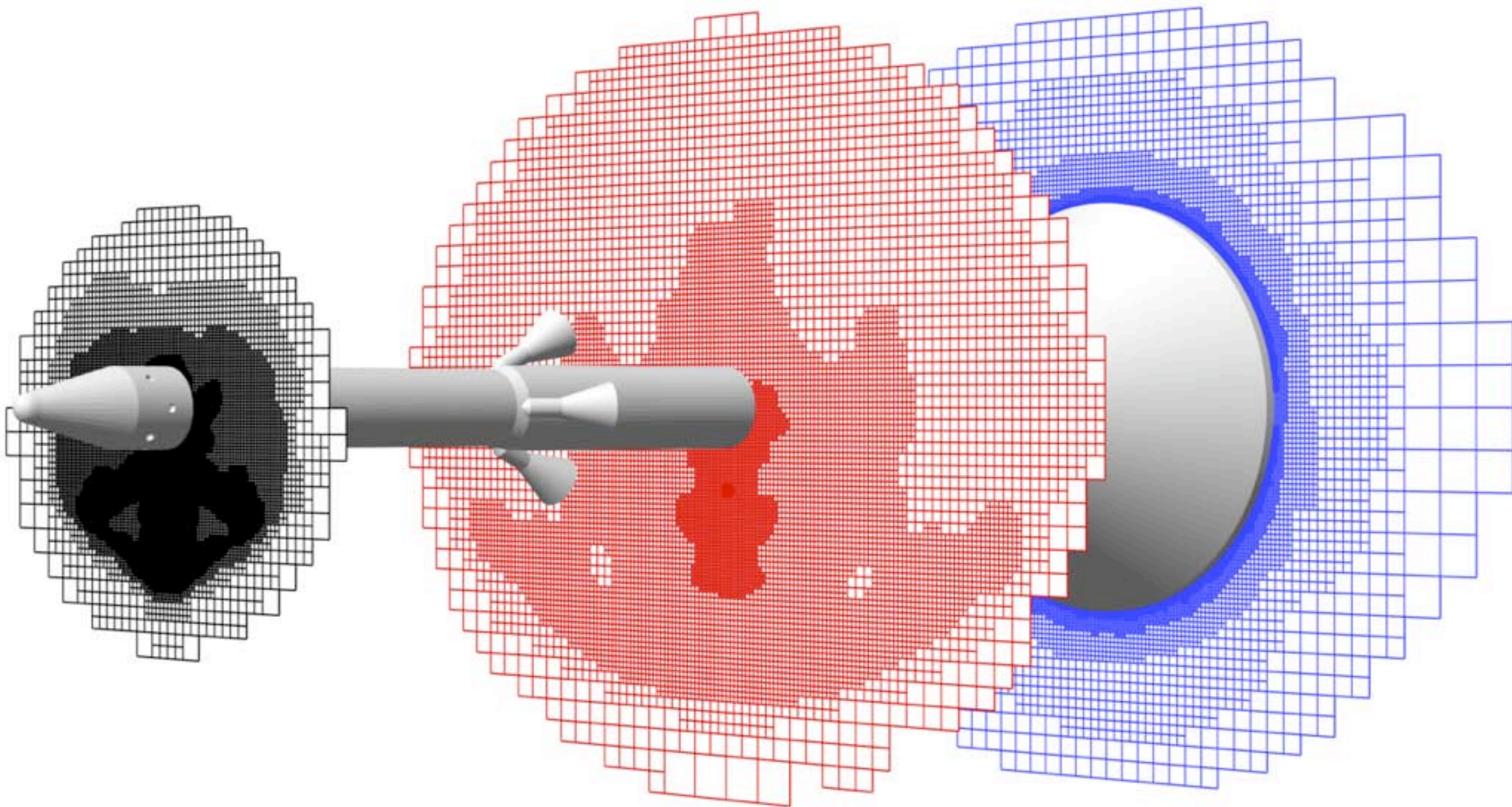
10M cells

Close-up view of lower surface ACM
and plume, colored by Mach number



Case B

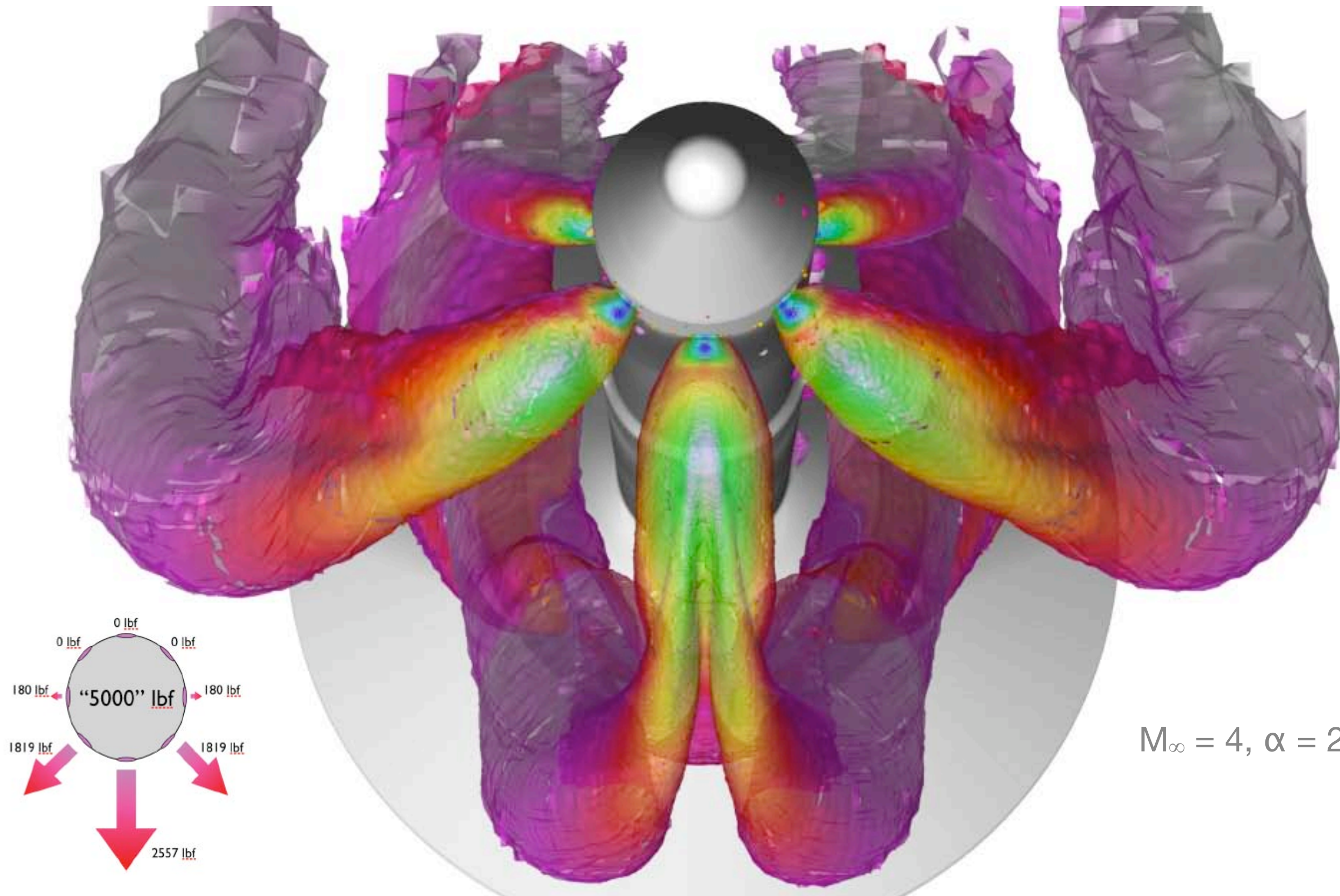
Final mesh at various x-stations



15 adaptations, $M_\infty = 4$, $\alpha = 20^\circ$

Case B

Front view of plumes on final mesh

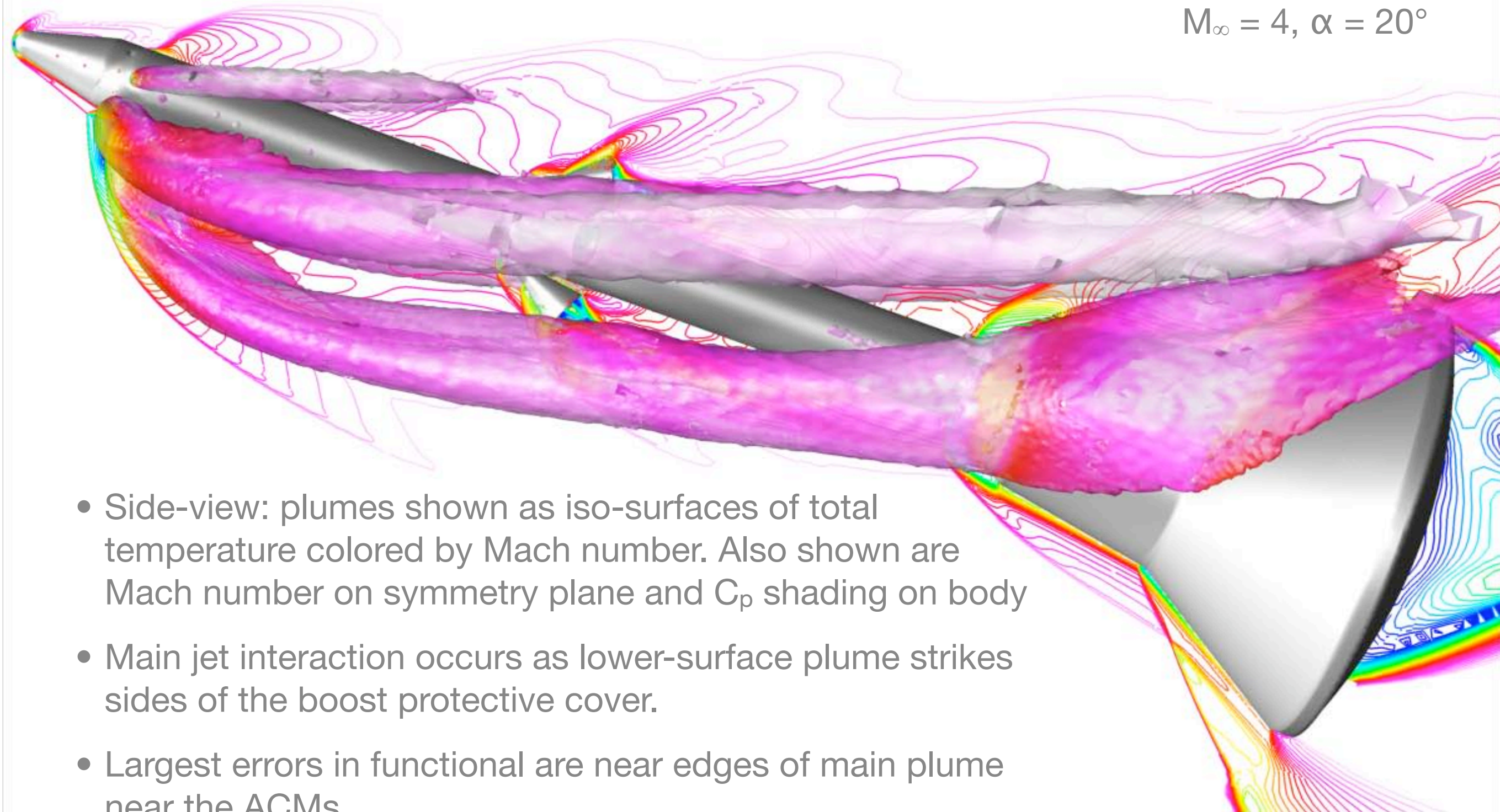


Launch Abort Vehicle

Plume Visualization on Final Mesh (~7.7M cells)



$$M_{\infty} = 4, \alpha = 20^{\circ}$$



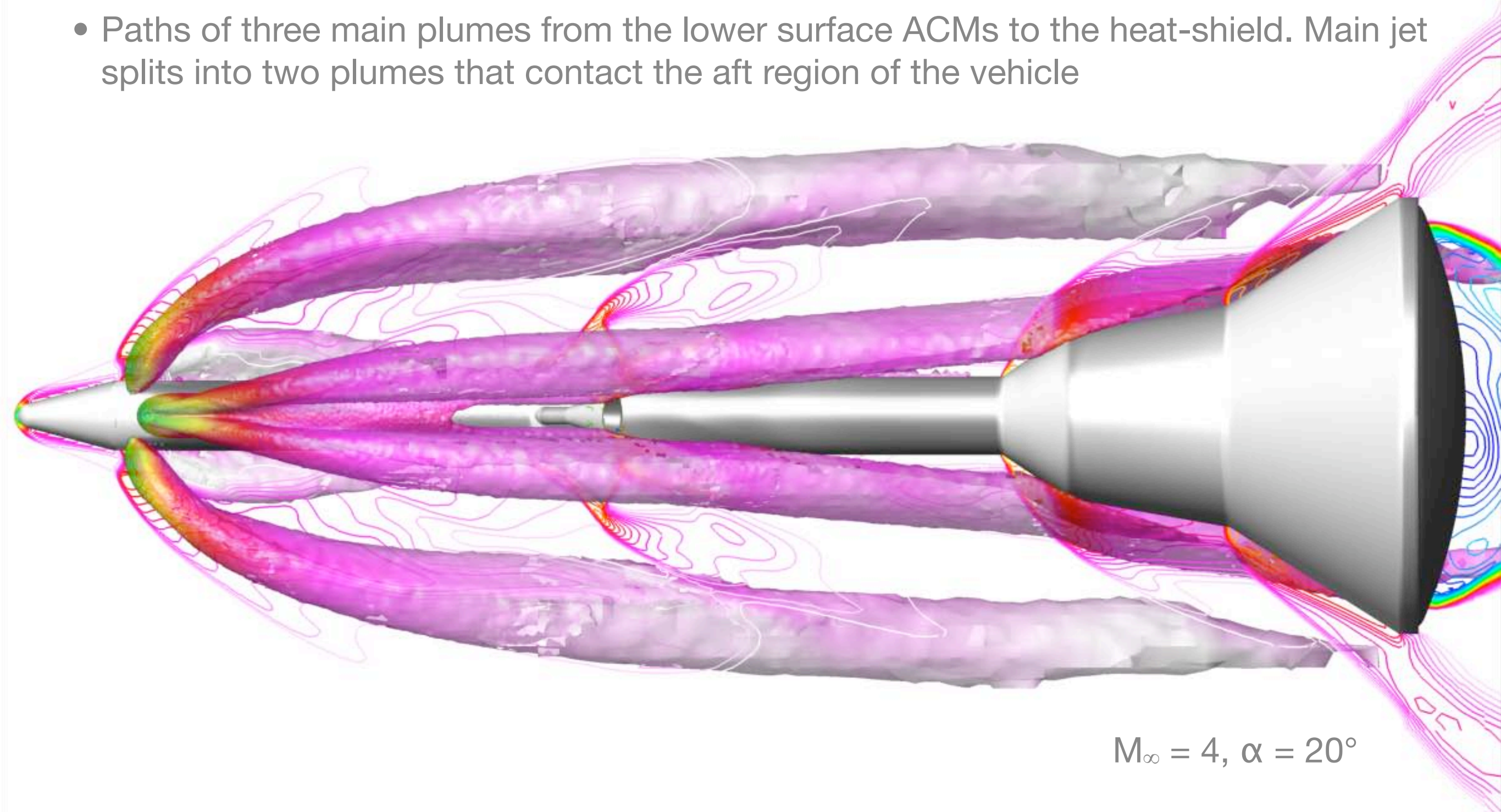
- Side-view: plumes shown as iso-surfaces of total temperature colored by Mach number. Also shown are Mach number on symmetry plane and C_p shading on body
- Main jet interaction occurs as lower-surface plume strikes sides of the boost protective cover.
- Largest errors in functional are near edges of main plume near the ACMs

Launch Abort Vehicle

Bottom view of plumes on final mesh



- Paths of three main plumes from the lower surface ACMs to the heat-shield. Main jet splits into two plumes that contact the aft region of the vehicle

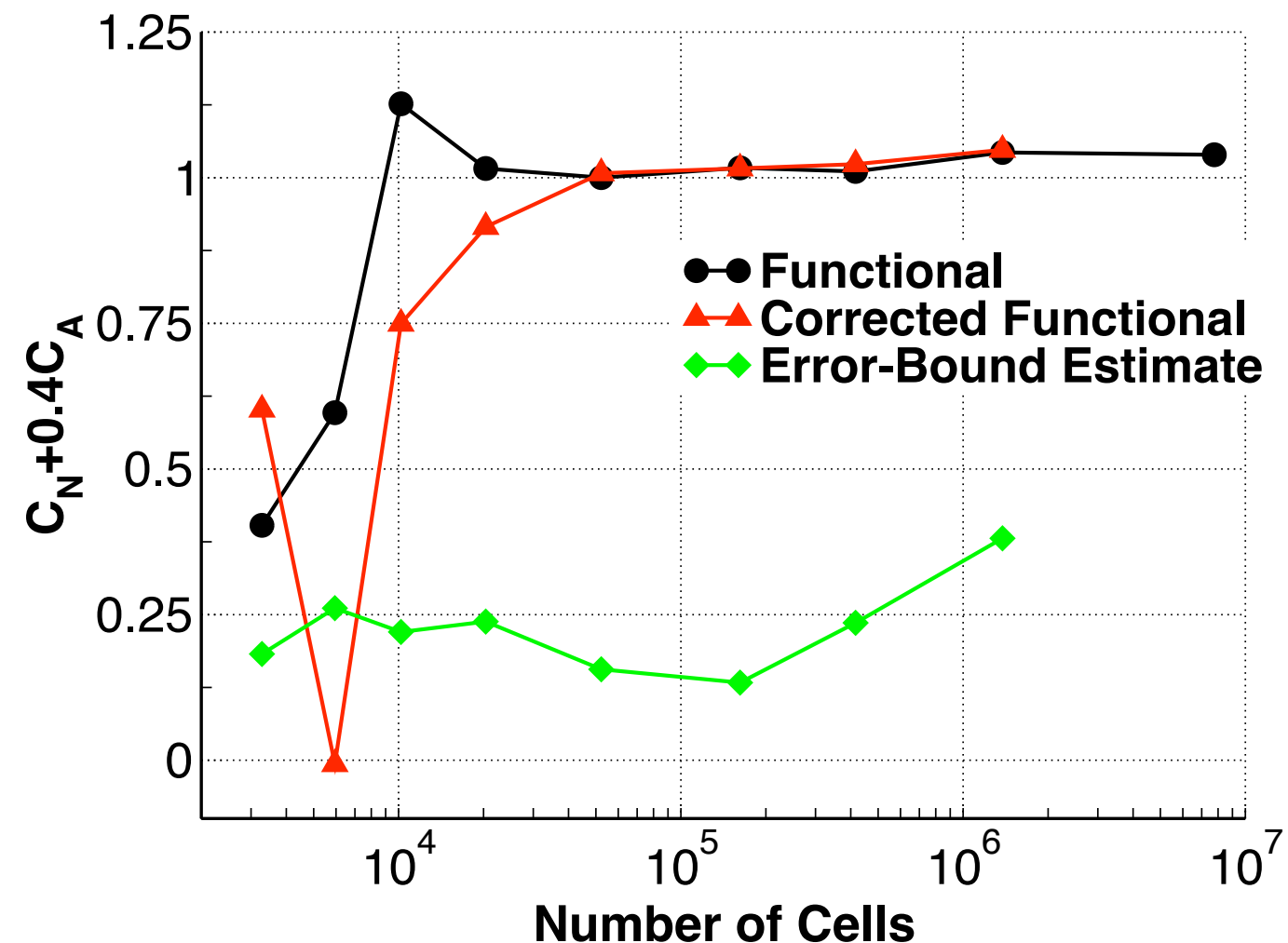


$$M_{\infty} = 4, \alpha = 20^{\circ}$$

Launch Abort Vehicle Functional Convergence



- Determination of plume paths and appropriate refinement of plume edges is not possible *a-priori*, yet these features determine the “aerodynamic shape” of the vehicle
- Adjoint error analysis identifies regions where jet interaction effects are important for the computation of aerodynamic coefficients and triggers mesh refinement
- Functional convergence settles down at ~1M cells, however, additional research is required to improve estimates of the error-bound



Results

Focus on Applications



Part A. Accuracy

- Launch Abort Vehicle with jets - uniform mesh refinement study

Part B. Efficiency

- Sonic-boom signature test case - computational cost summary

Part C. Databases

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- Launch Abort Vehicle with Jettison Motor plumes

69° Swept Delta Wing-Body

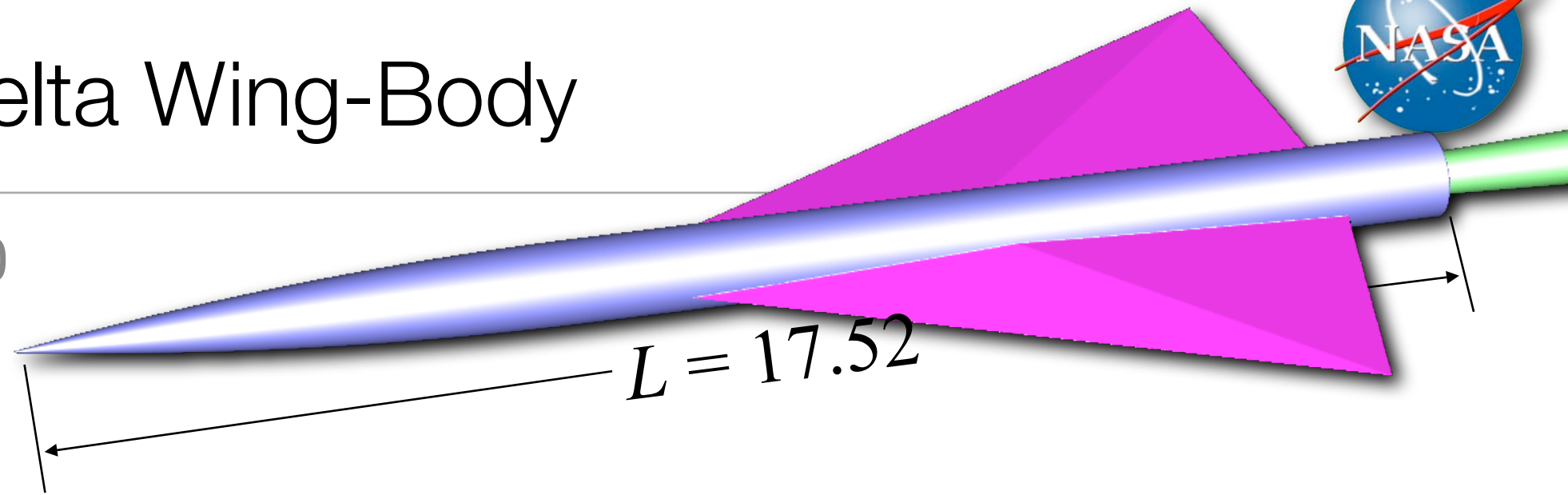


- NASA TN D-7160

- ▶ $M_\infty = 1.68$

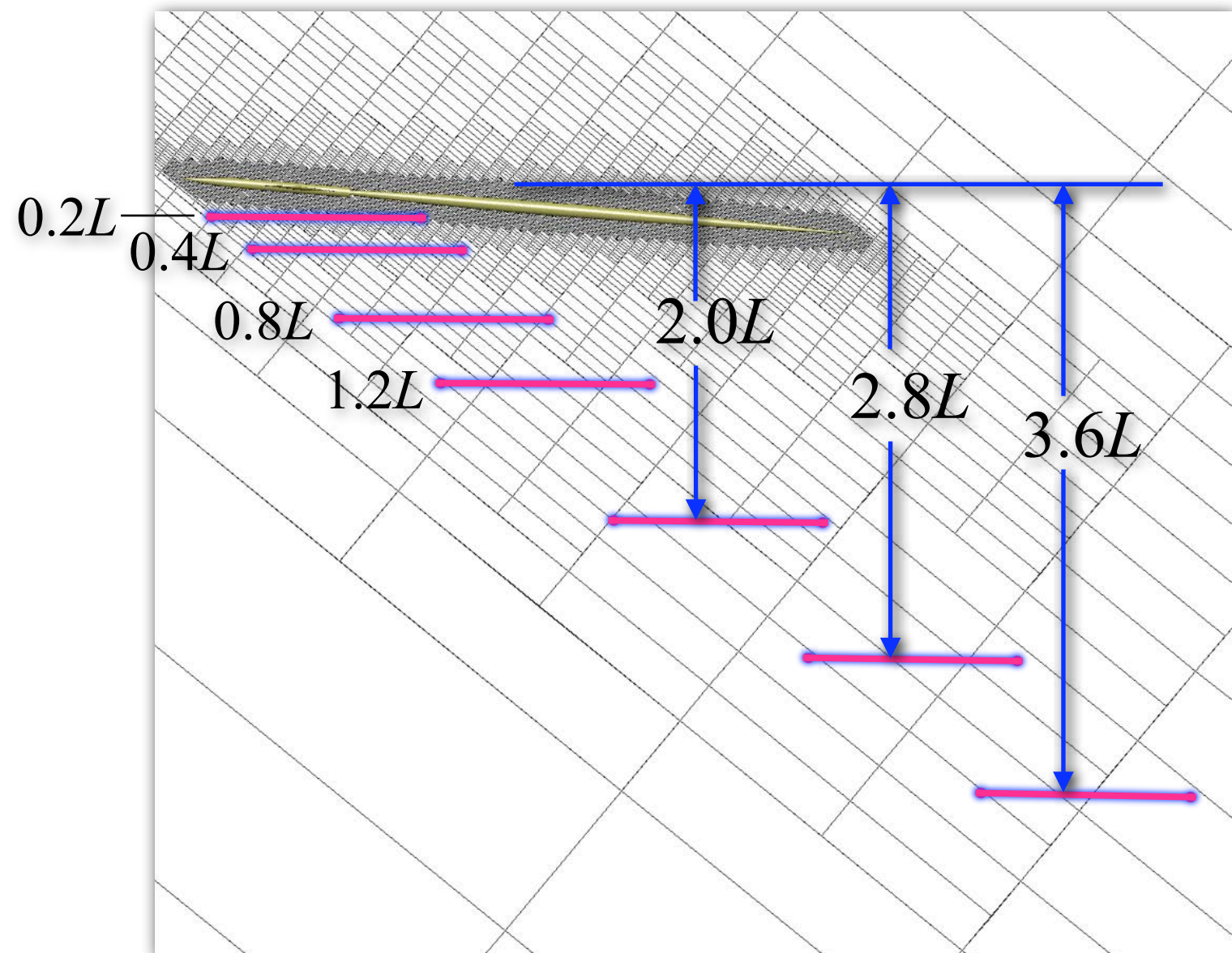
- ▶ $\alpha = 4.74^\circ$

- ▶ Sensor offset, $h/L = 3.6$ & $\{0.2, 0.4, 0.8, 1.2, 2.0, 2.8\}$



- Initial mesh ~ 22 k cells

$$J_s = \int_0^L \left(\frac{\Delta p}{p_\infty} \right)^2 ds$$

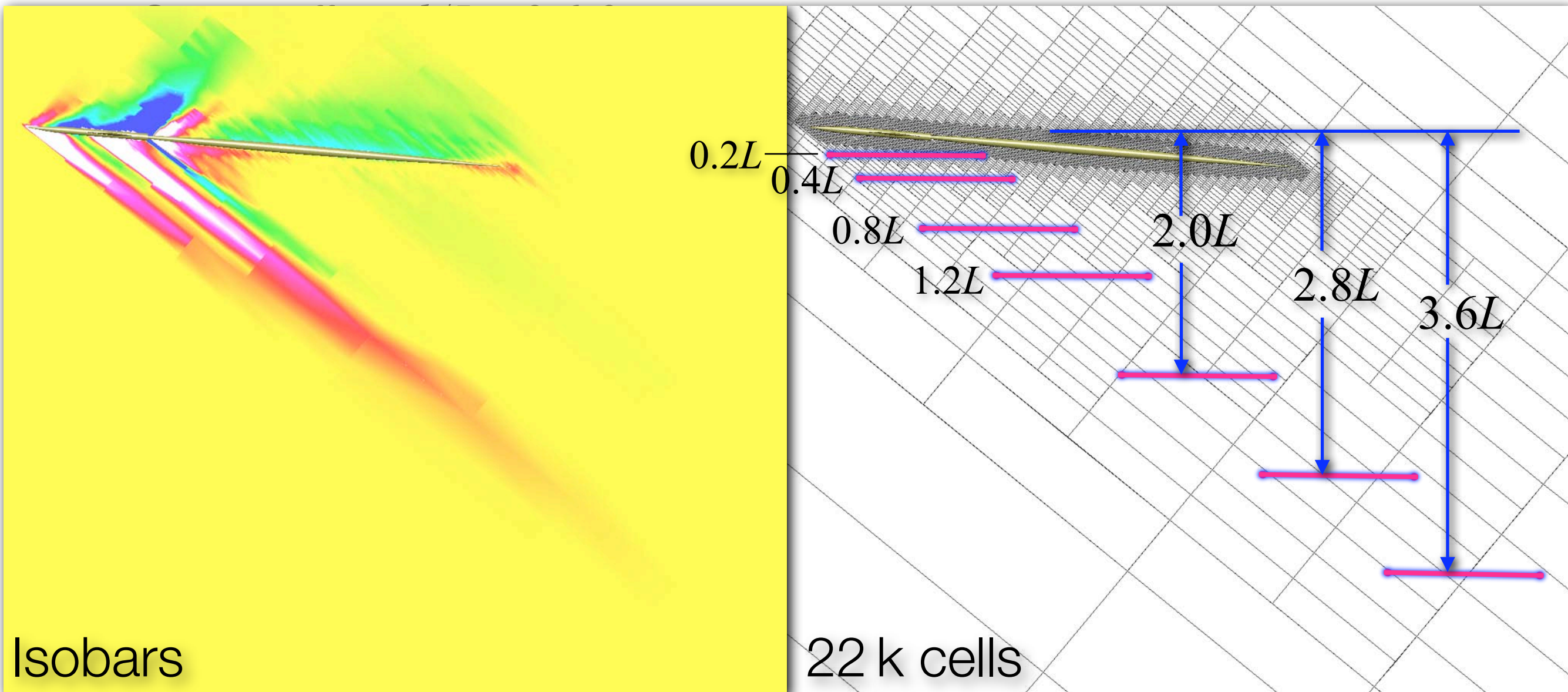
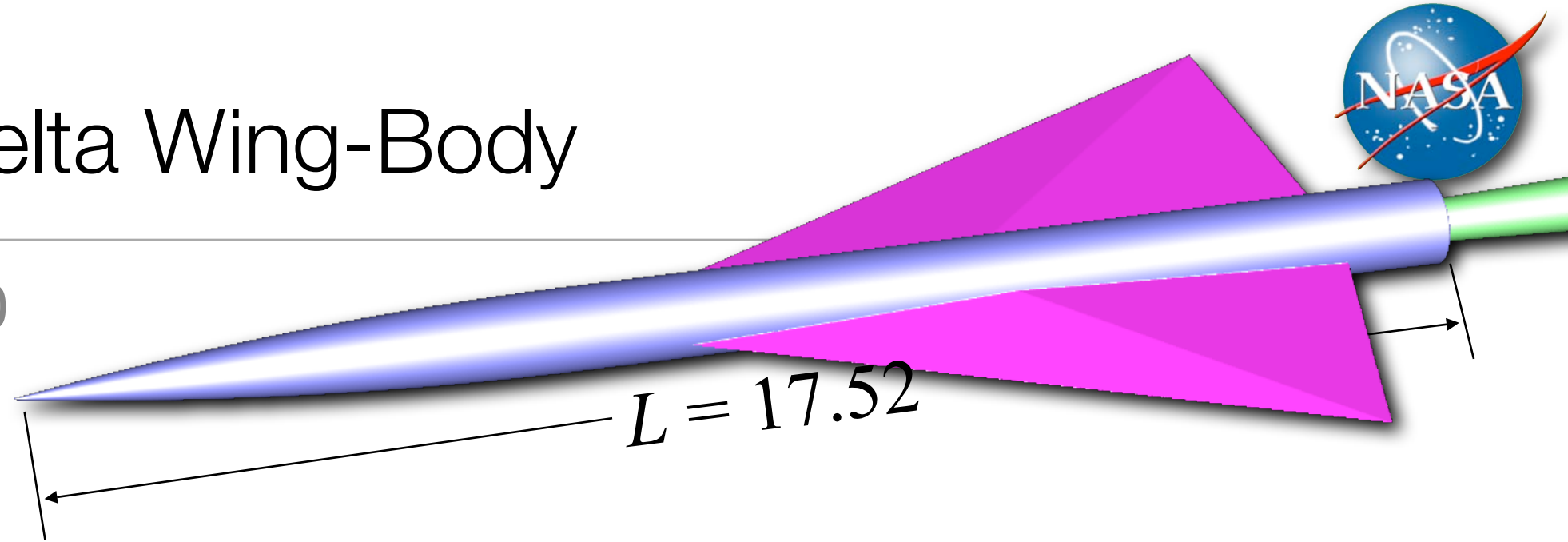


69° Swept Delta Wing-Body

- NASA TN D-7160

- ▶ $M_\infty = 1.68$

- ▶ $\alpha = 4.74^\circ$

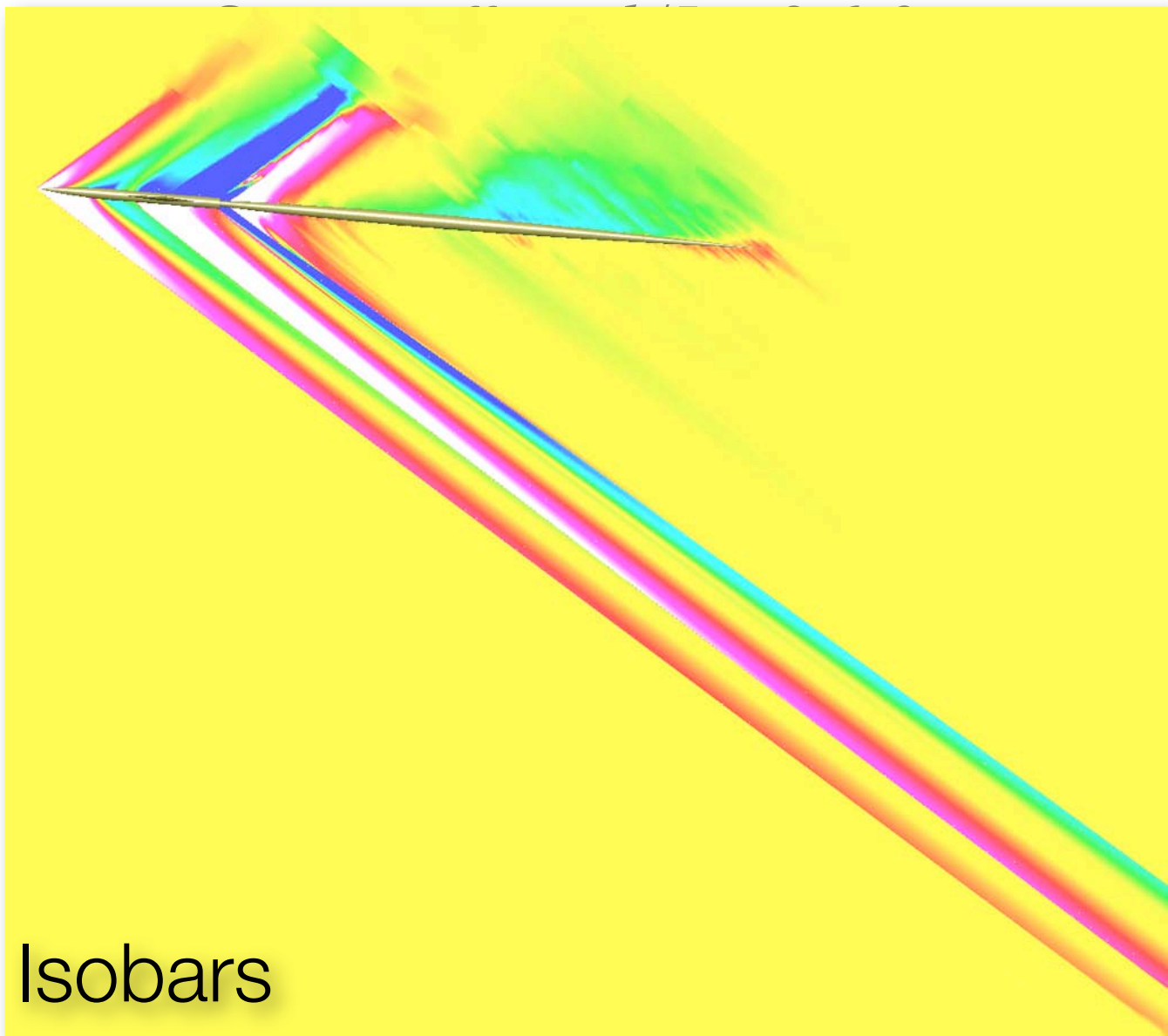
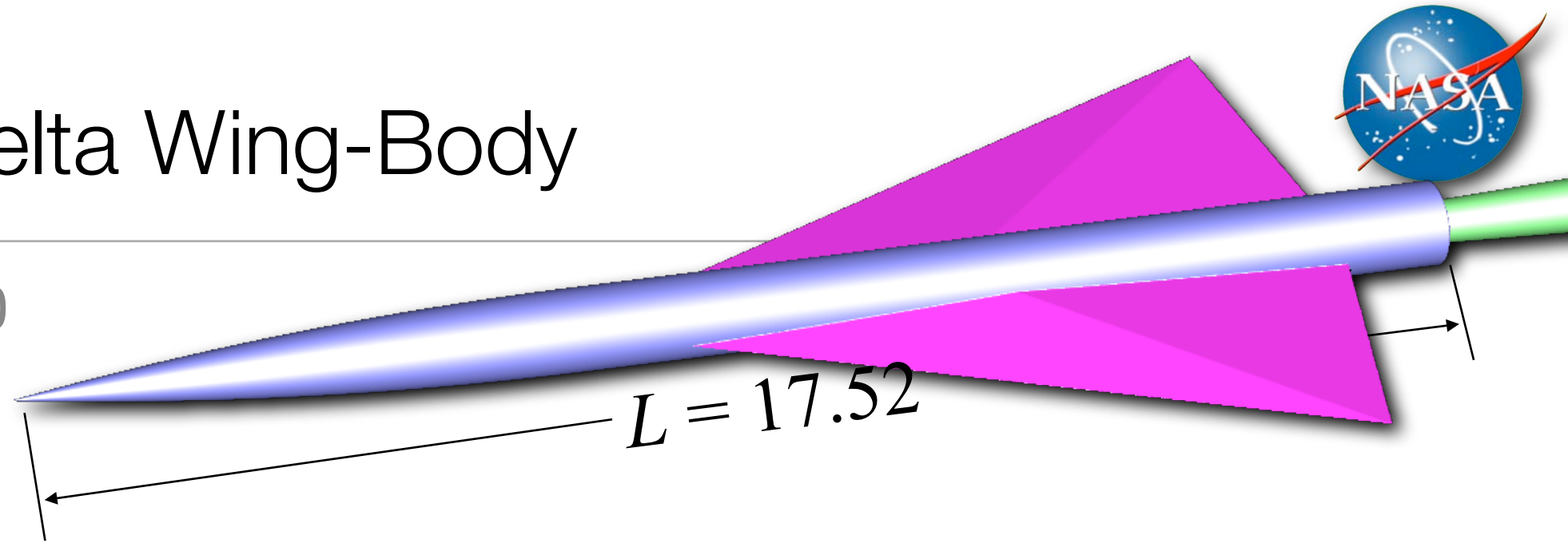


69° Swept Delta Wing-Body

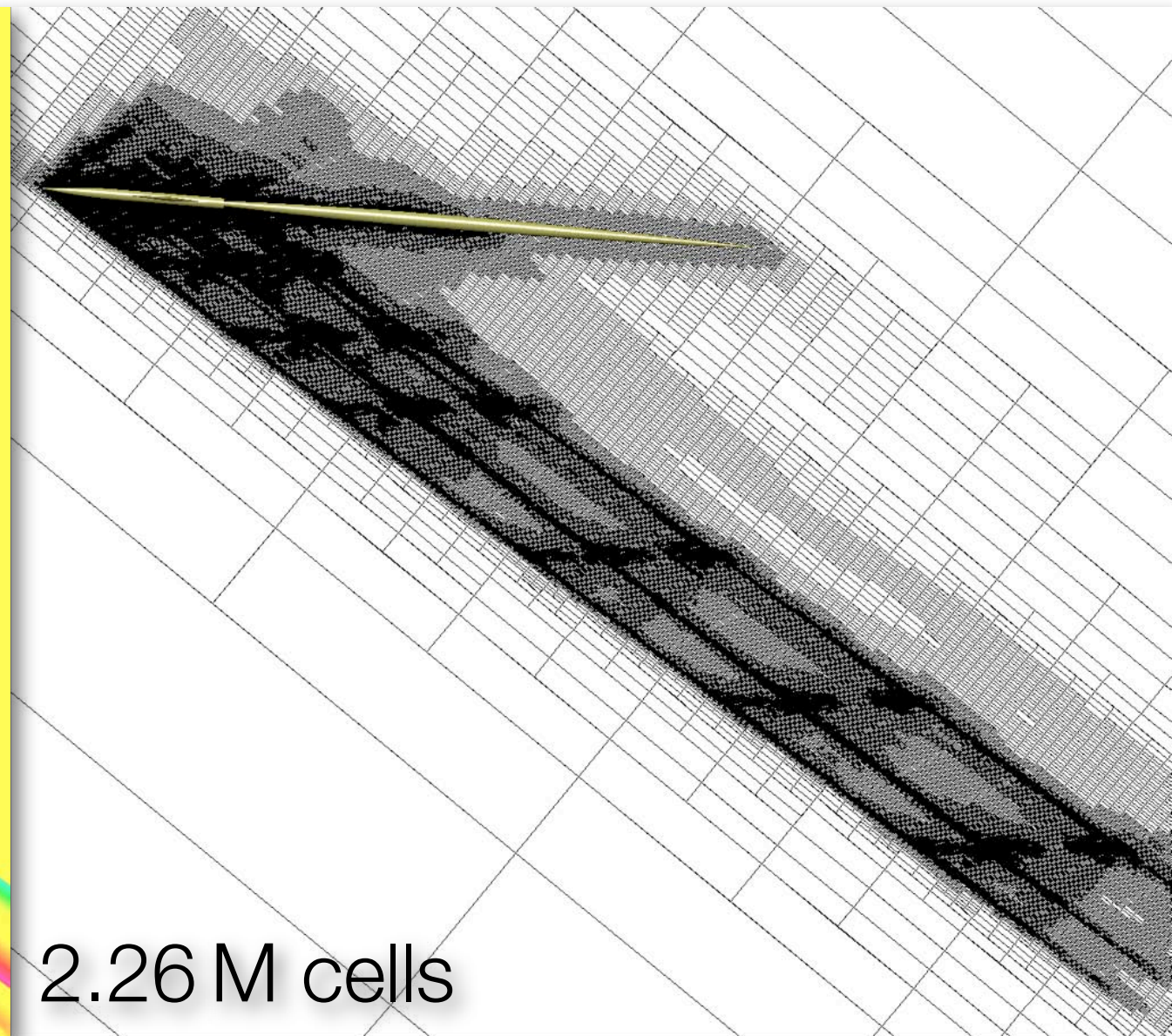
- NASA TN D-7160

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Isobars



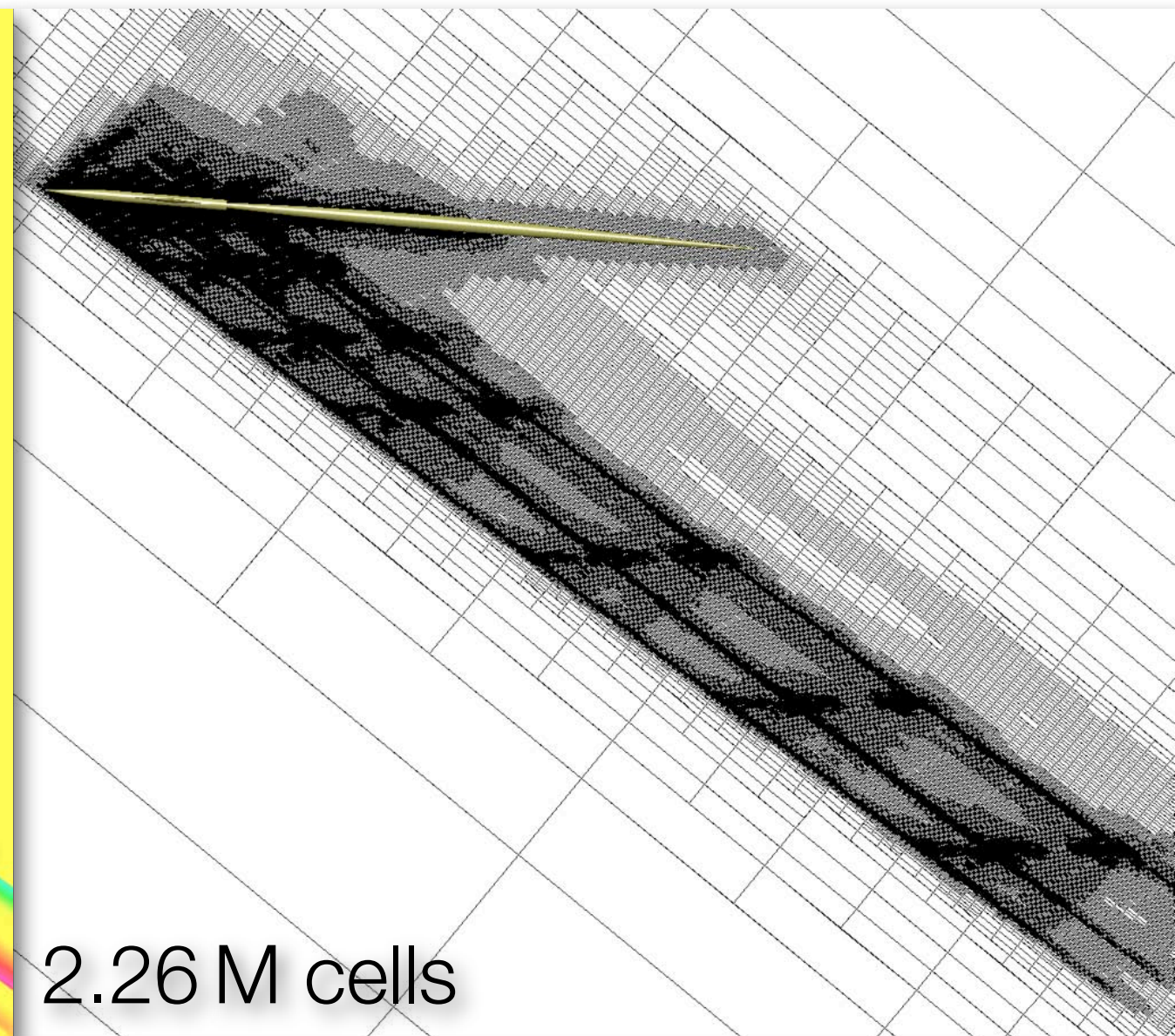
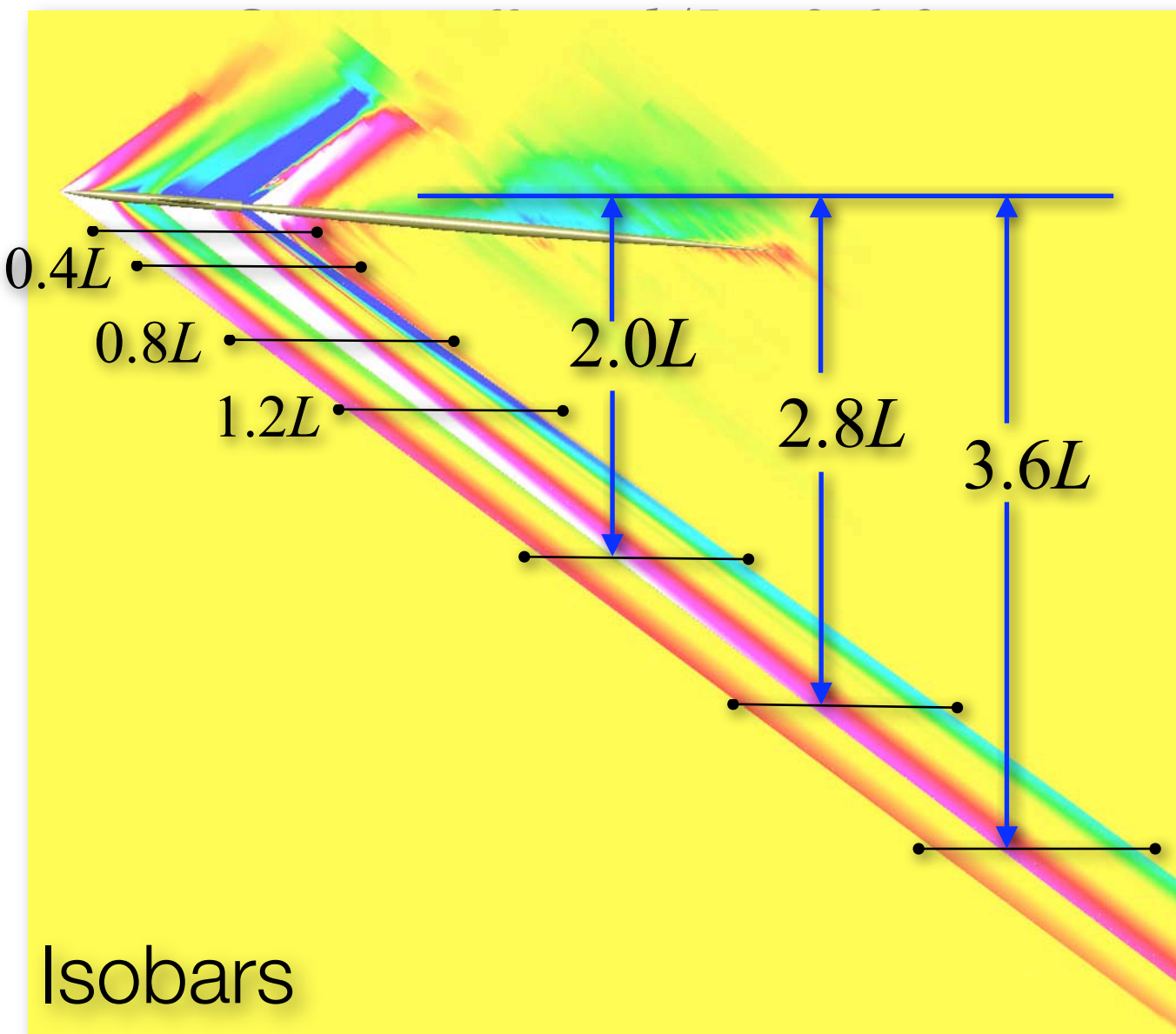
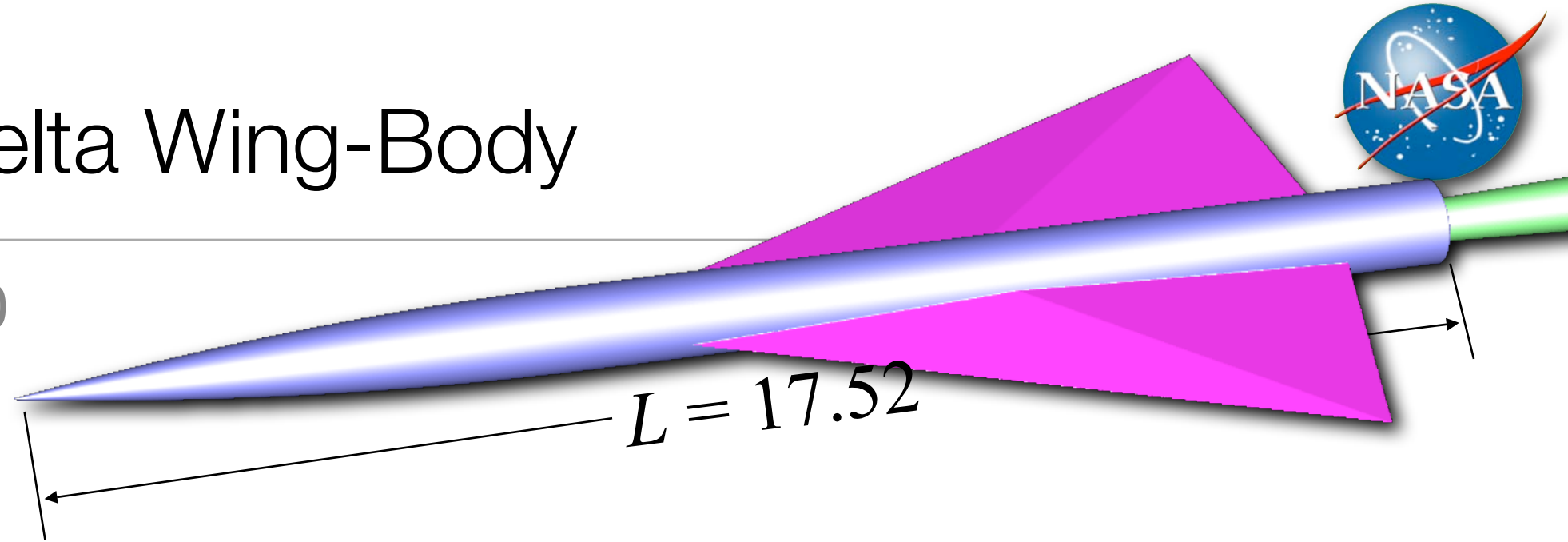
2.26 M cells

69° Swept Delta Wing-Body

- NASA TN D-7160

- ▶ $M_\infty = 1.68$

- ▶ $\alpha = 4.74^\circ$

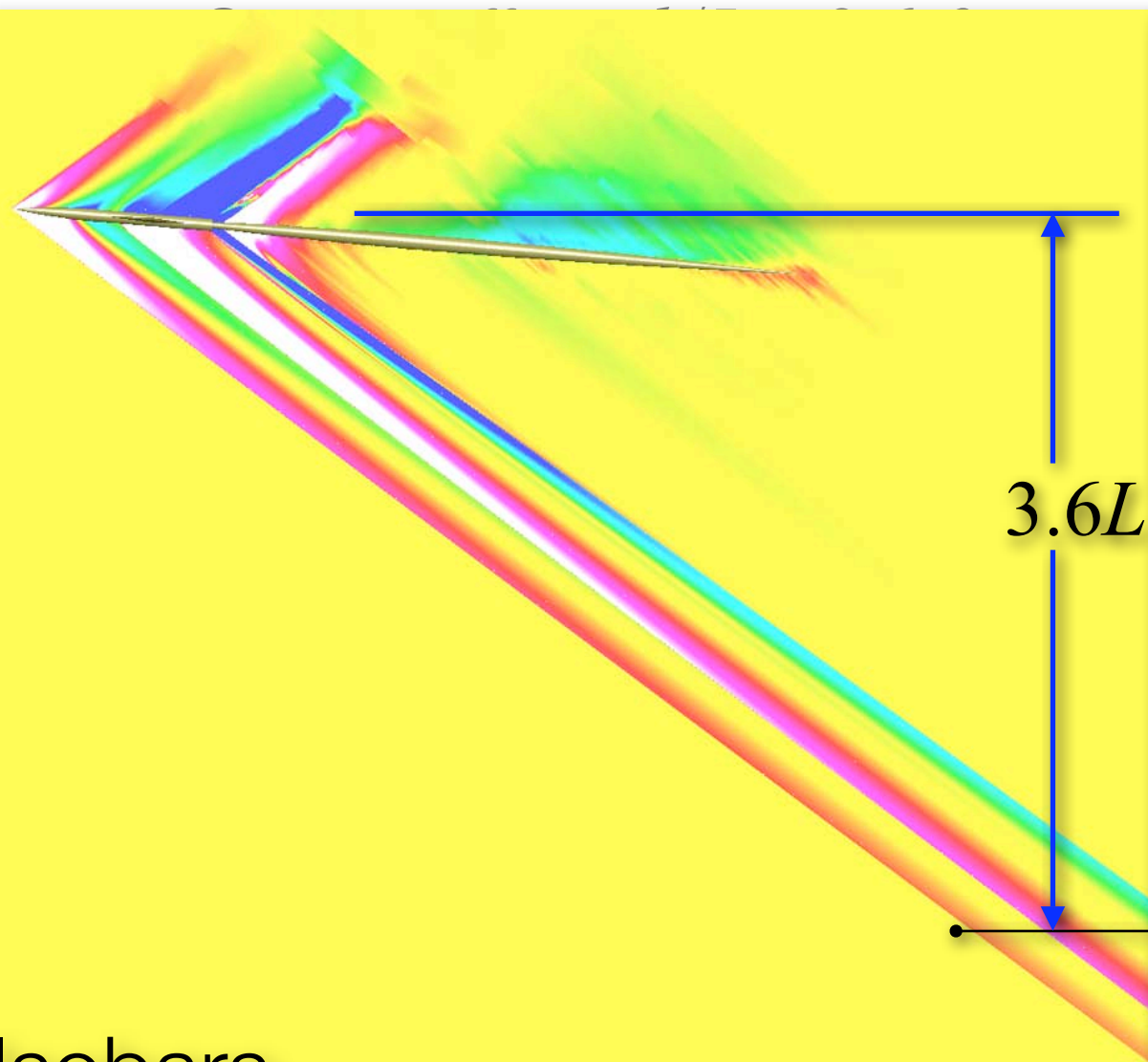
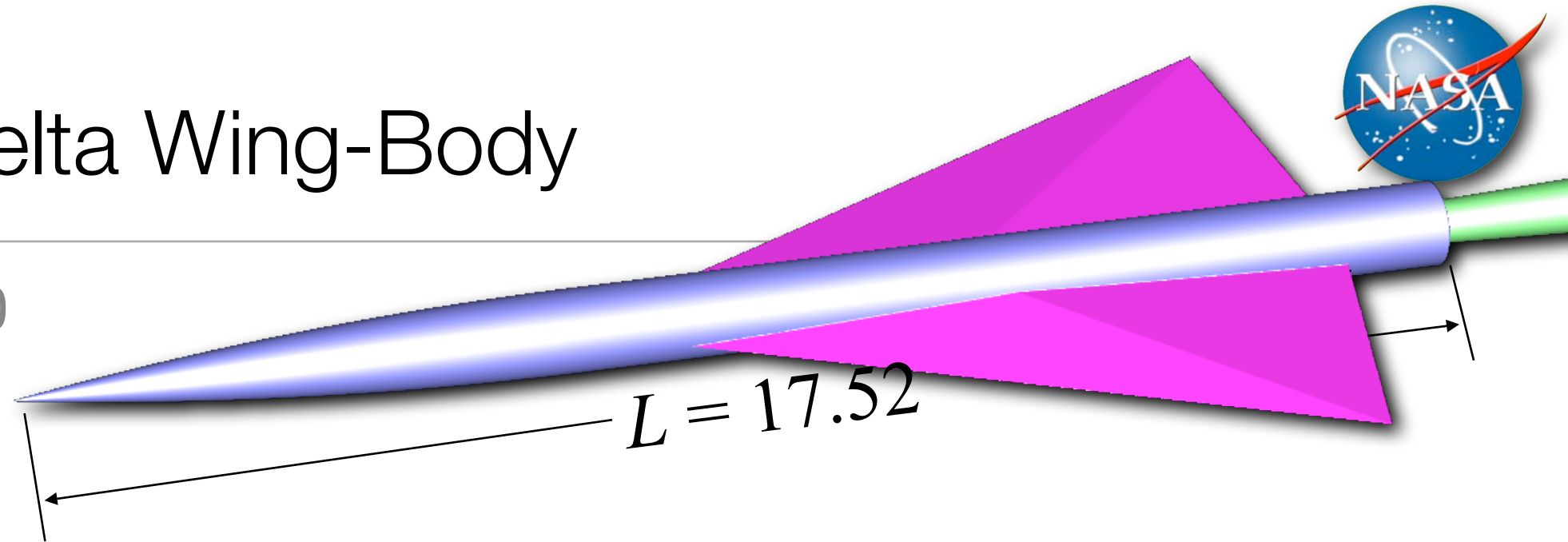


69° Swept Delta Wing-Body

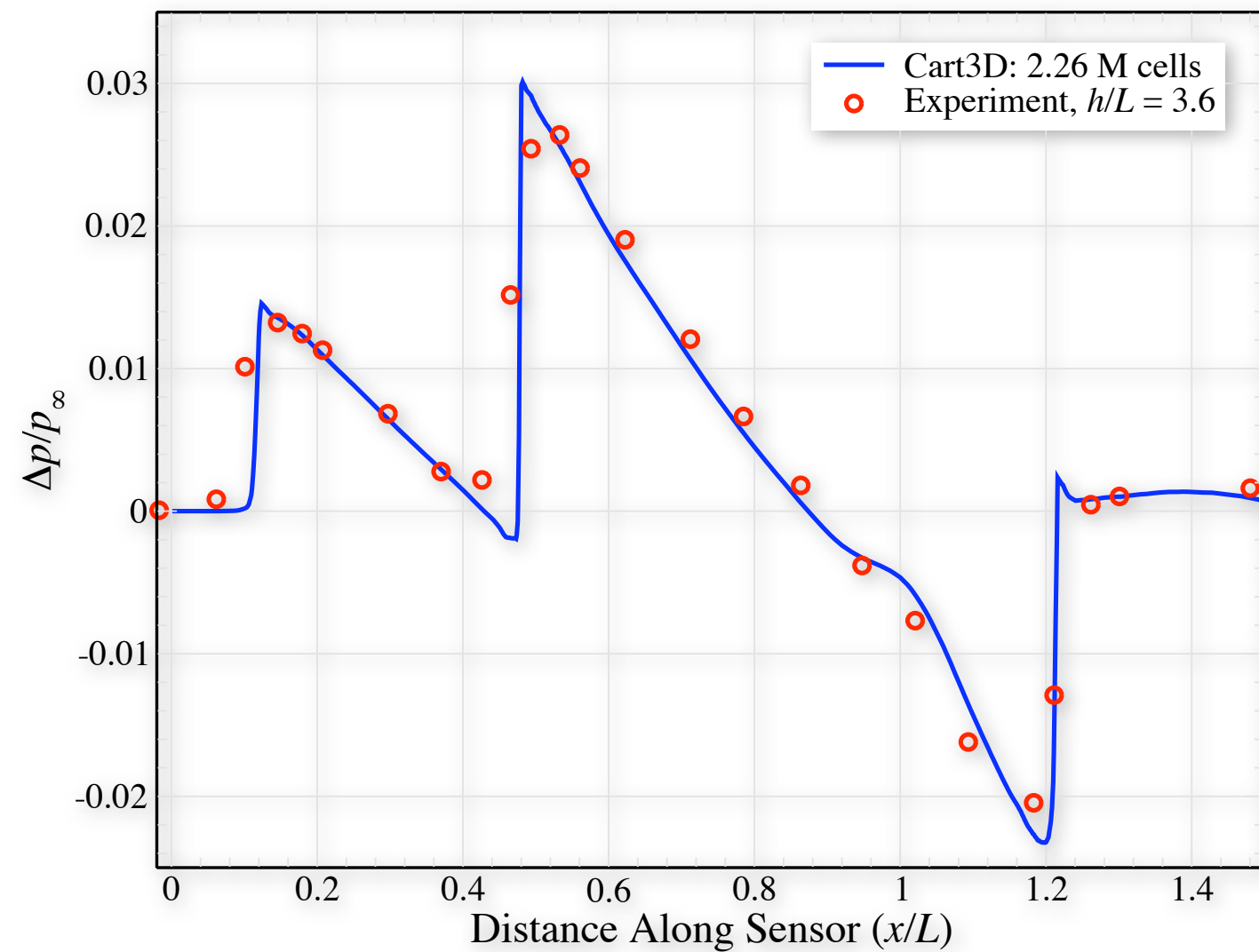
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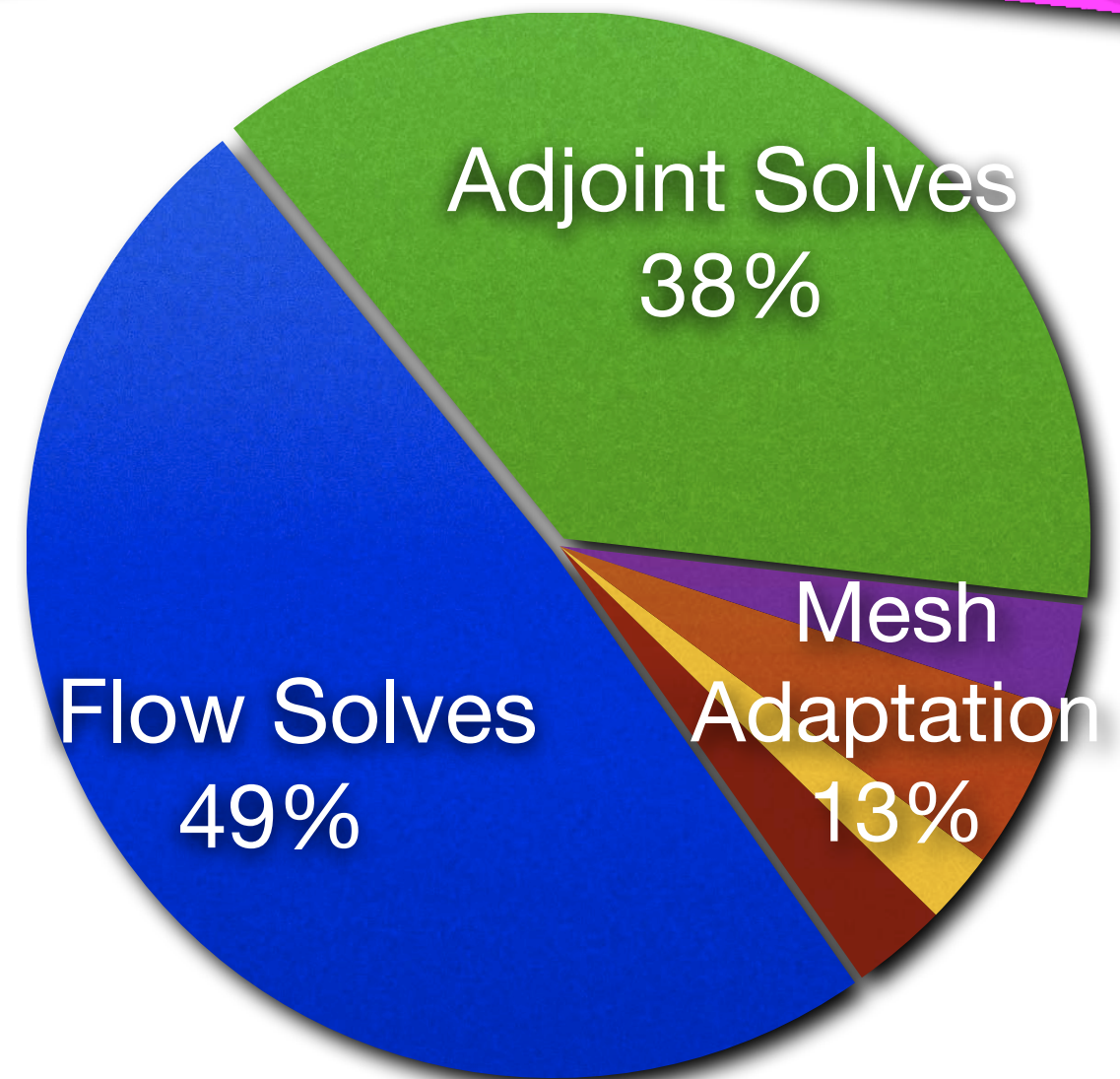
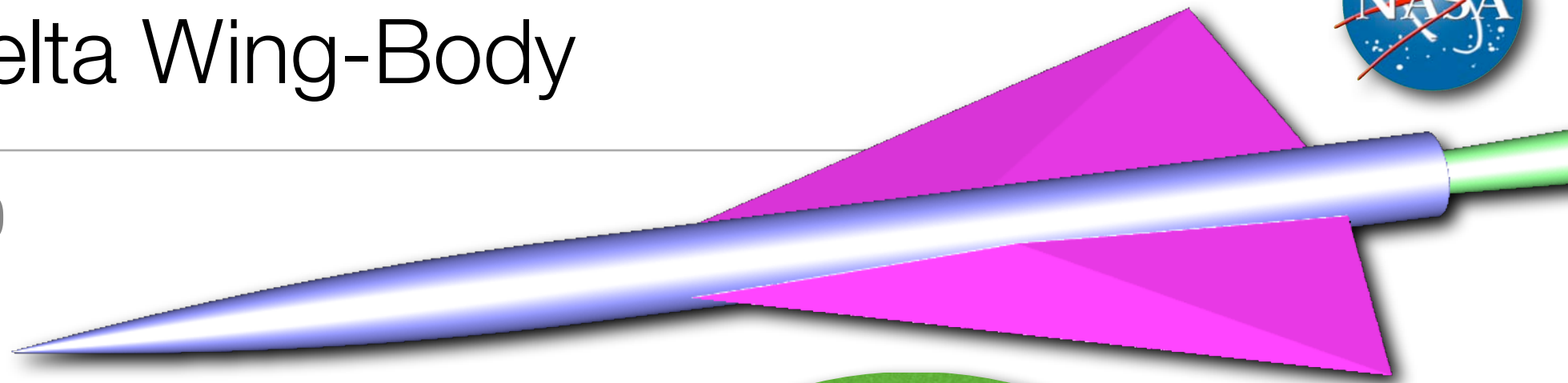
Isobars





69° Swept Delta Wing-Body

- NASA TN D-7160
 - ▶ $M_\infty = 1.68$
 - ▶ $\alpha = 4.74^\circ$
 - ▶ $h/L = \{.2, .4, .8, 1.2, 2.0, 2.8, 3.6\}$
- Simulation performed on desktop workstation
 - ▶ Dual quad-core (8 cores)
 - ▶ Intel Xeon, 3.2Ghz
 - ▶ 16 Gb memory
- Total simulation time 53 mins.
(all adaptations & mesh gen)



Total = 53 mins.

Results

Focus on Applications



Part A. Accuracy

- Launch Abort Vehicle with jets - uniform mesh refinement study

Part B. Efficiency

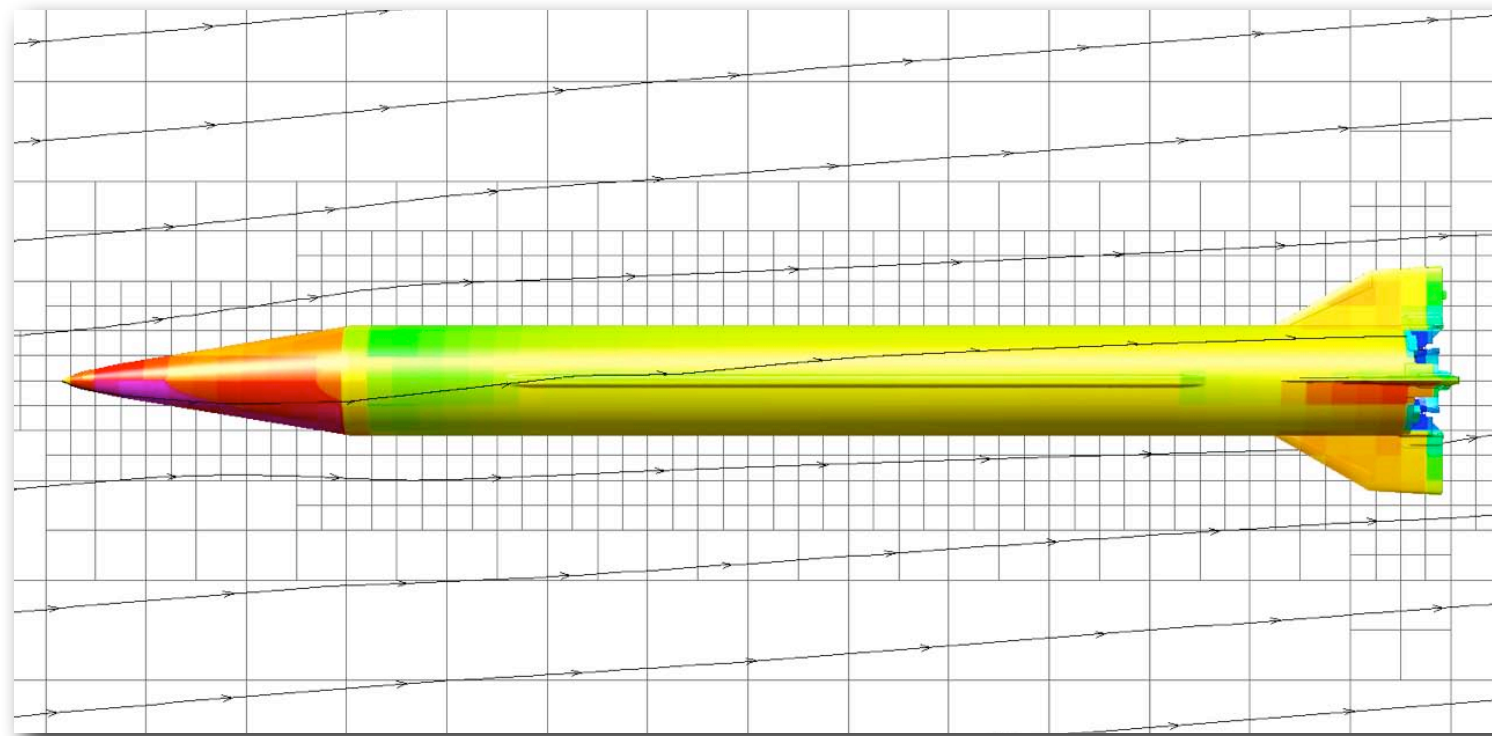
- Sonic-boom signature test case - computational cost summary

Part C. Databases

- Nozzle-Guide-Vane Missile
- Launch Abort Vehicle with Jettison Motor plumes

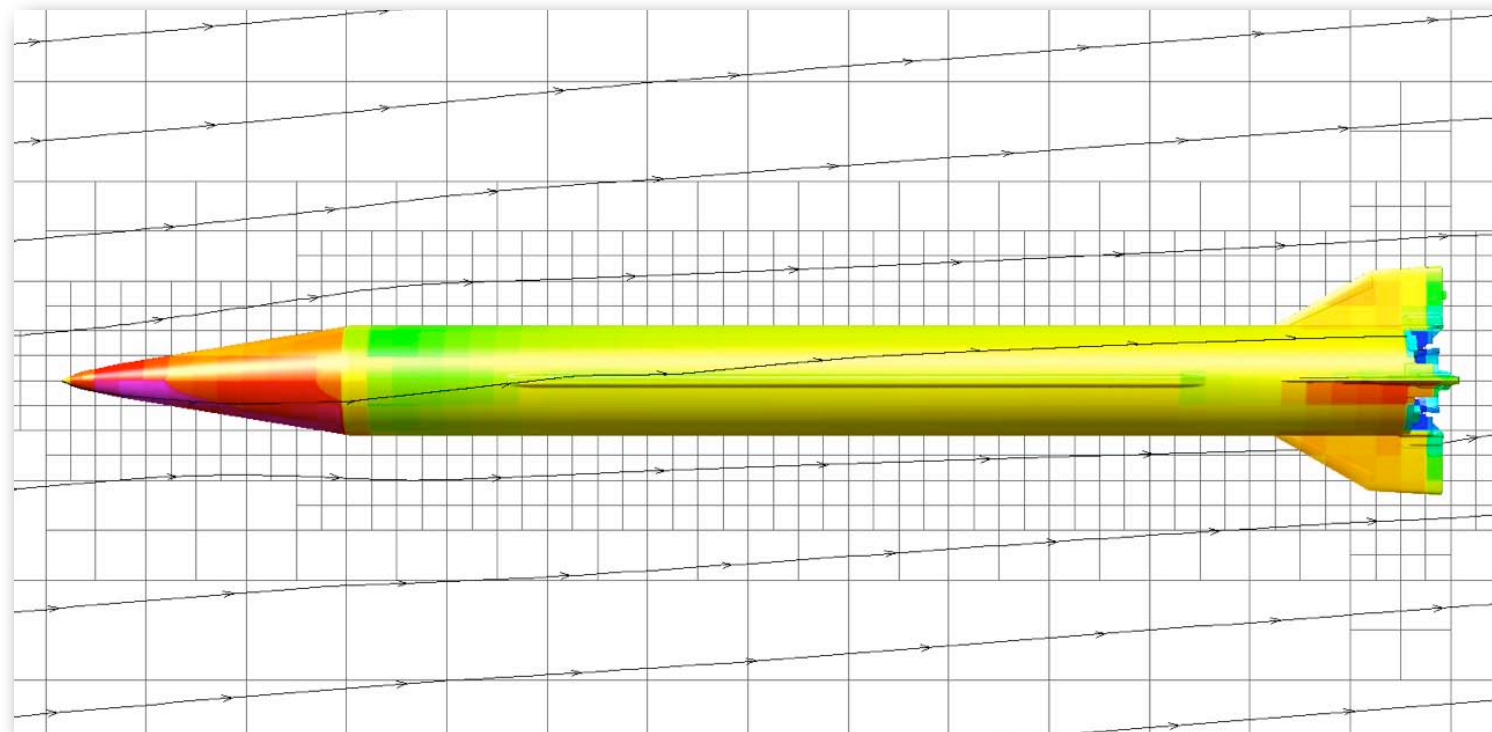
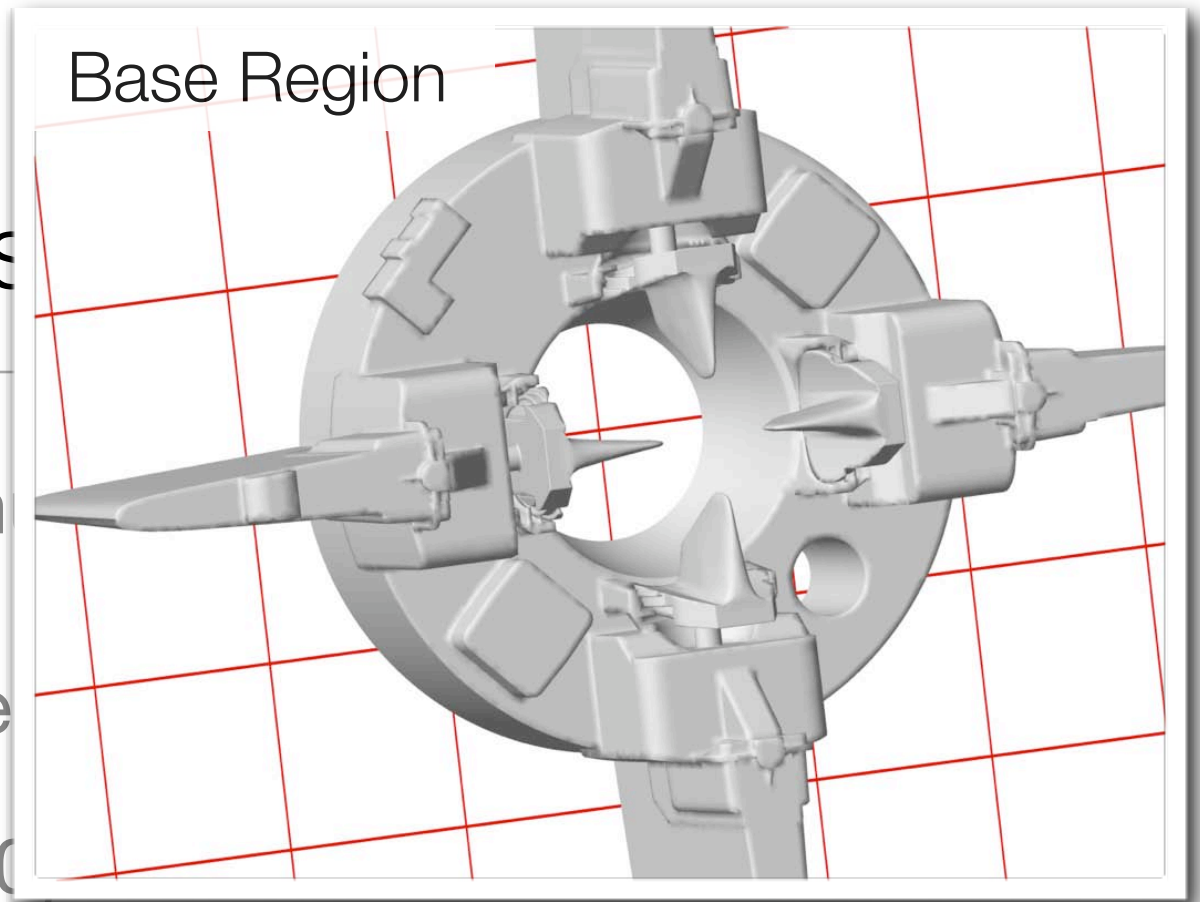
Error Controlled Aero Database

- Realistically complex model with plenum, guide vanes, etc.
- Perform (data blind) aero analysis over range of operating conditions
 - $M_\infty = \{0.5, 0.7, 0.9, 1.1, 1.3, 1.6, 2.0\}$
 - $\alpha = \{0^\circ, 5^\circ, 10^\circ, 15^\circ, 20^\circ\} = 35$ cases total
 - Output functional: $J = C_N + 0.1C_A$, TOL = 0.05
- Starting mesh has ~8000 cells



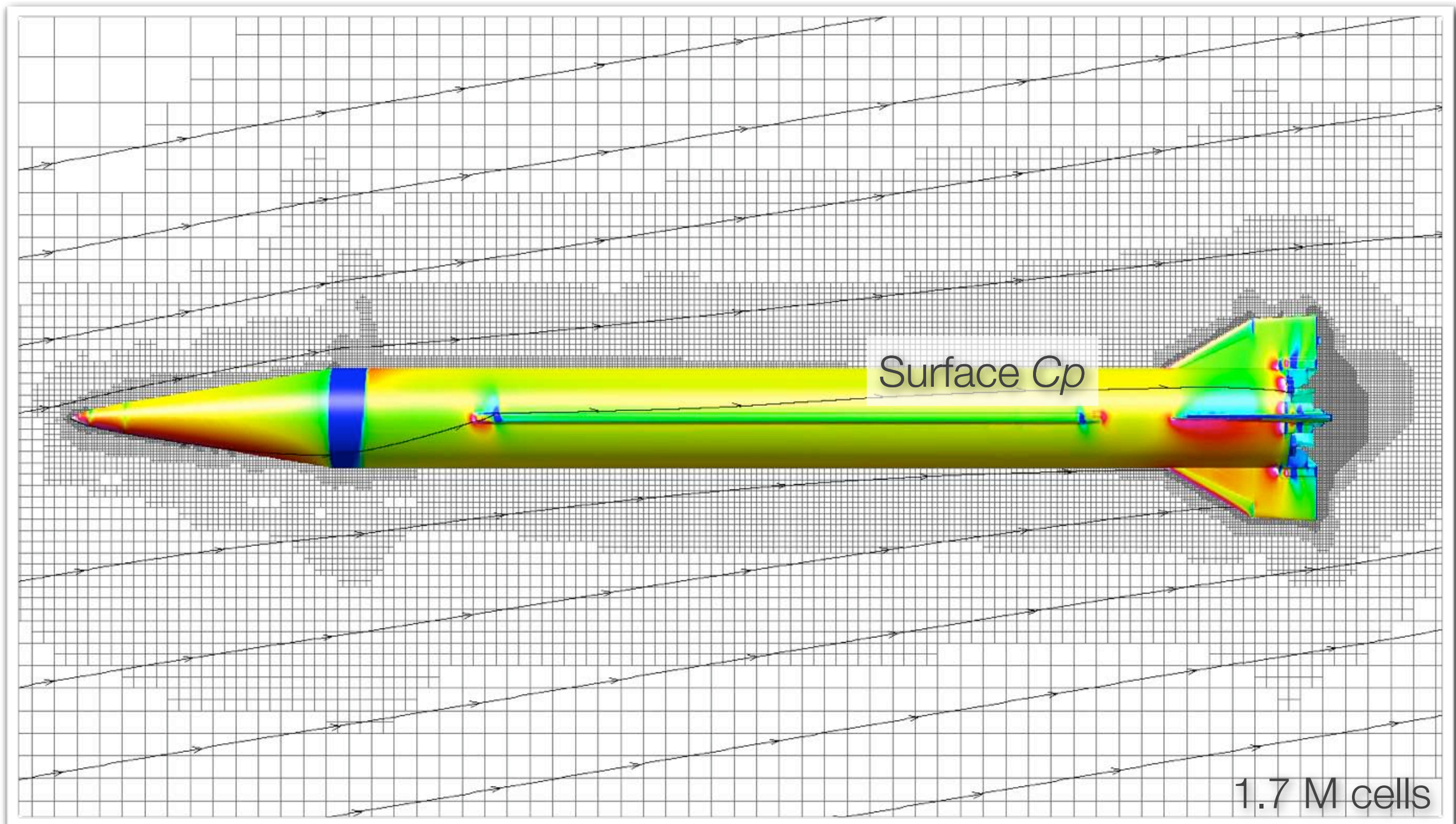
Error Controlled Aero Databas

- Realistically complex model with plenty of detail
- Perform (data blind) aero analysis over
 - $M_\infty = \{0.5, 0.7, 0.9, 1.1, 1.3, 1.6, 2.0\}$
 - $\alpha = \{0^\circ, 5^\circ, 10^\circ, 15^\circ, 20^\circ\} = 35$ cases total
 - Output functional: $J = C_N + 0.1C_A$, TOL = 0.05
- Starting mesh has ~8000 cells



Example Case

$$M_{\infty} = 0.9, \alpha = 10^{\circ}$$



Example Case

$$M_{\infty} = 0.9, \alpha = 10^{\circ}$$

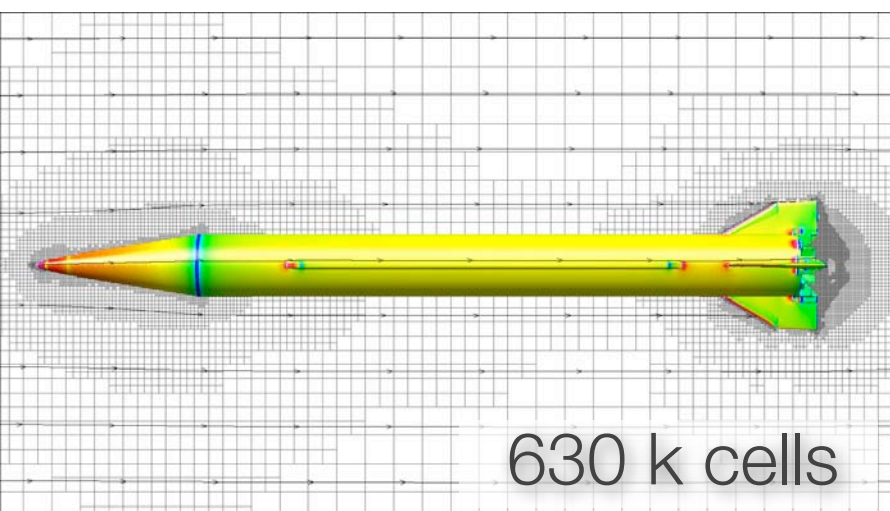




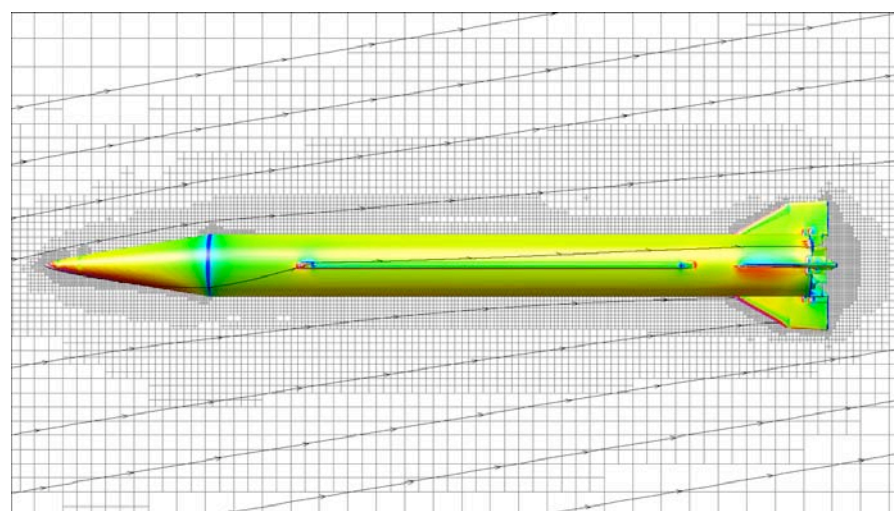
Error Controlled Aero Database

$$M_{\infty} = 0.5$$

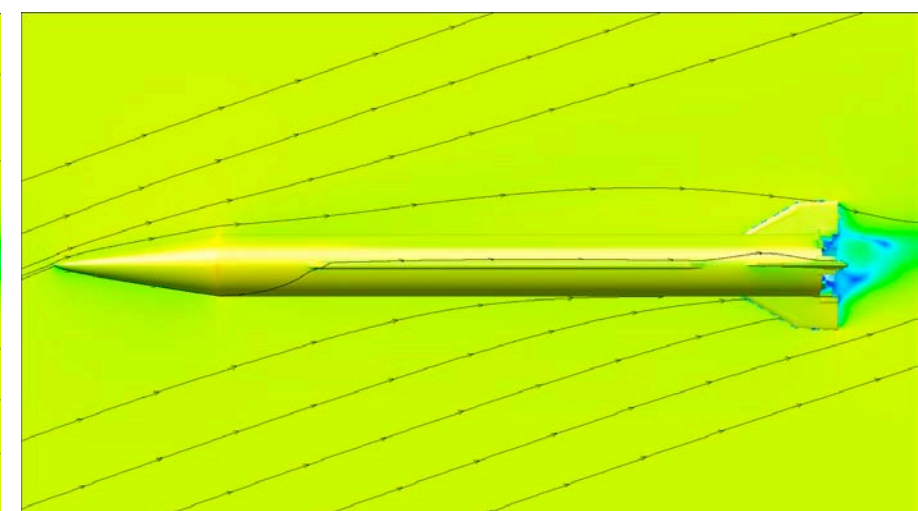
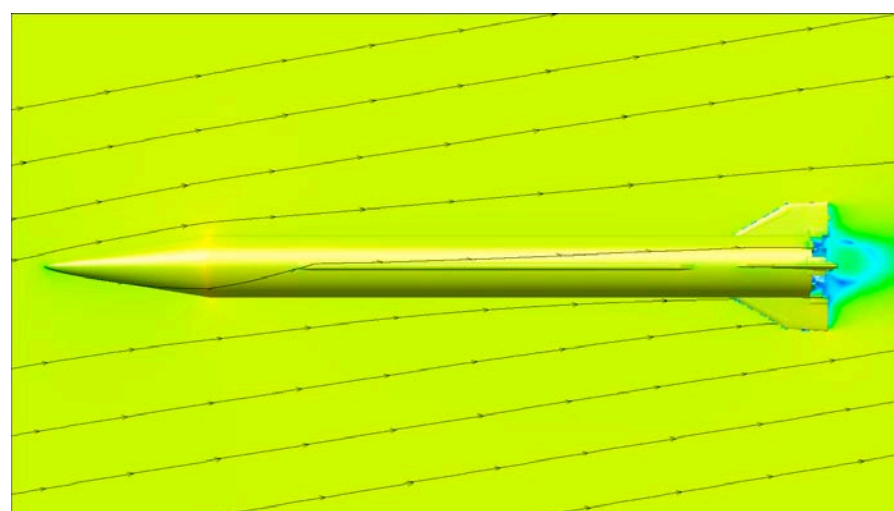
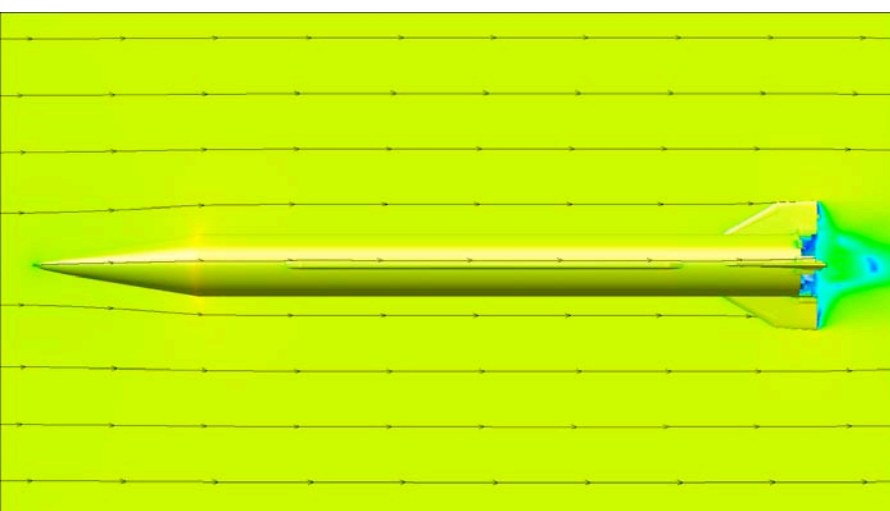
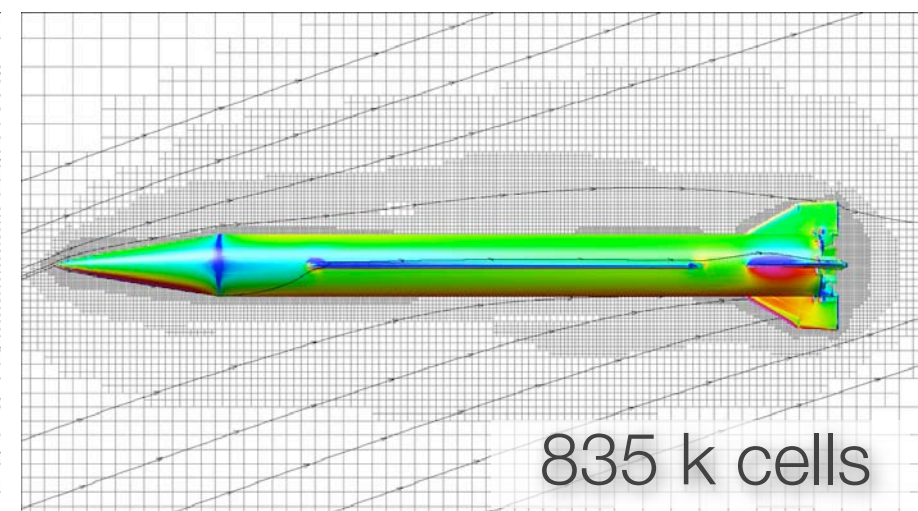
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$



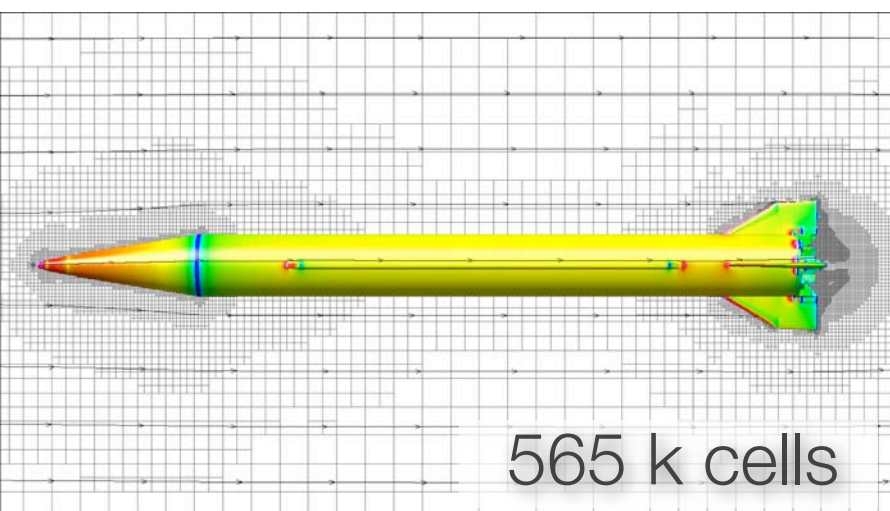
Mach Contours



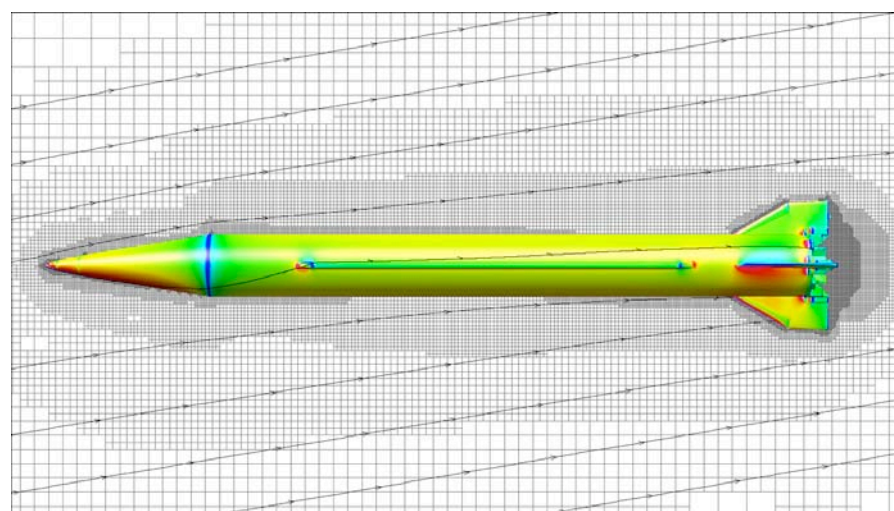
Error Controlled Aero Database

$$M_{\infty} = 0.7$$

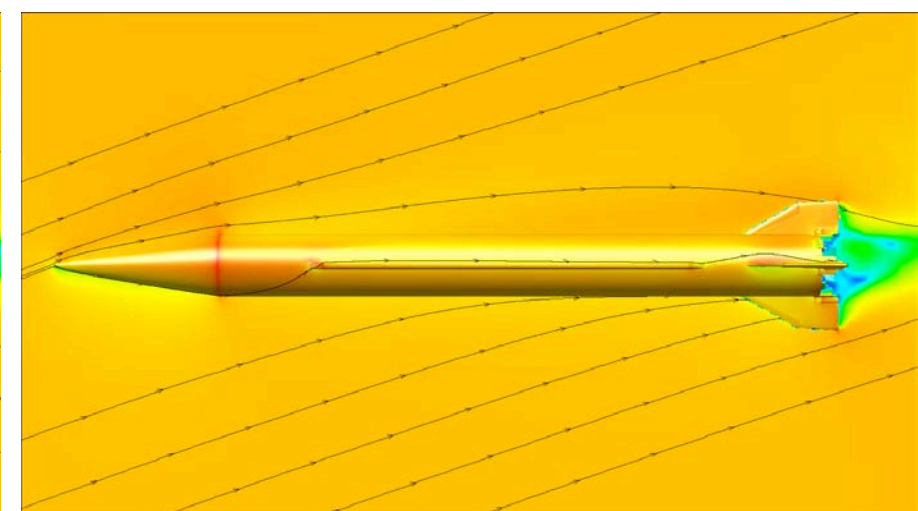
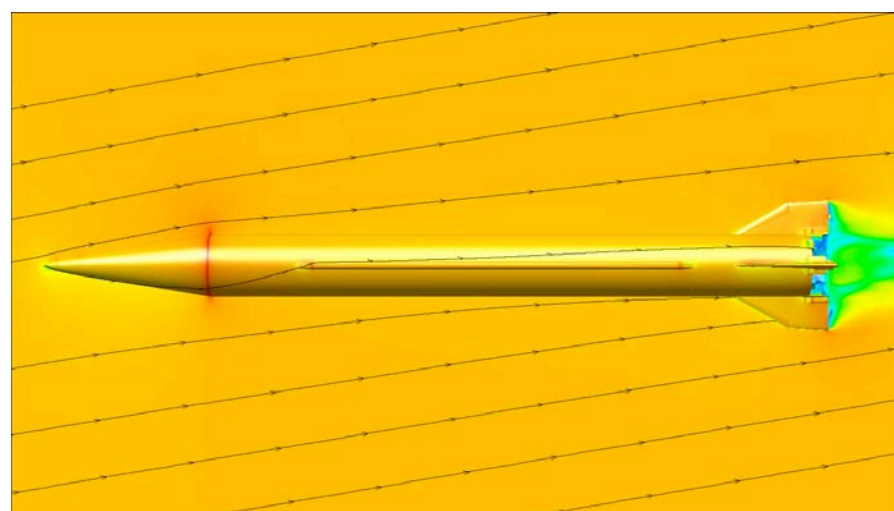
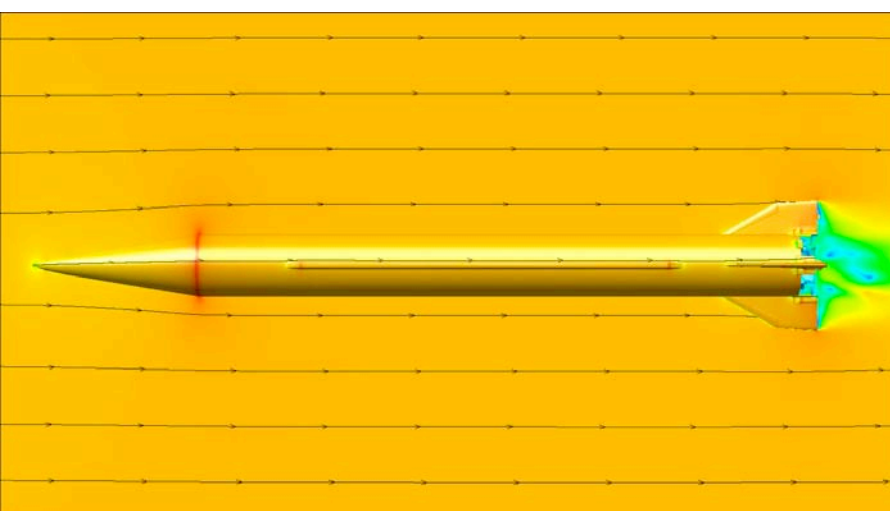
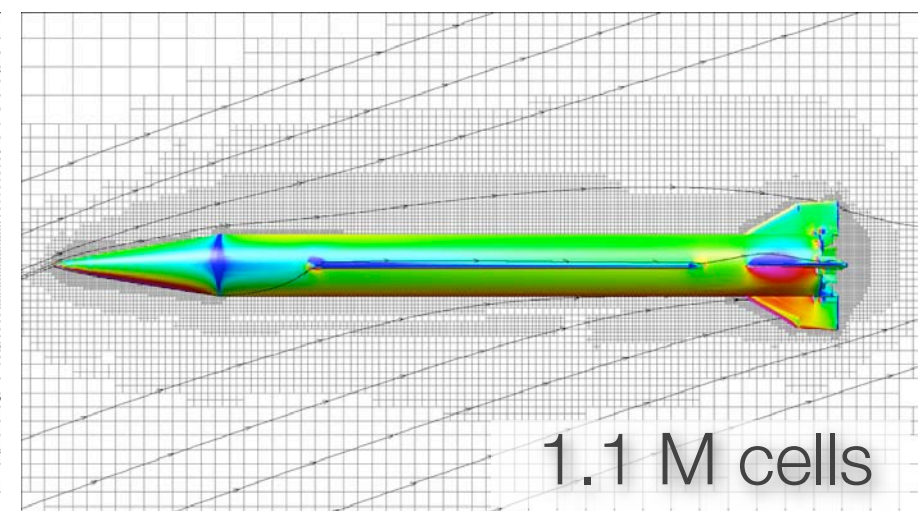
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$



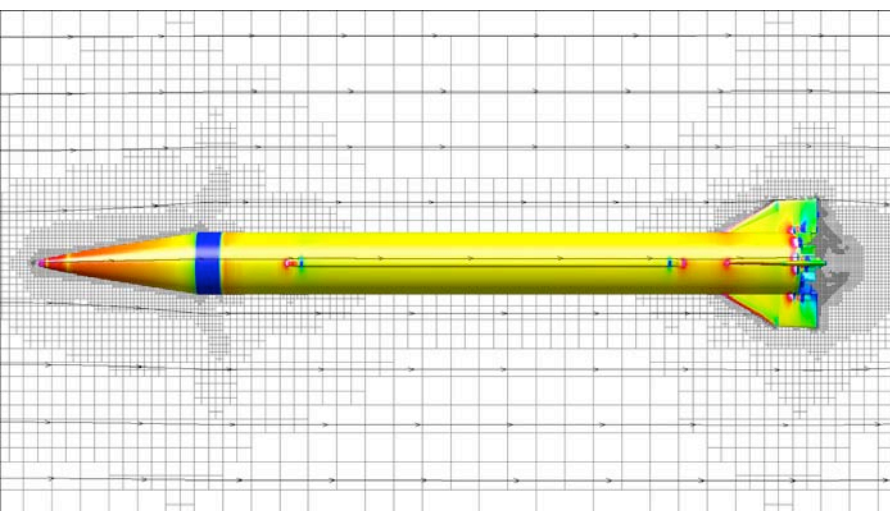
Mach Contours



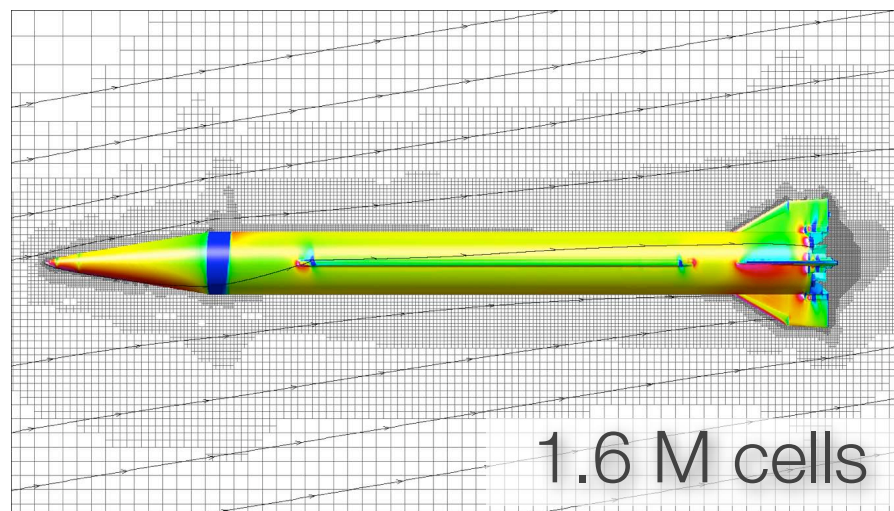
Error Controlled Aero Database

$$M_{\infty} = 0.9$$

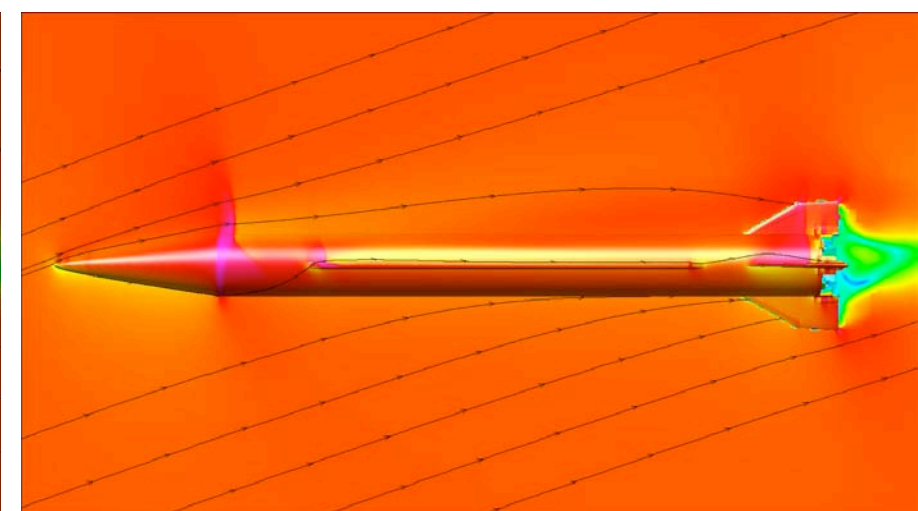
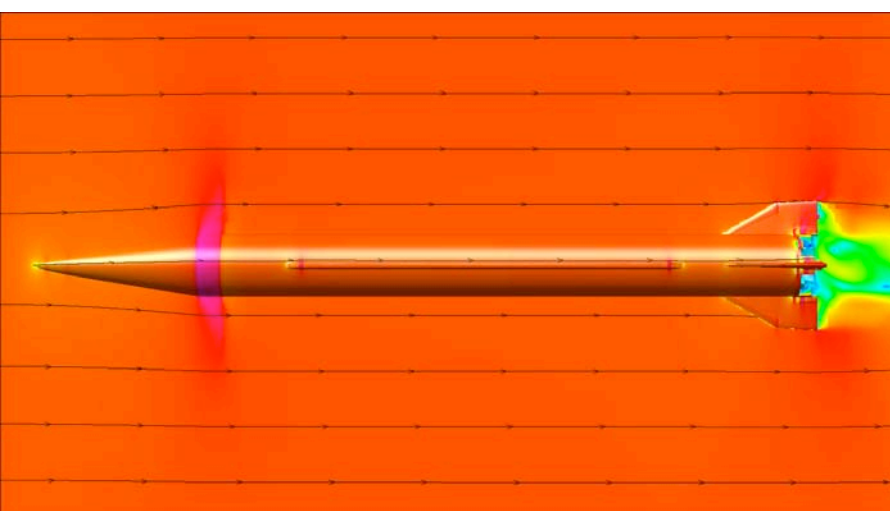
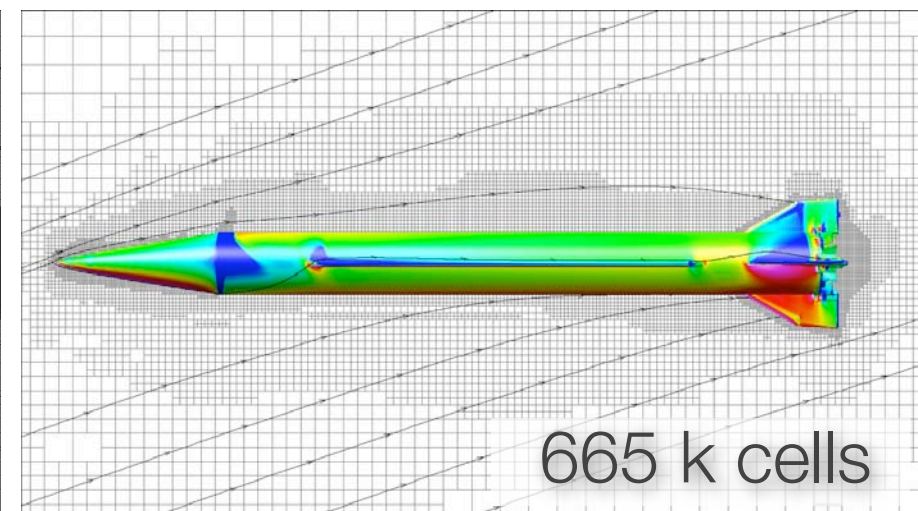
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$



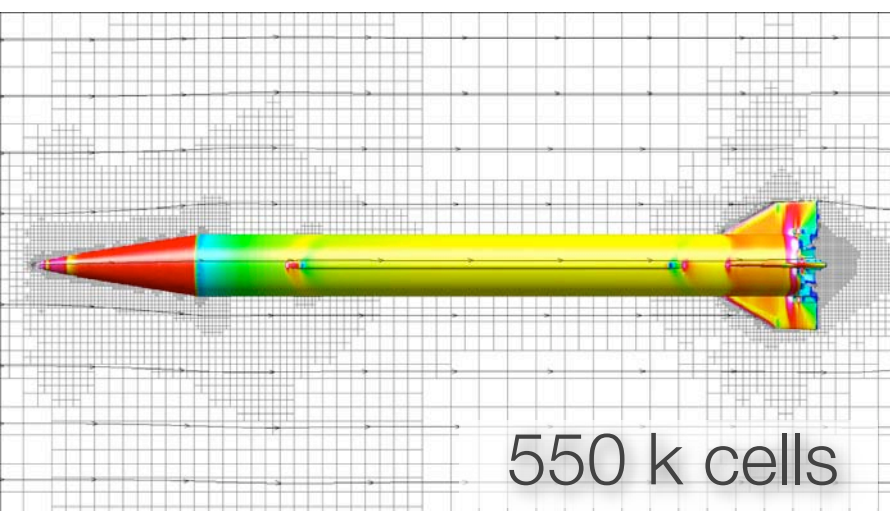
Mach Contours



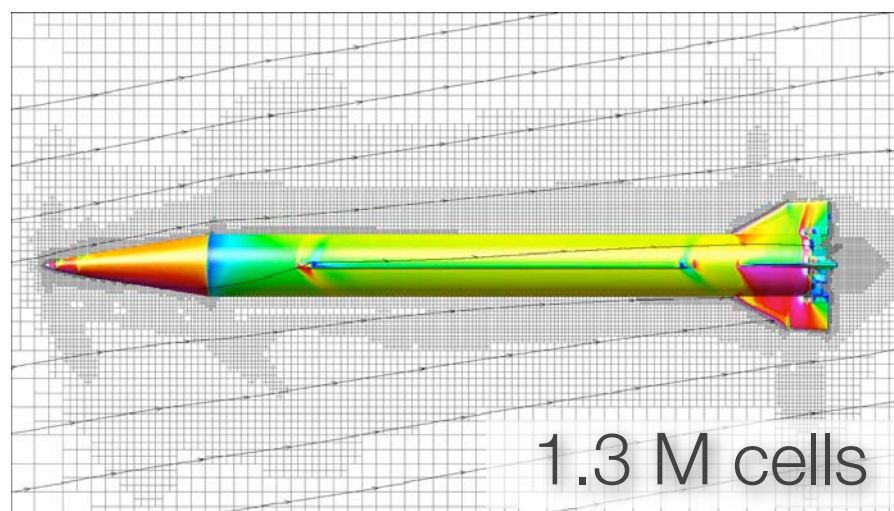
Error Controlled Aero Database

$$M_{\infty} = 1.1$$

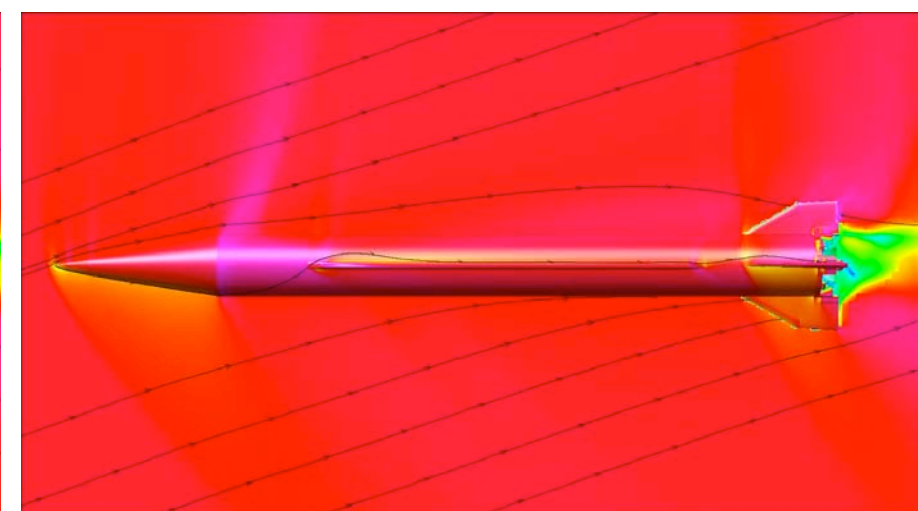
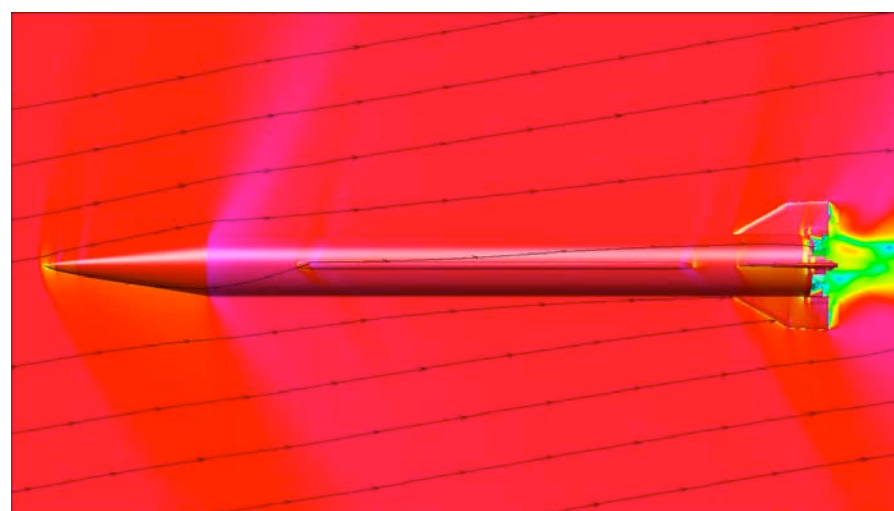
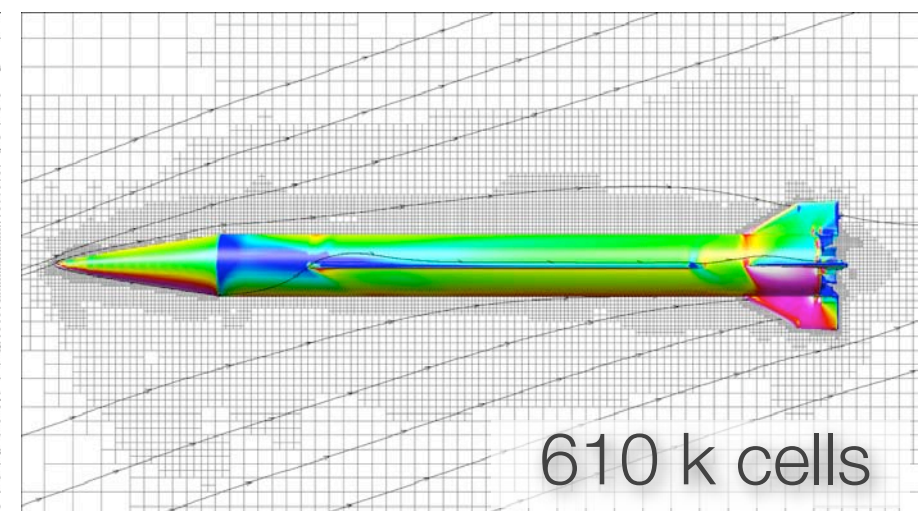
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$

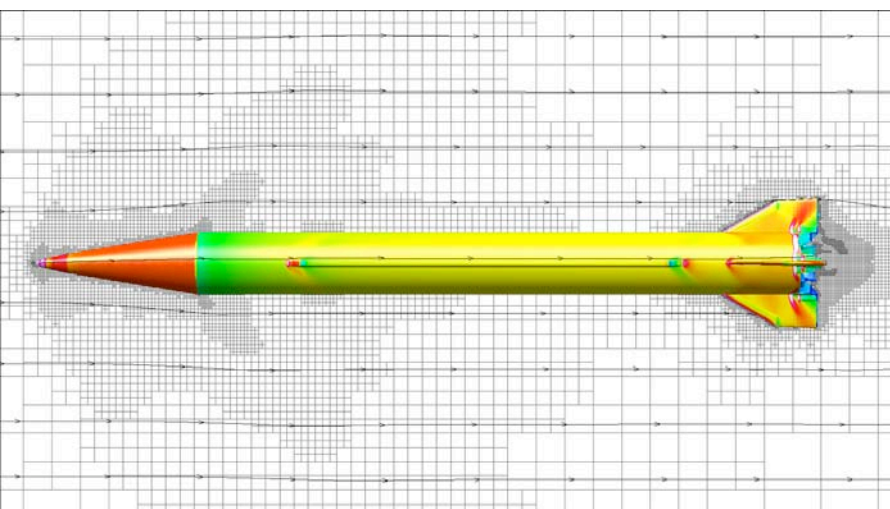




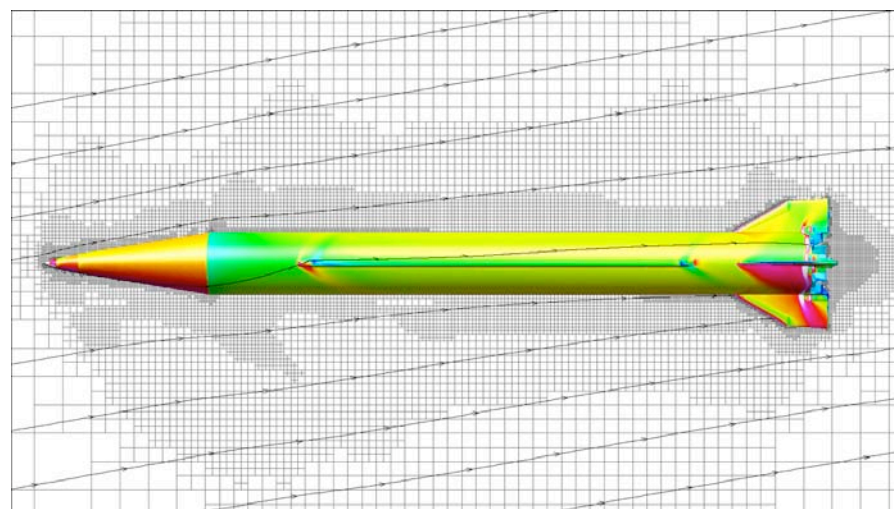
Error Controlled Aero Database

$$M_{\infty} = 1.3$$

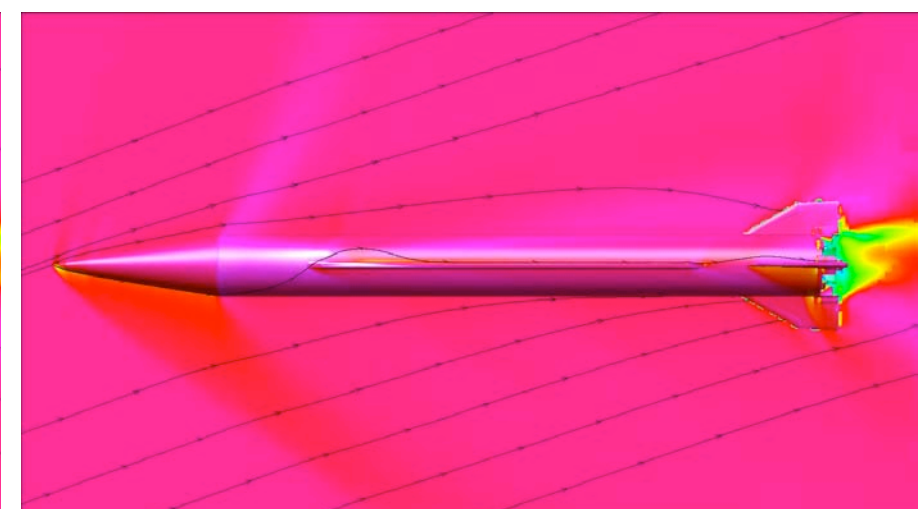
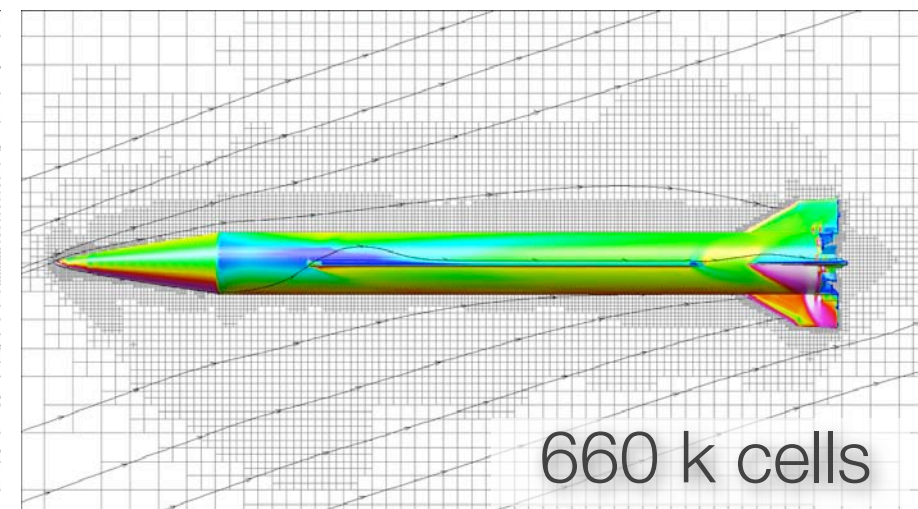
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$



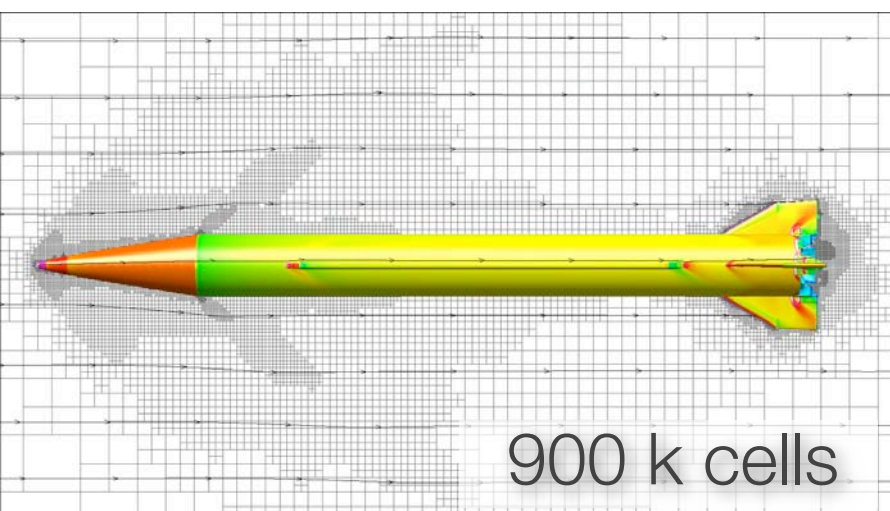
Mach Contours



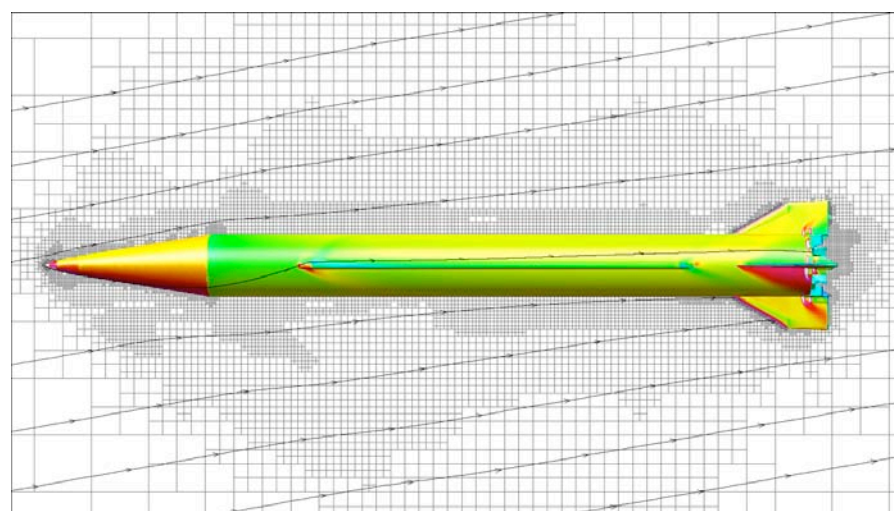
Error Controlled Aero Database

$$M_{\infty} = 1.6$$

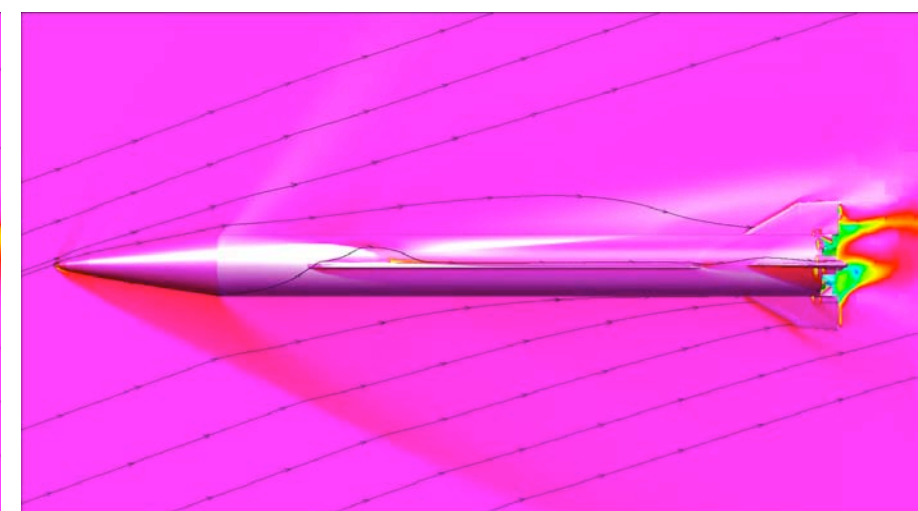
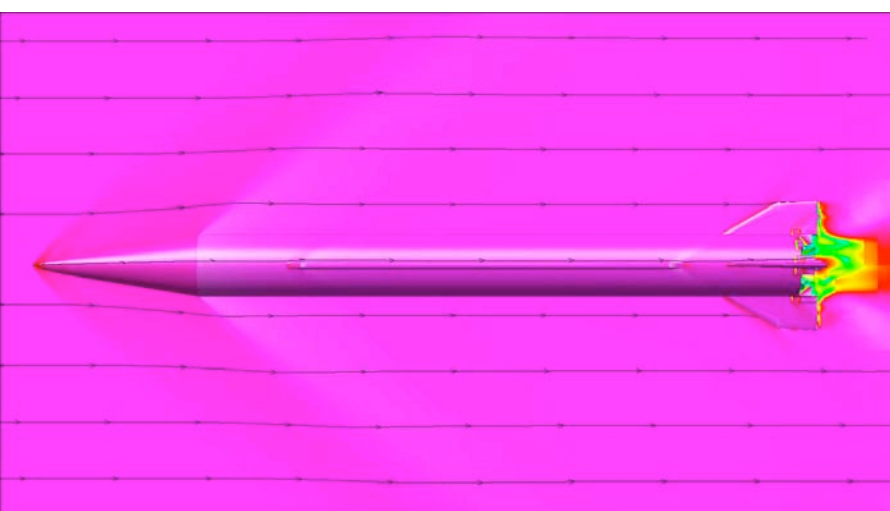
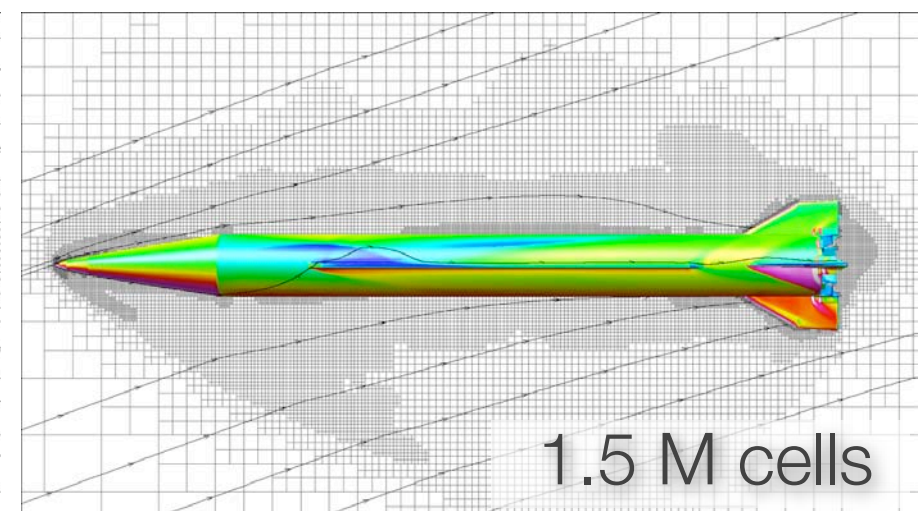
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$



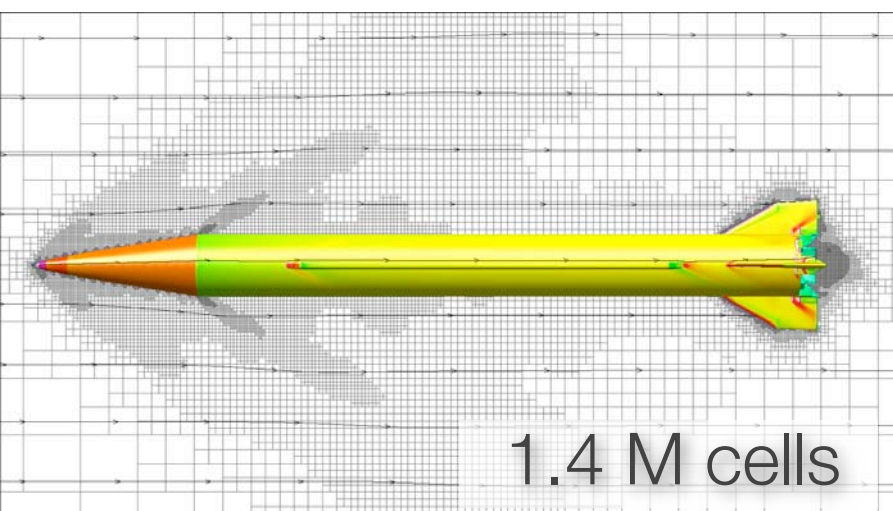
Mach Contours



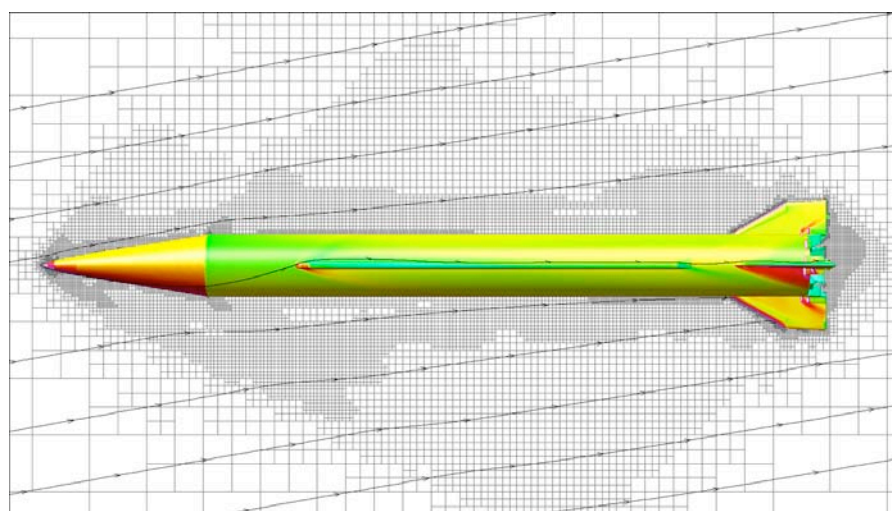
Error Controlled Aero Database

$$M_{\infty} = 2.0$$

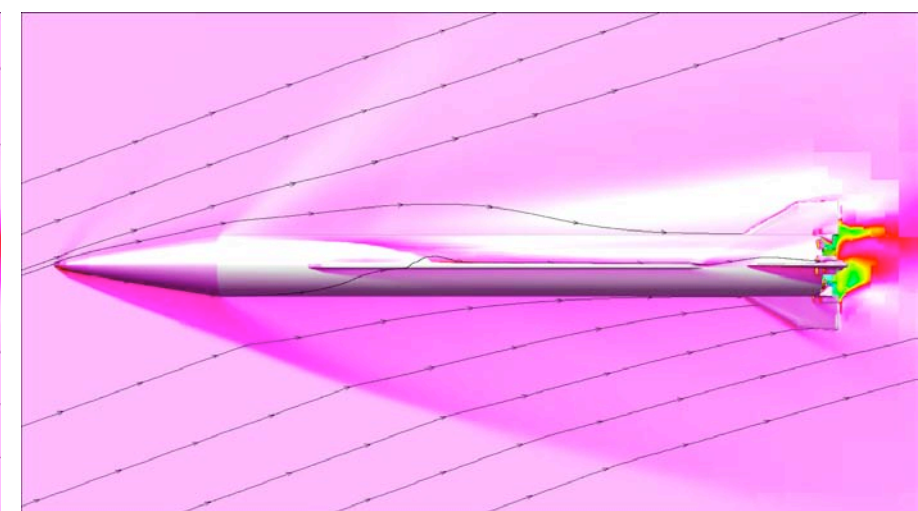
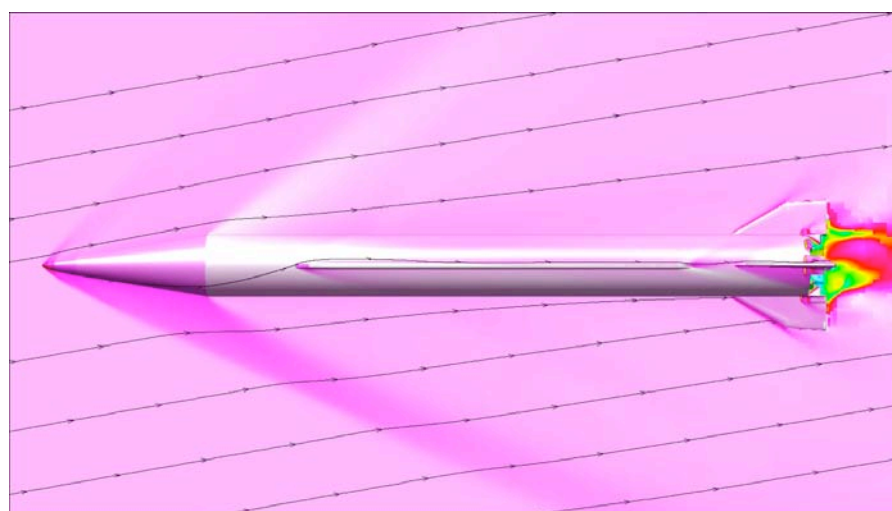
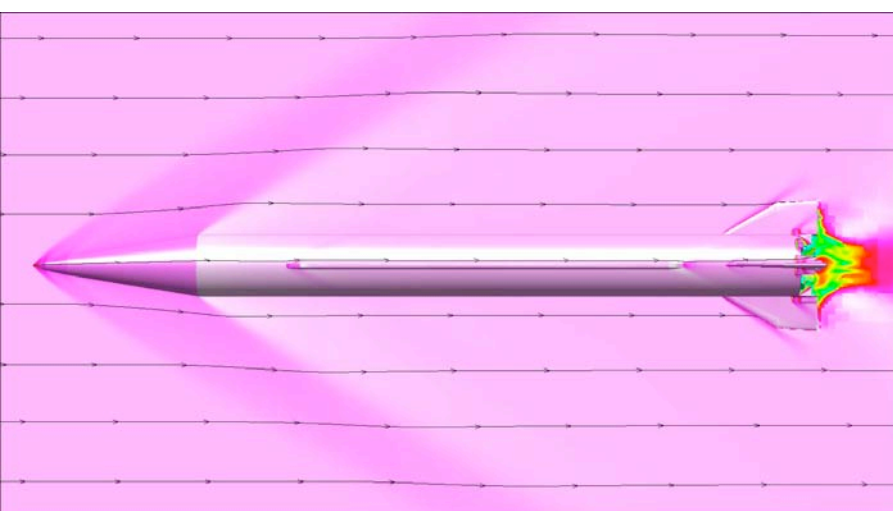
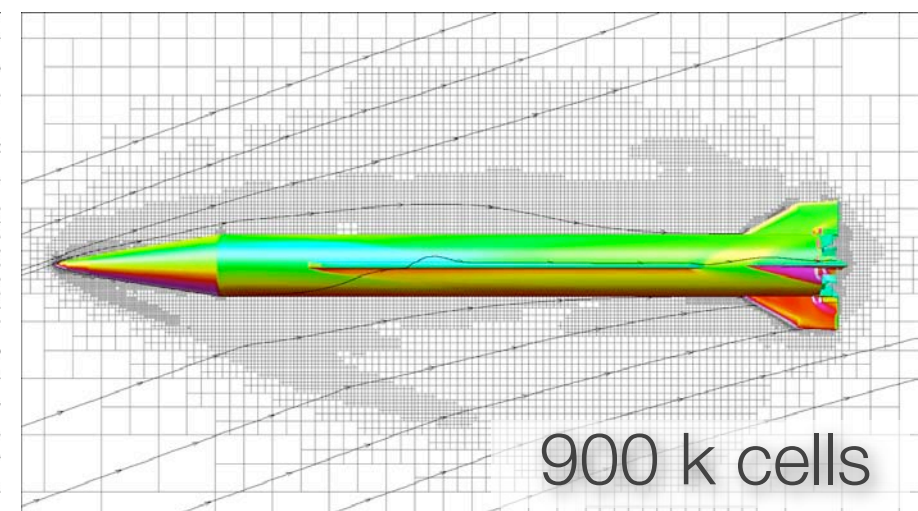
$$\alpha = 0^{\circ}$$



$$\alpha = 10^{\circ}$$



$$\alpha = 20^{\circ}$$

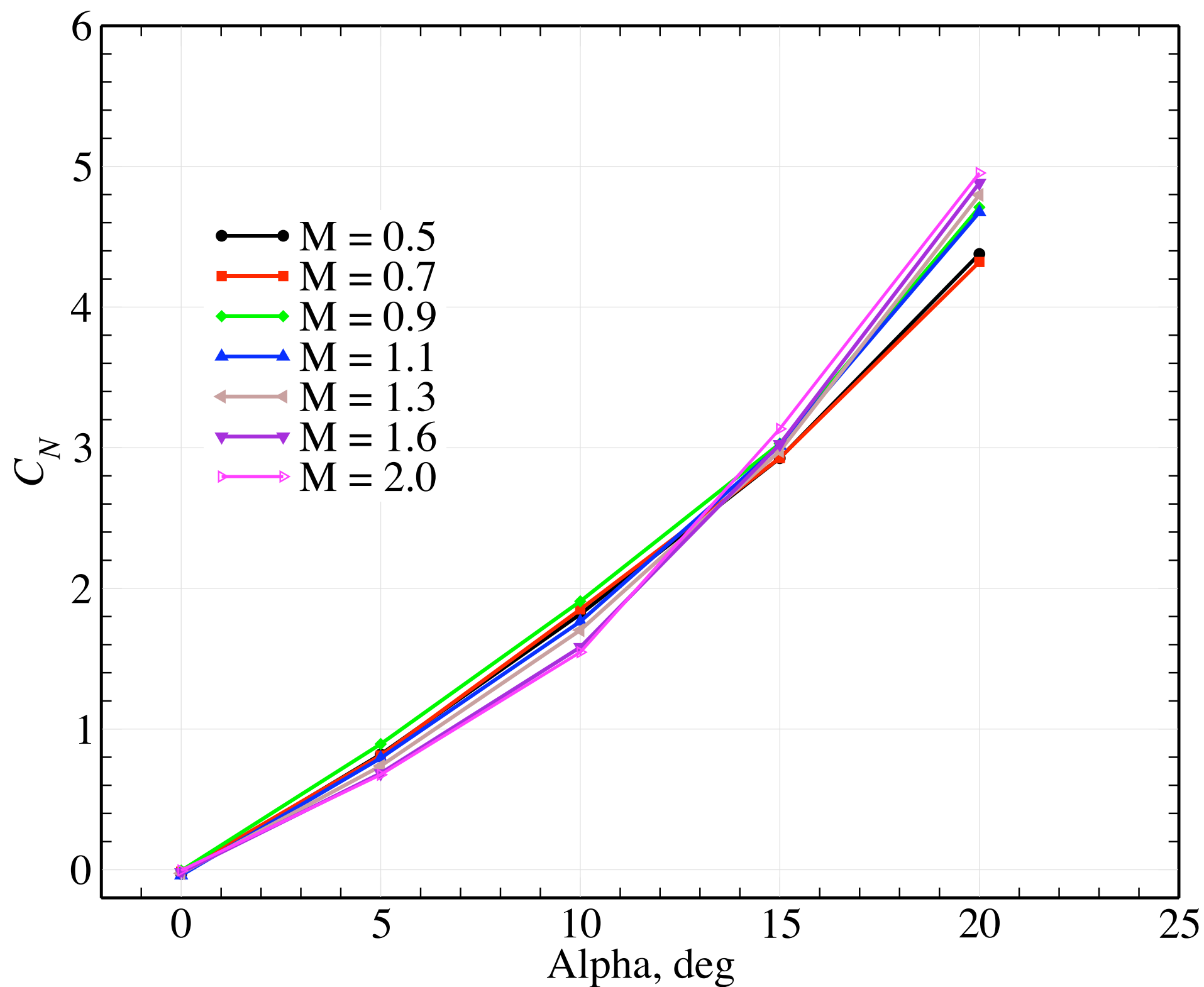


Mach Contours



Error Controlled Aero Database

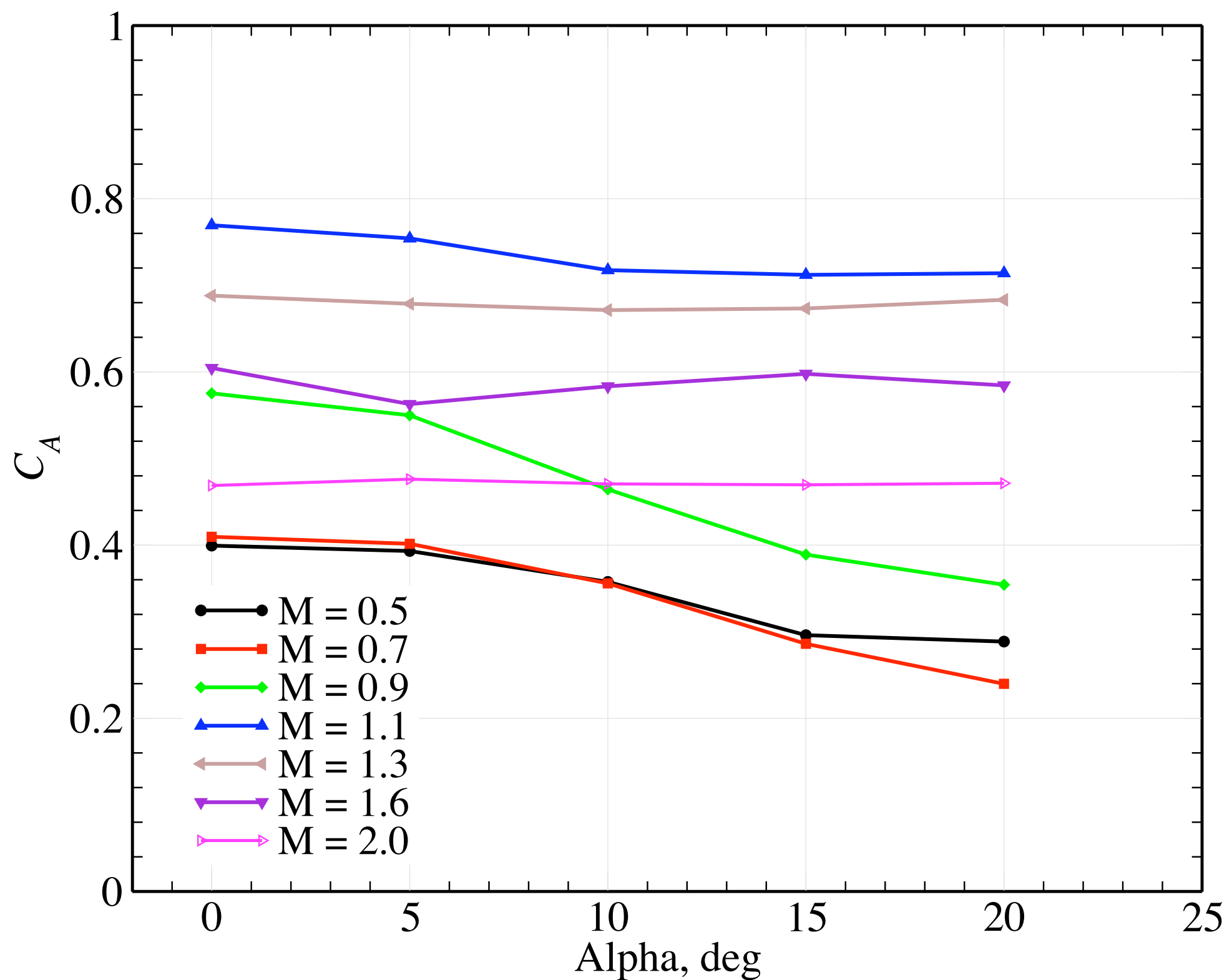
Normal Force
Coefficient





Error Controlled Aero Database

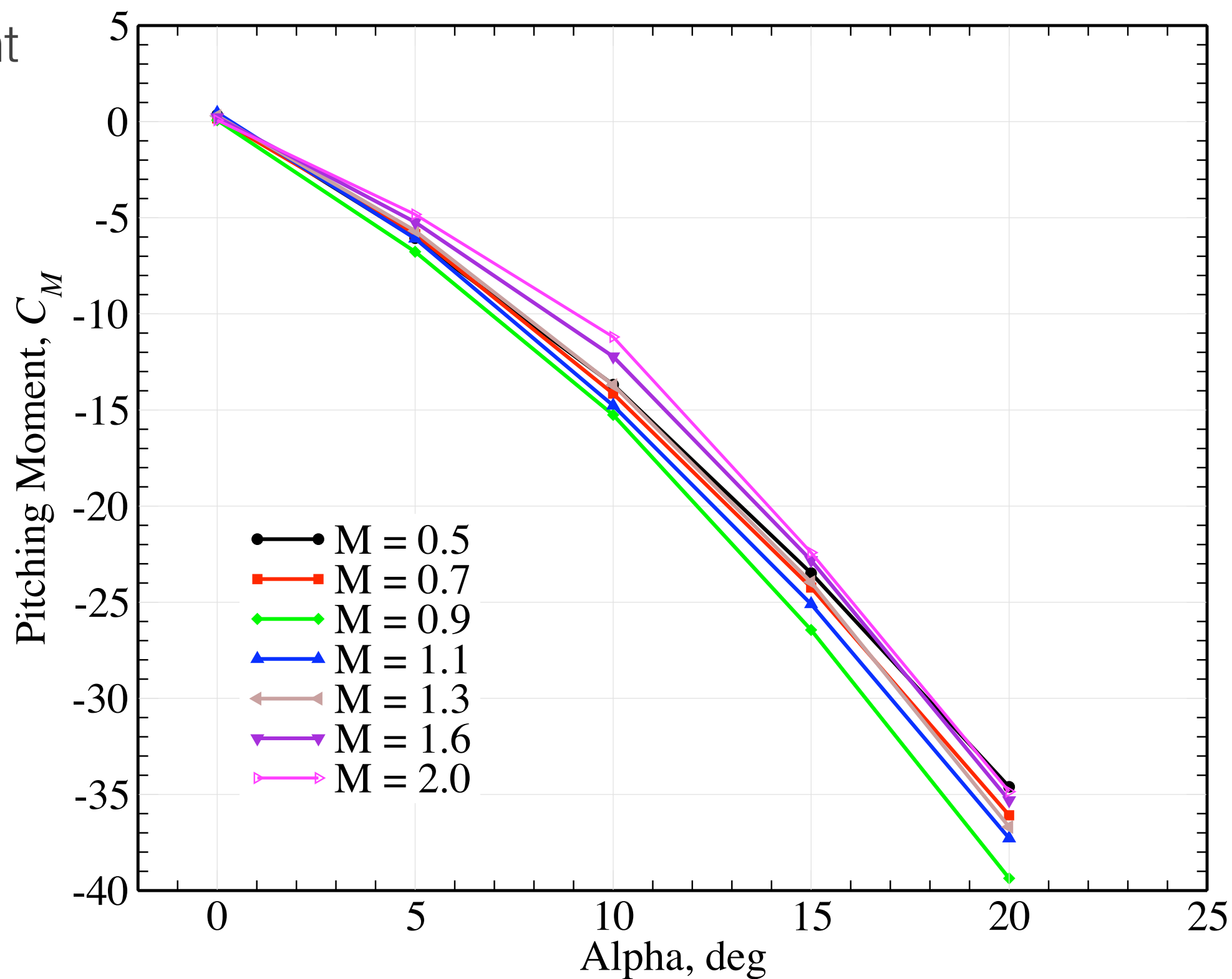
Axial Force
Coefficient





Error Controlled Aero Database

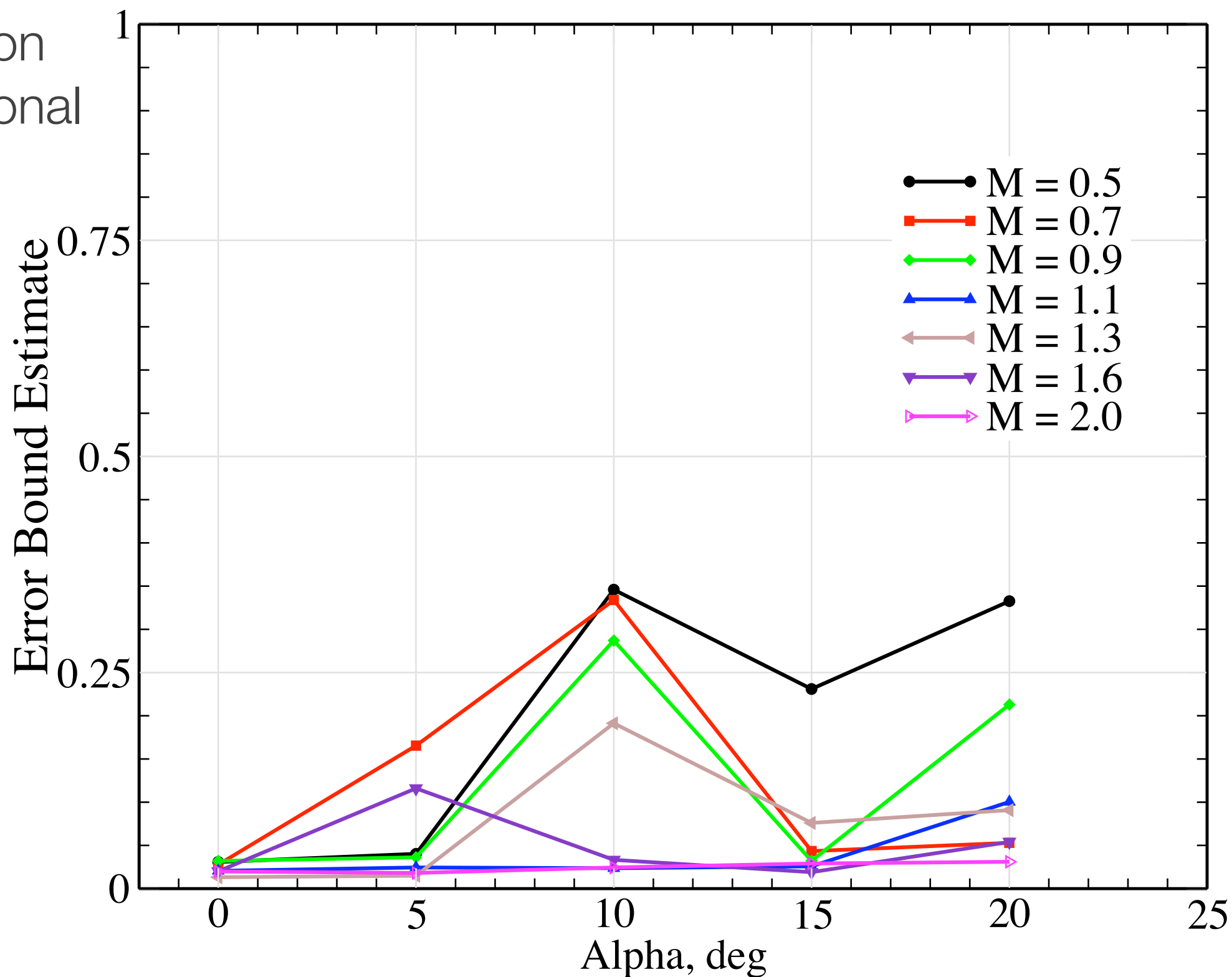
Pitch moment
about nose





Error Controlled Aero Database

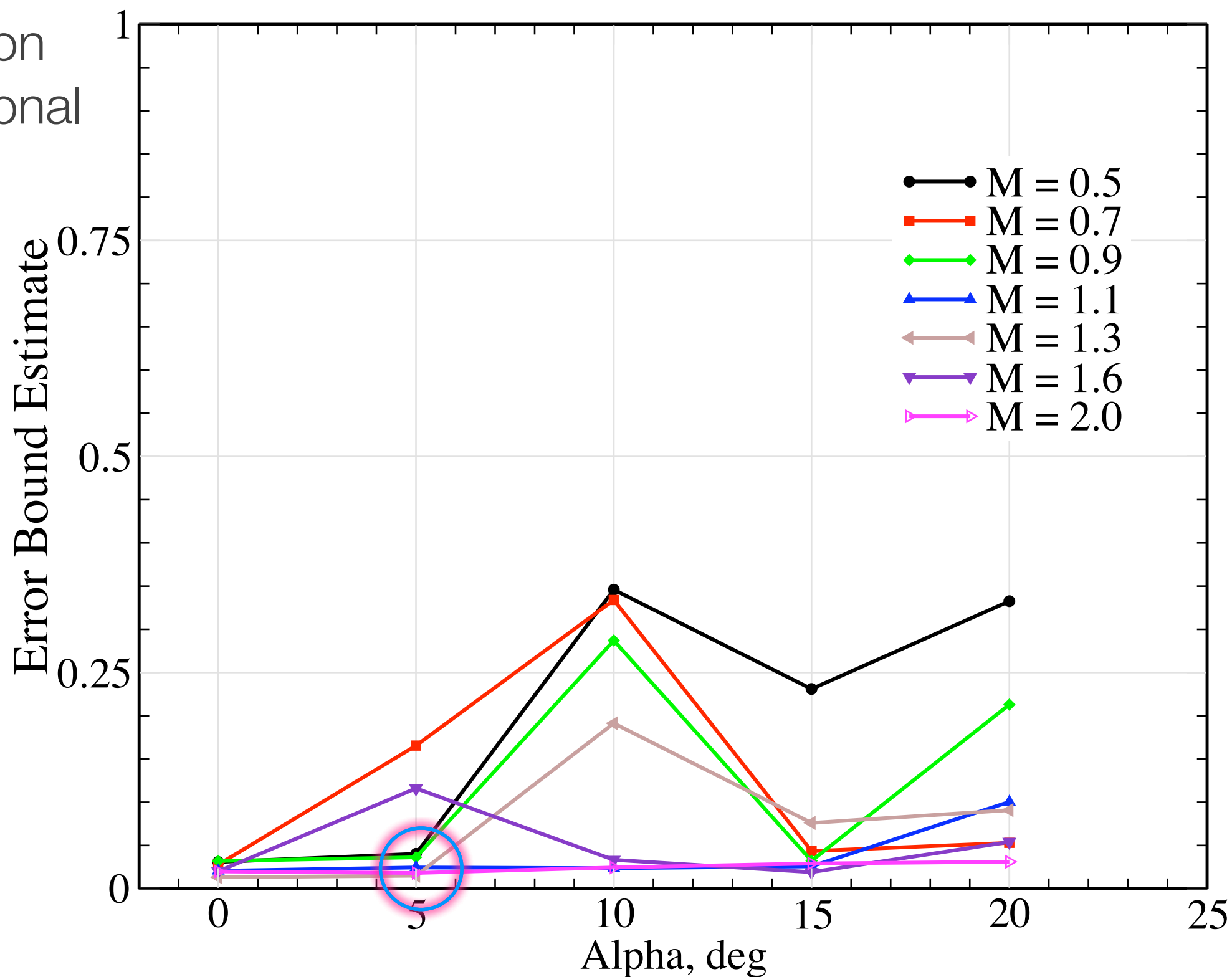
Error bound on
output functional

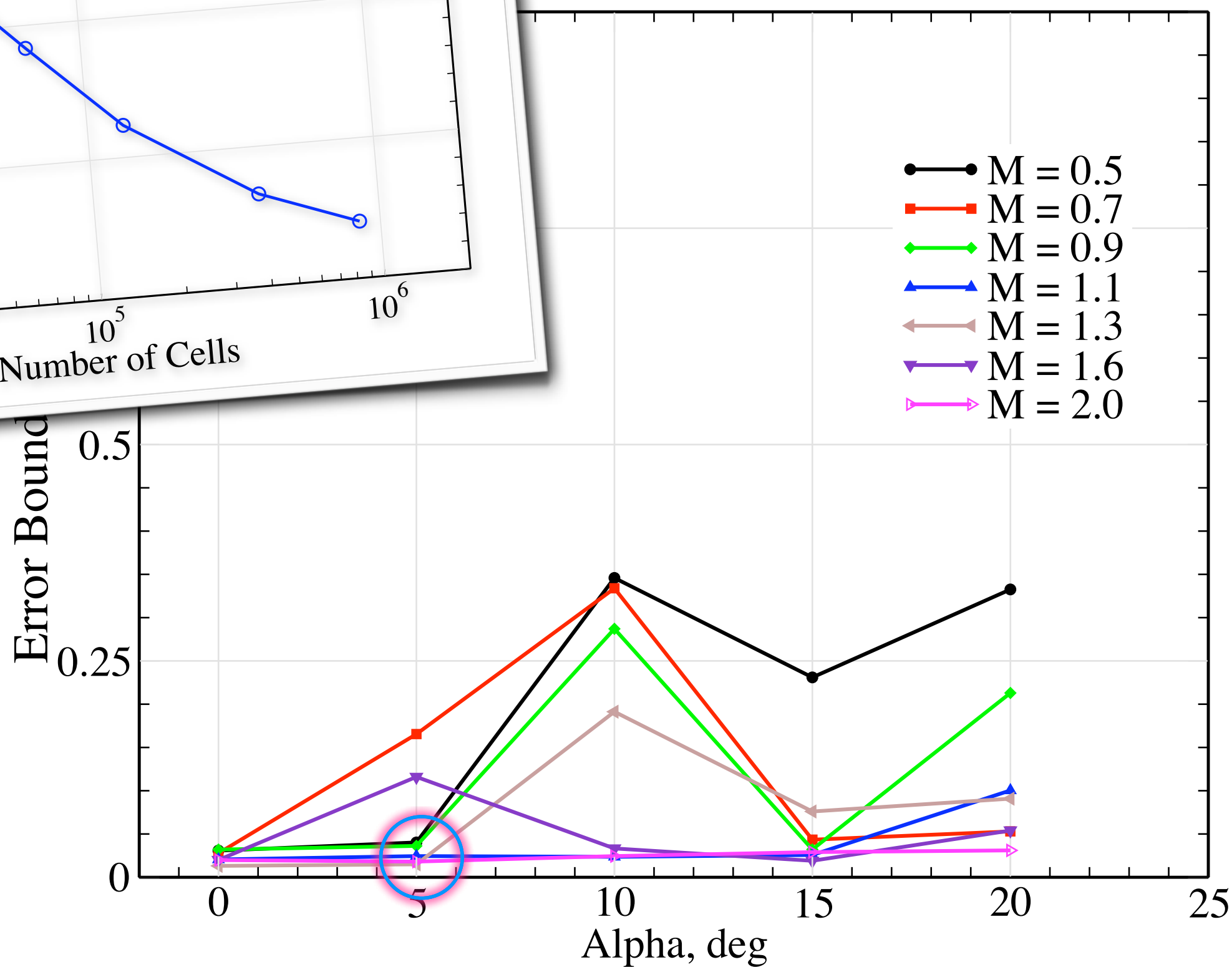
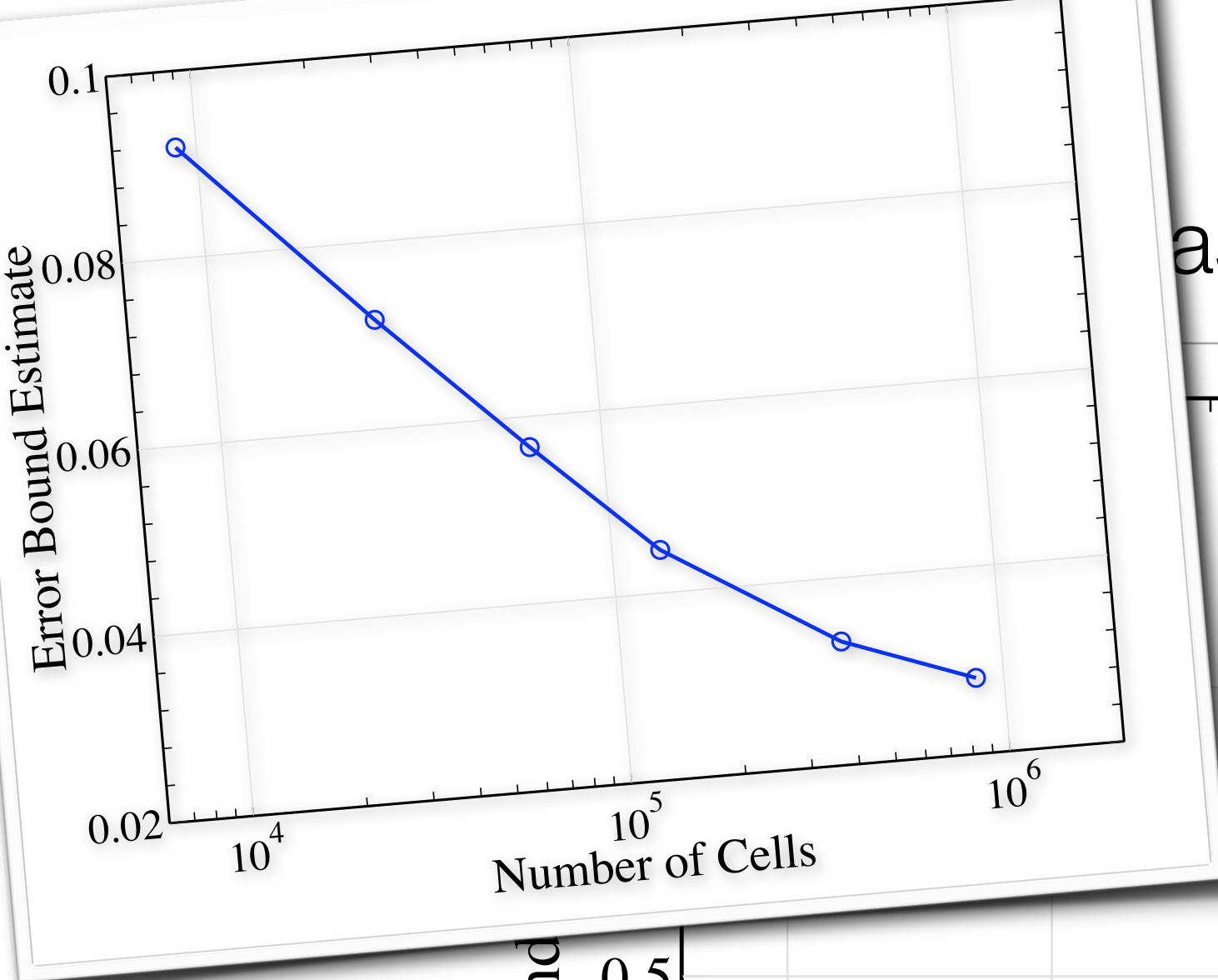


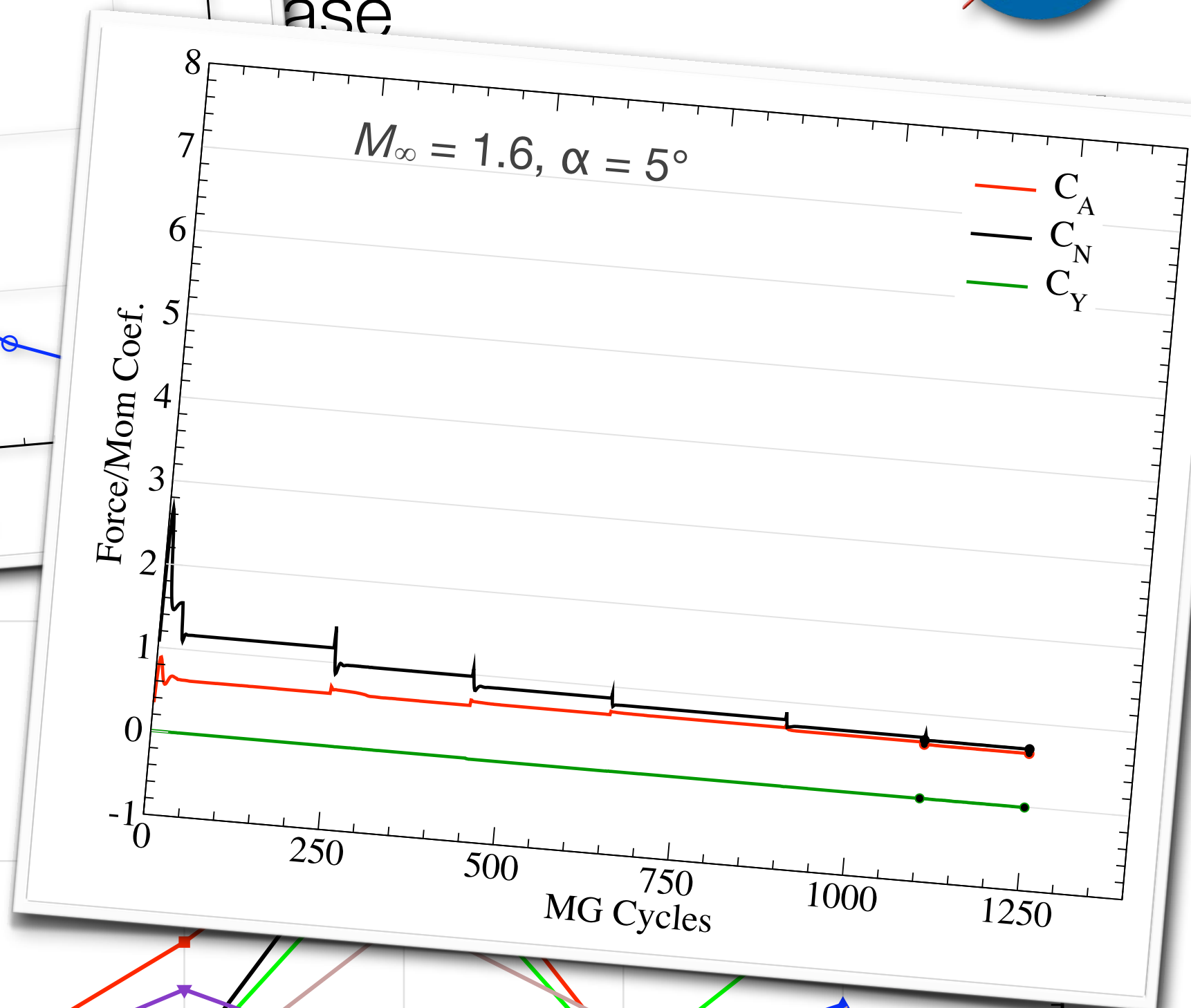
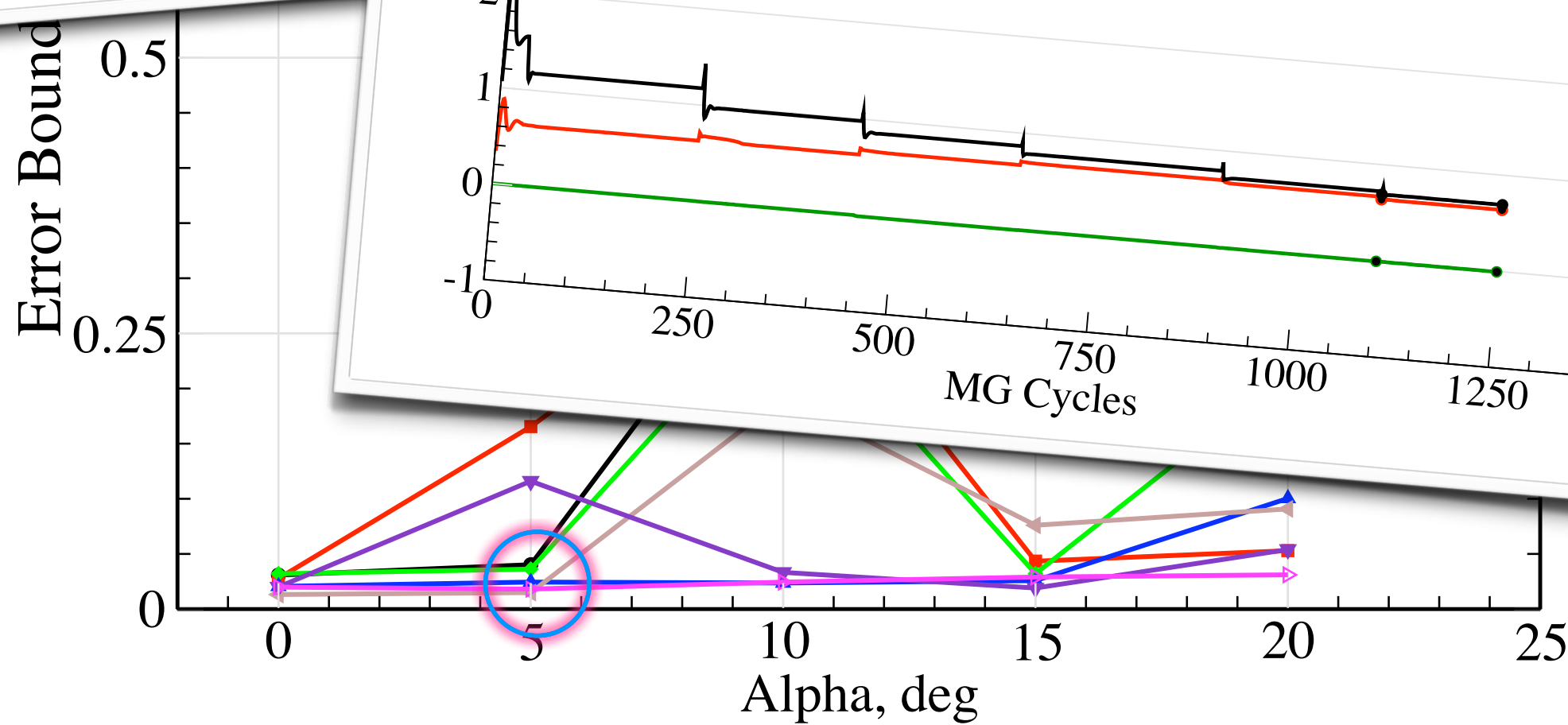
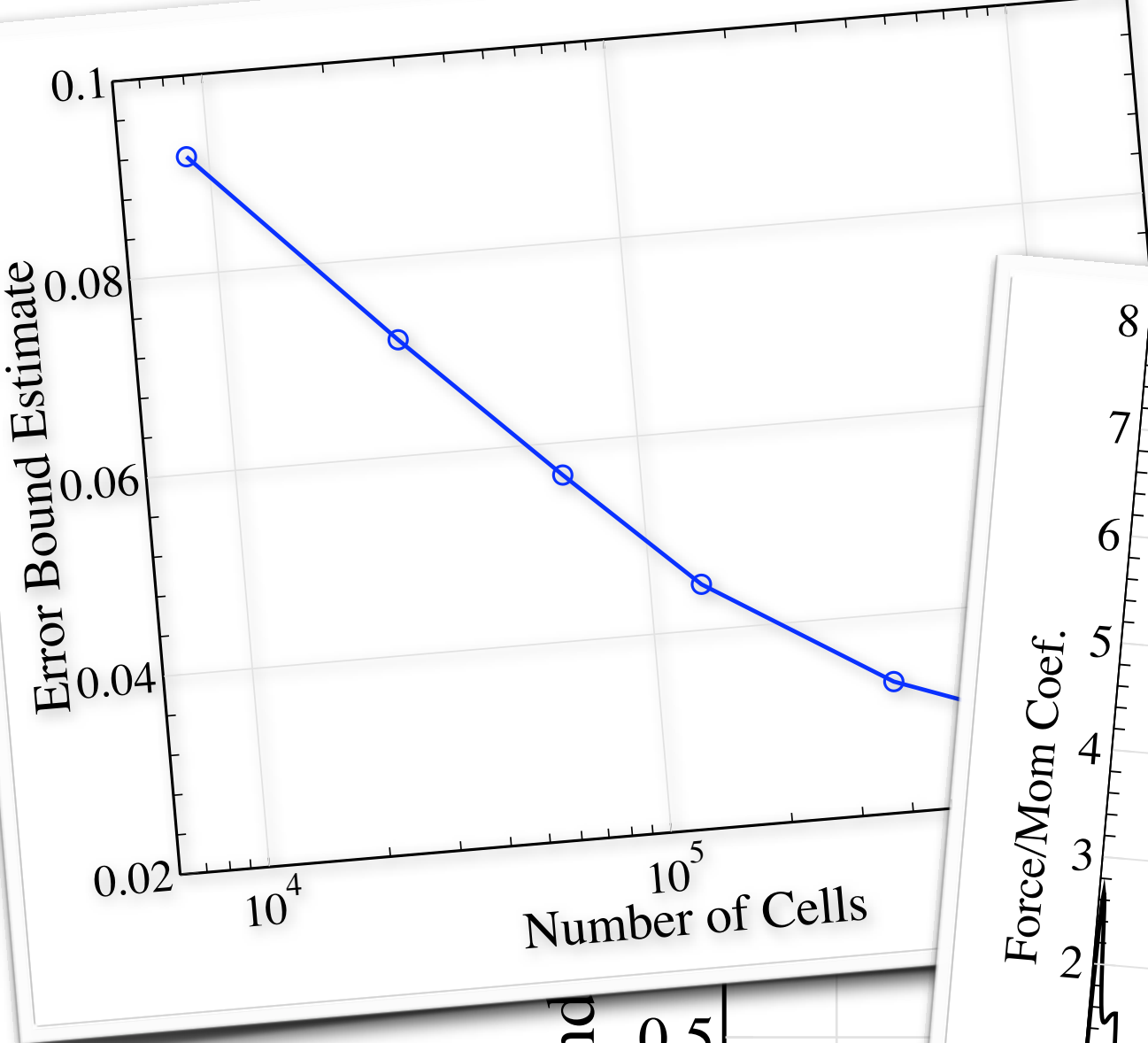


Error Controlled Aero Database

Error bound on
output functional



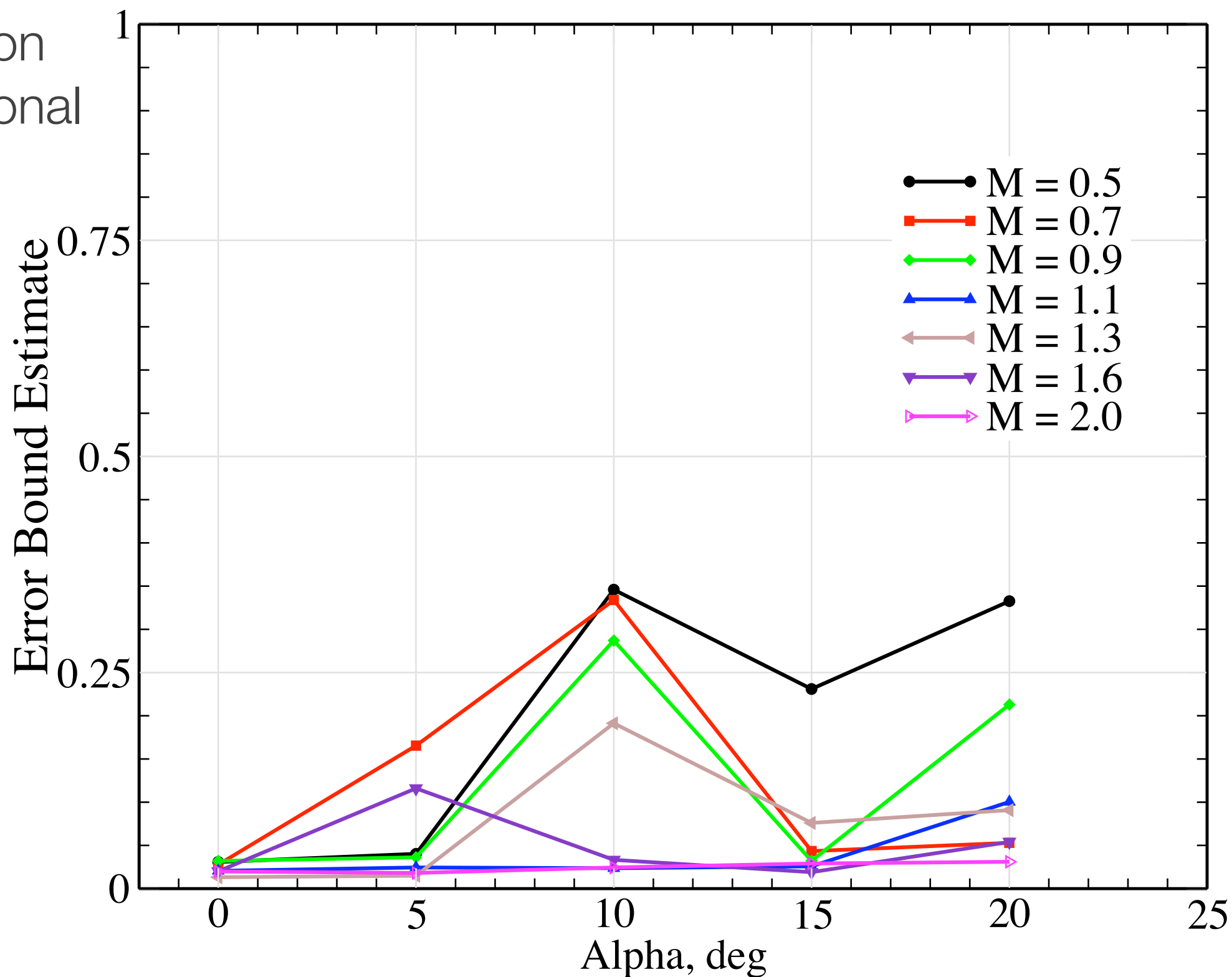






Error Controlled Aero Database

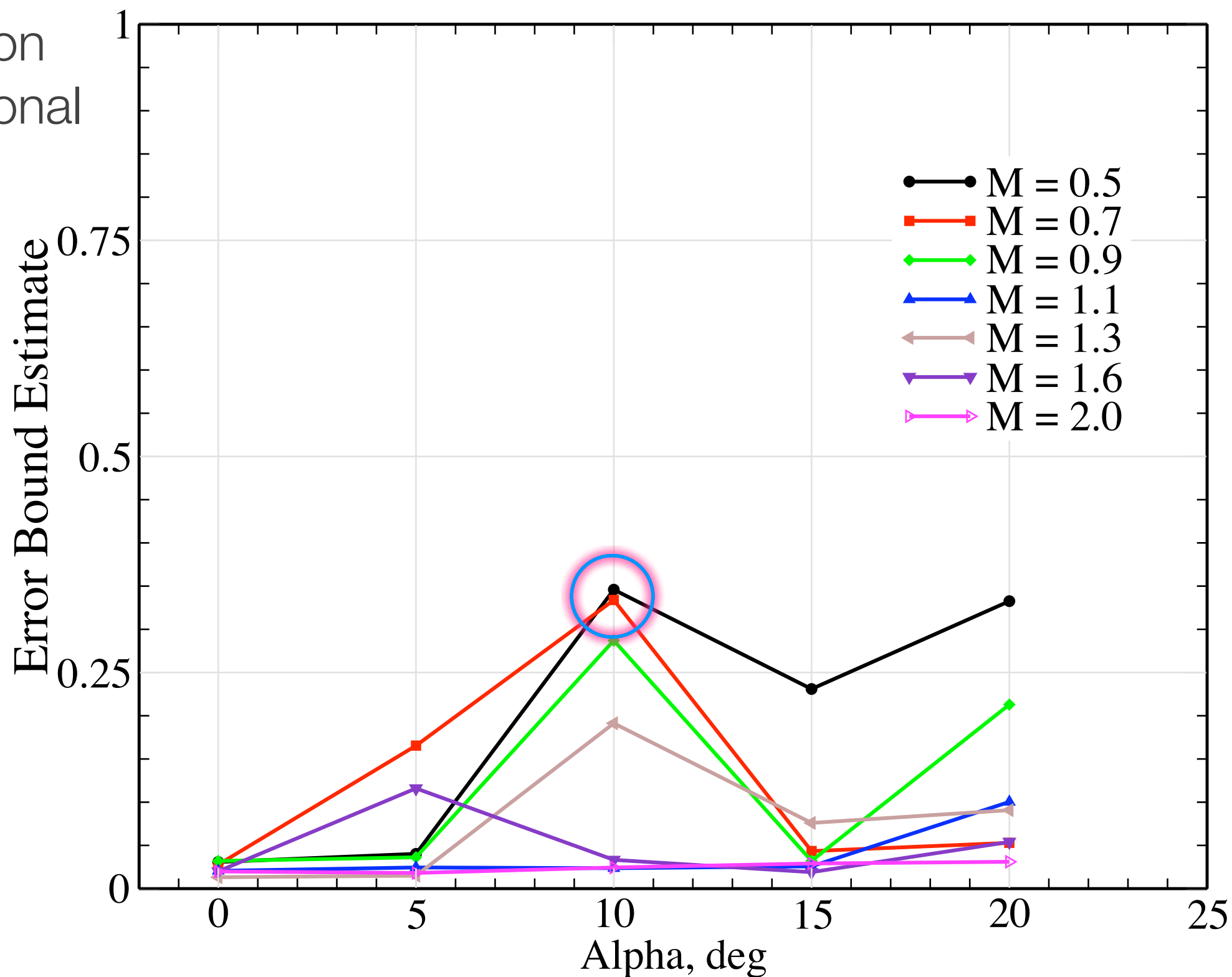
Error bound on
output functional





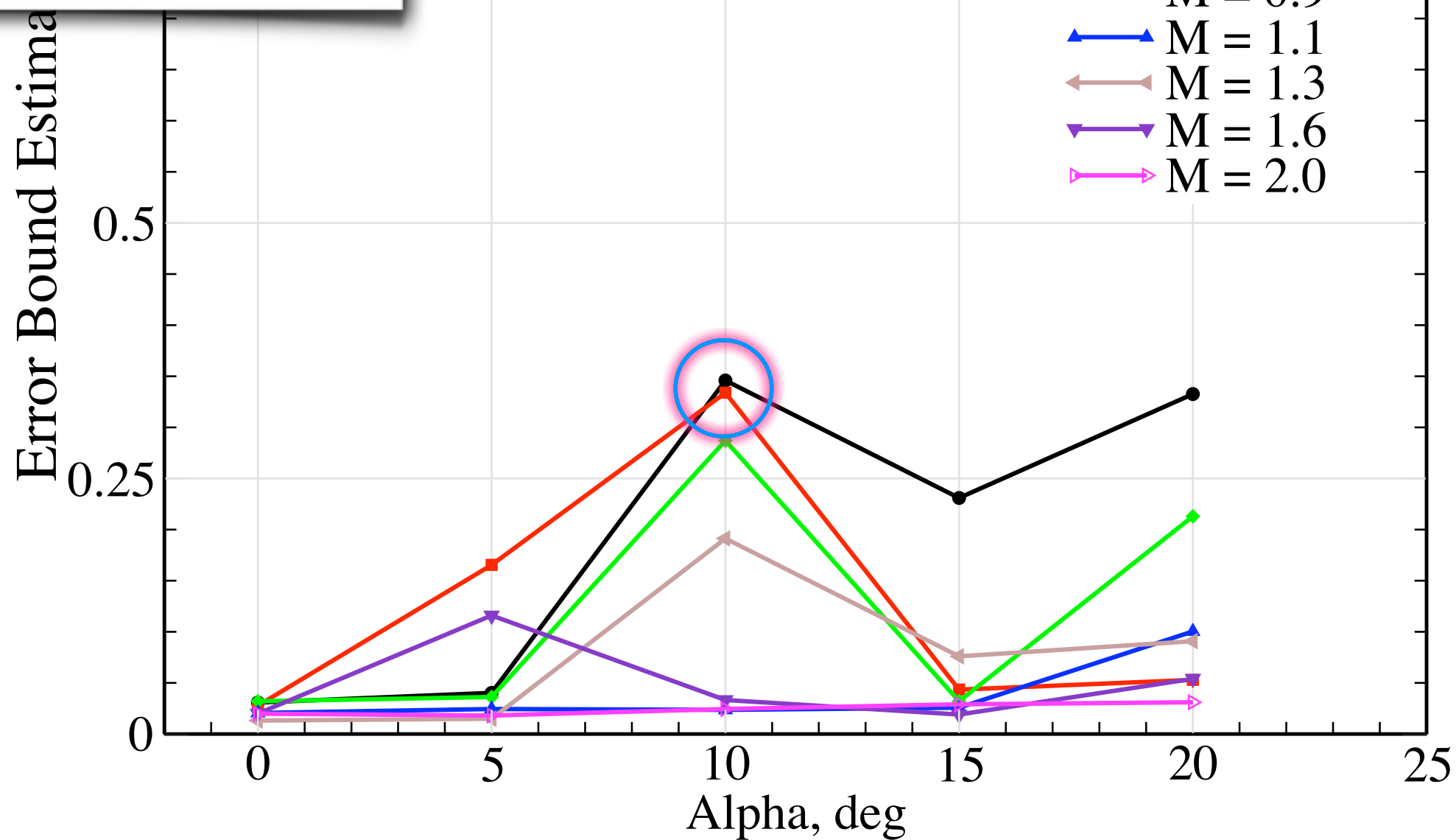
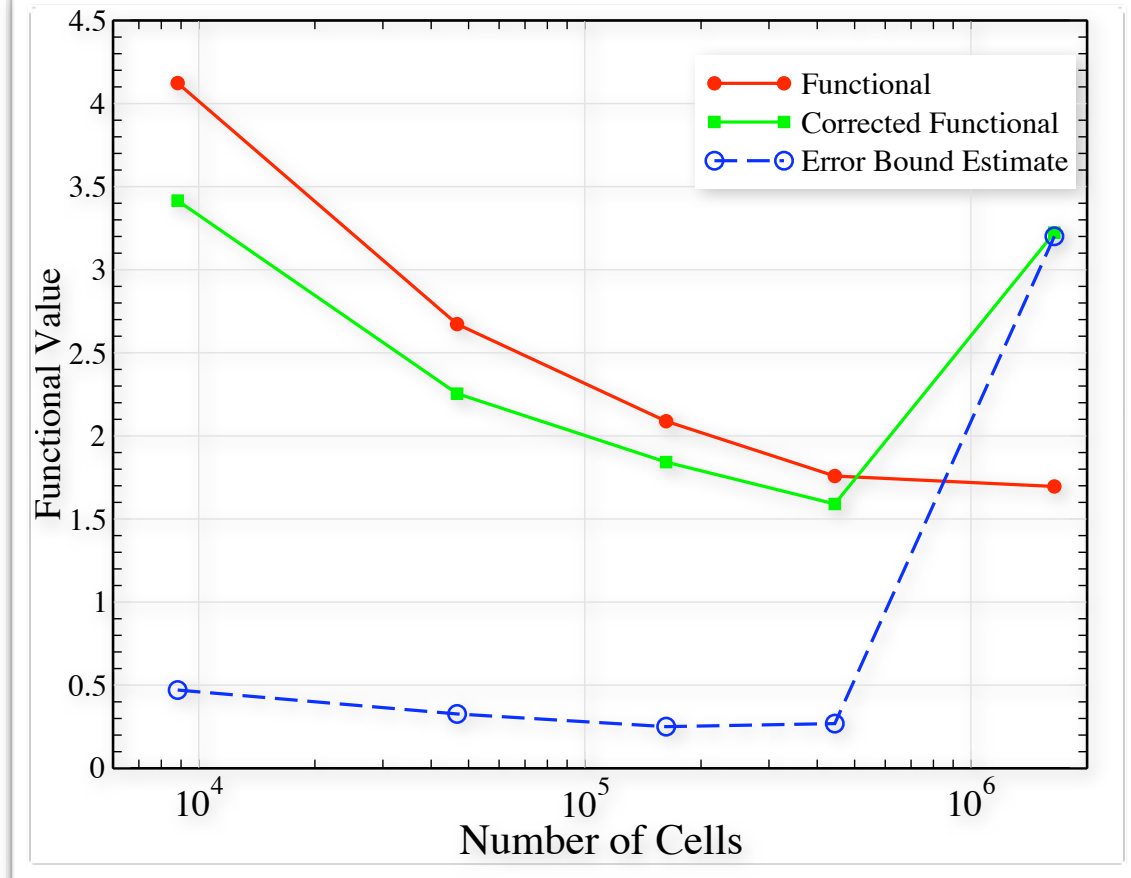
Error Controlled Aero Database

Error bound on
output functional



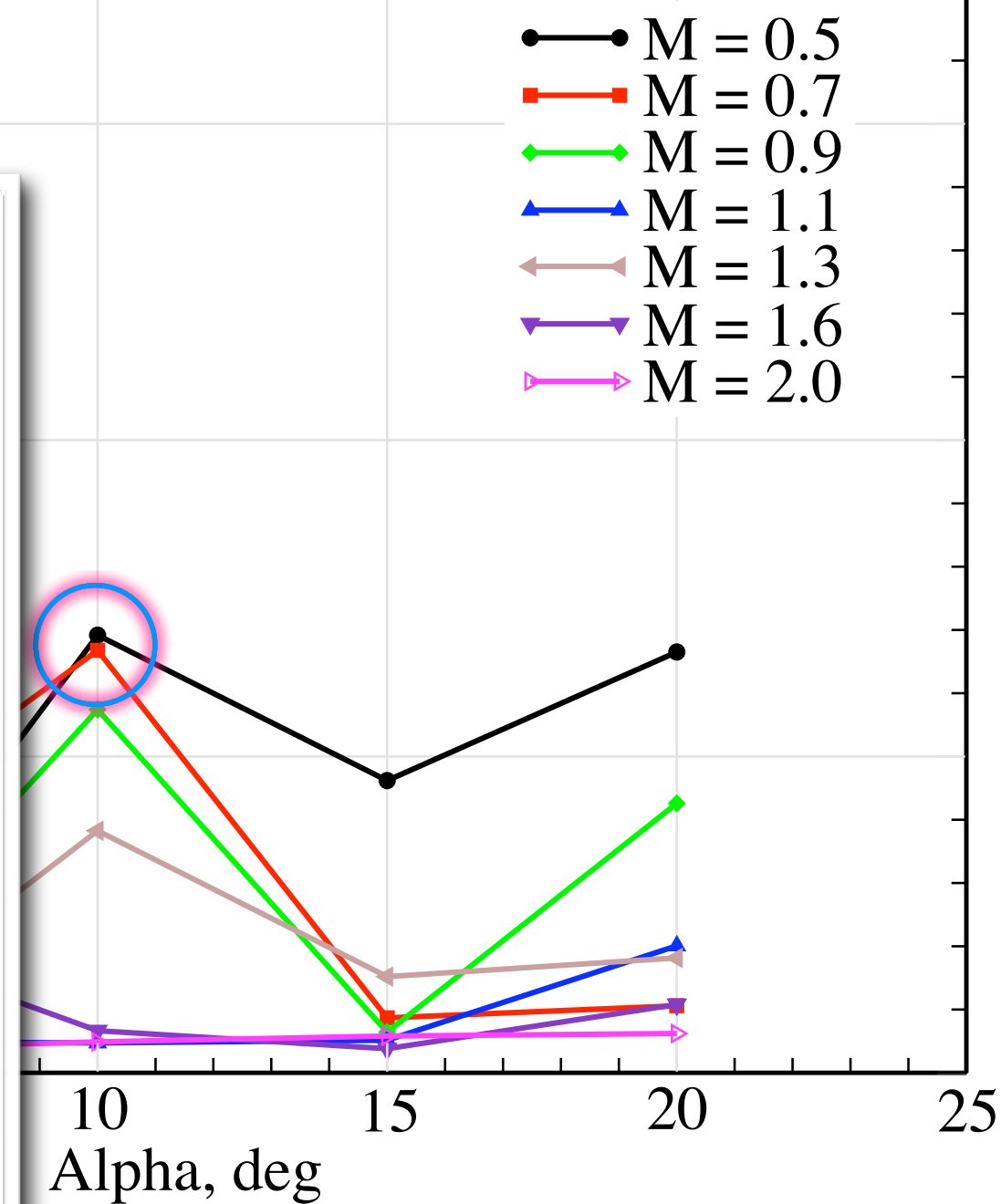
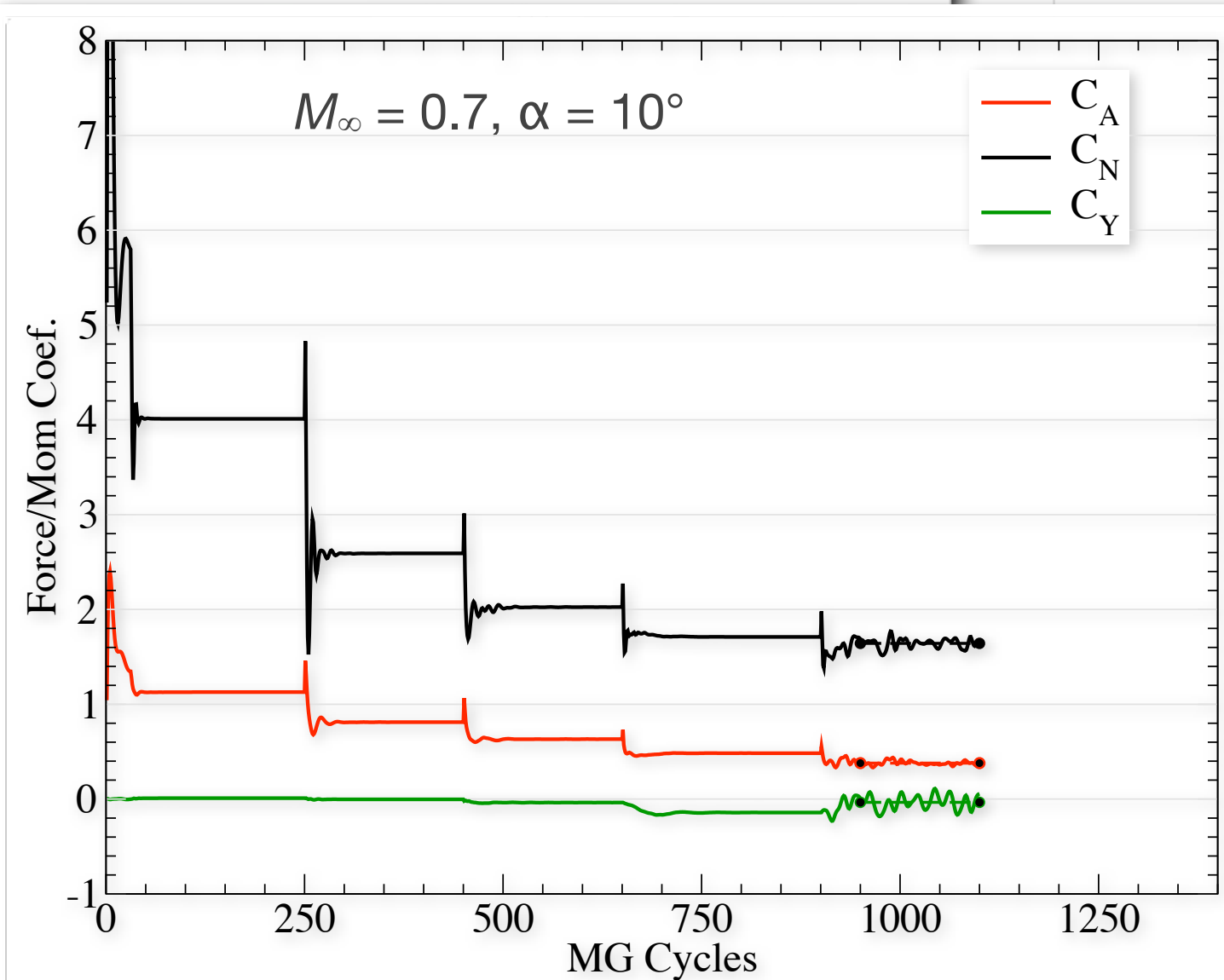
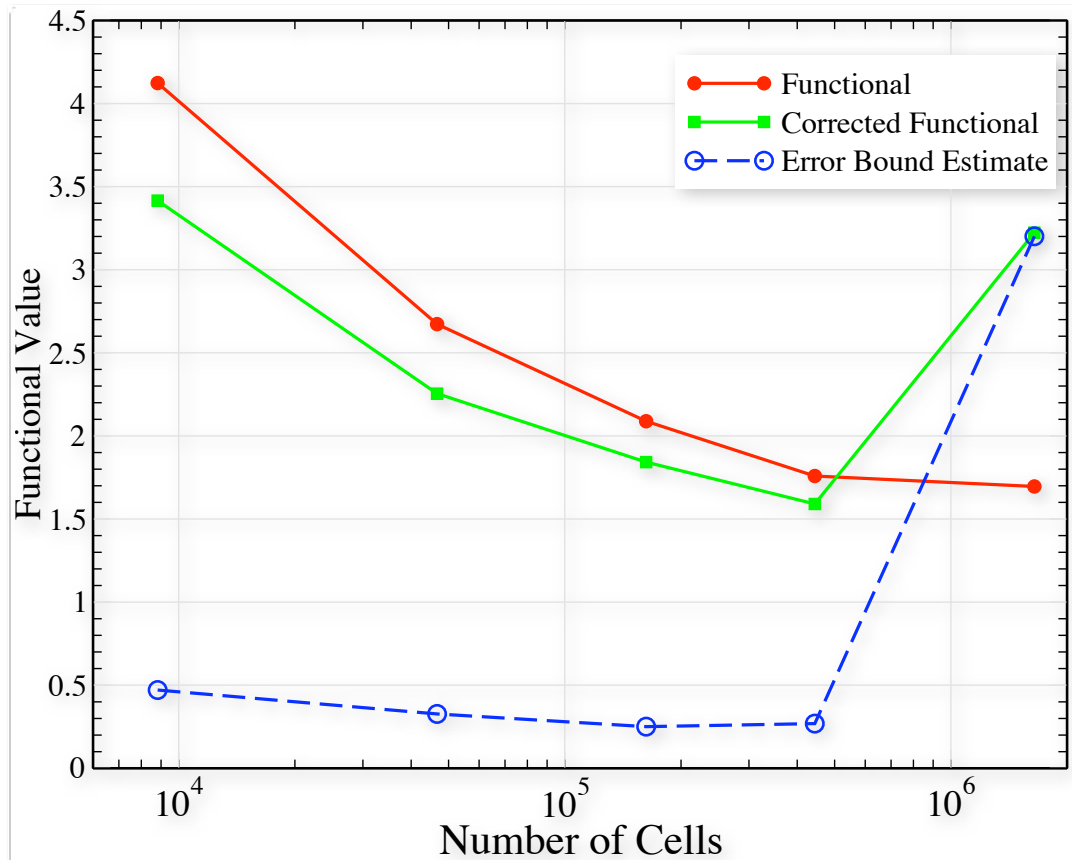


Database

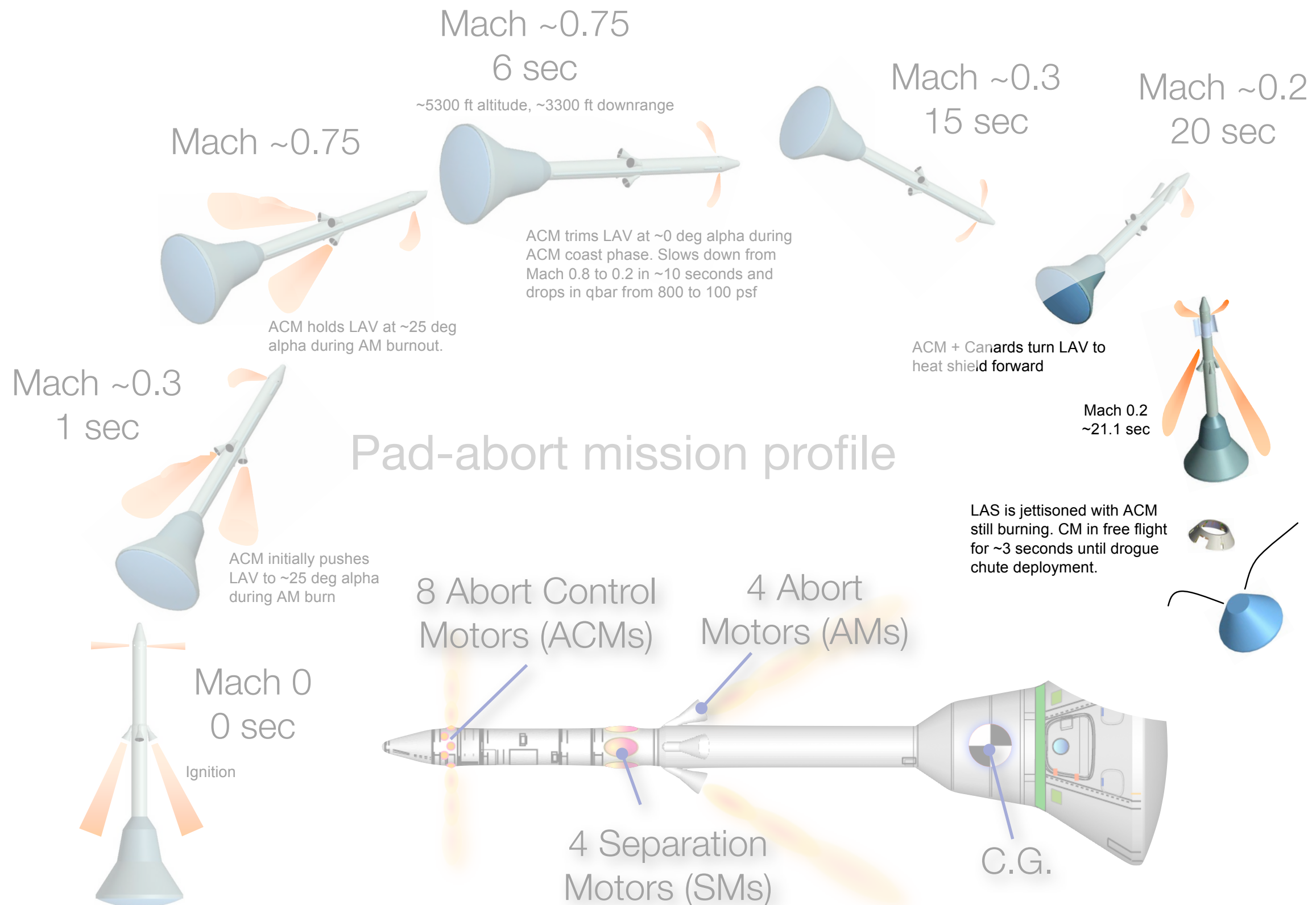




Database

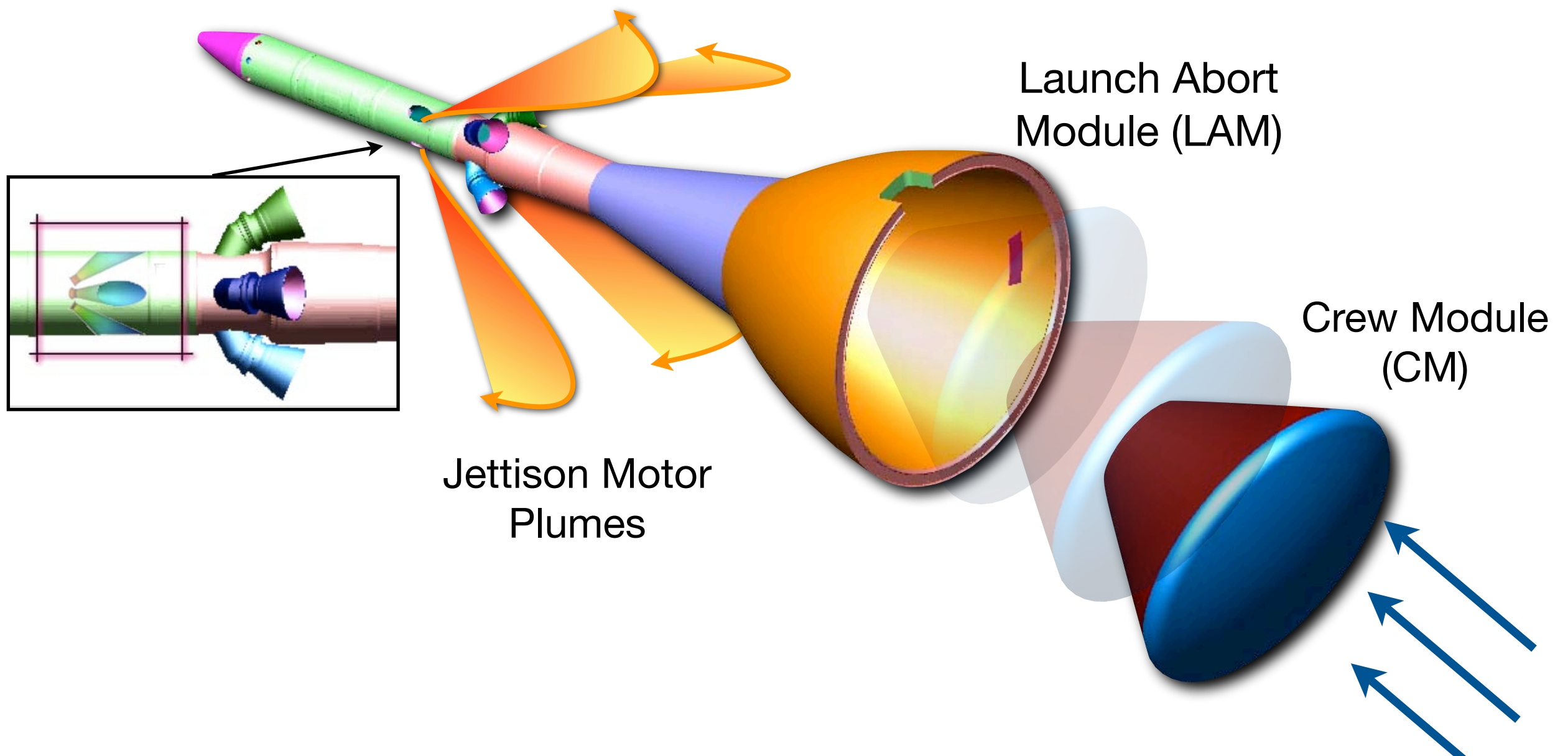


Launch Abort System Tower Jettison Database



Launch Abort System Tower Jettison

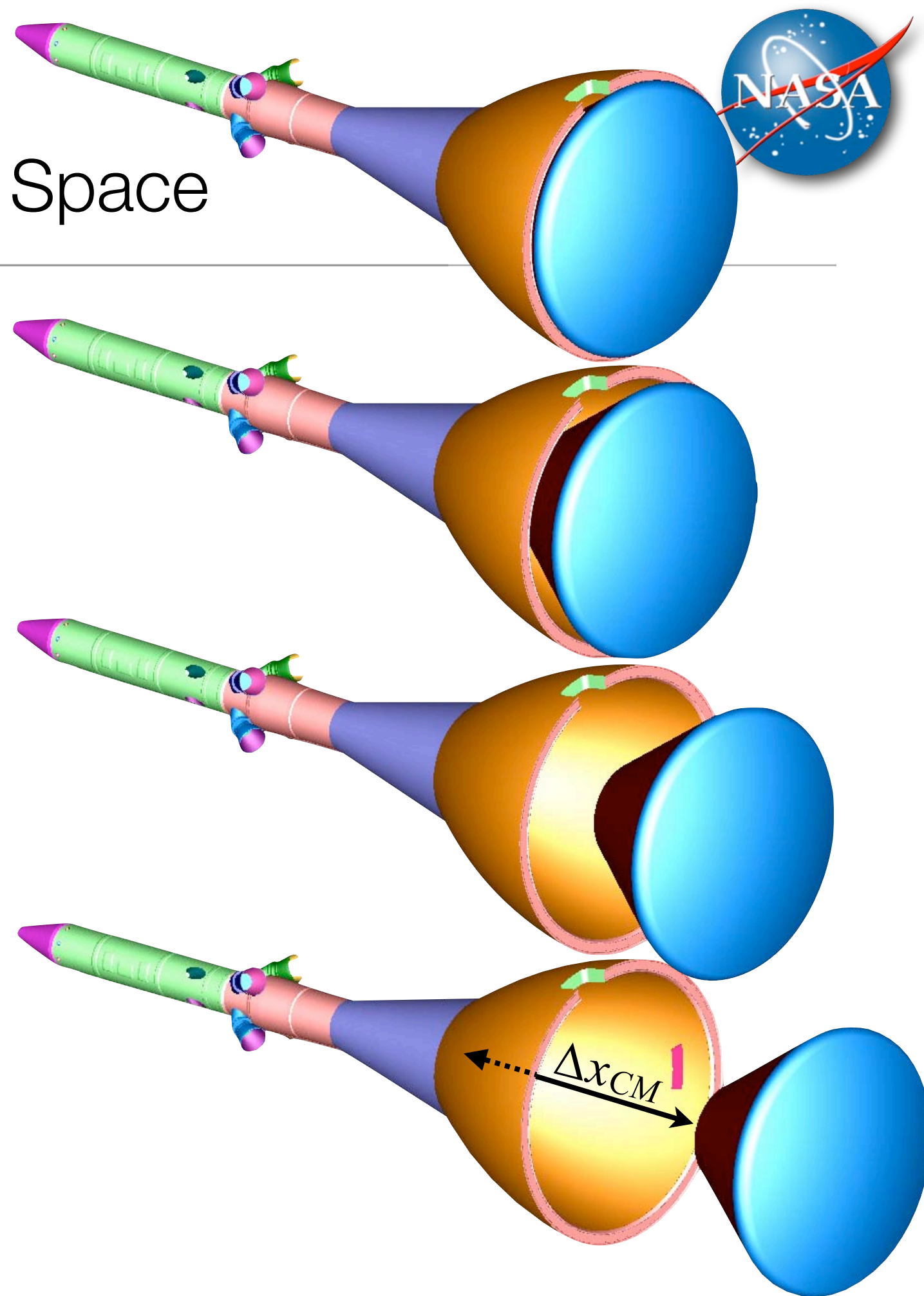
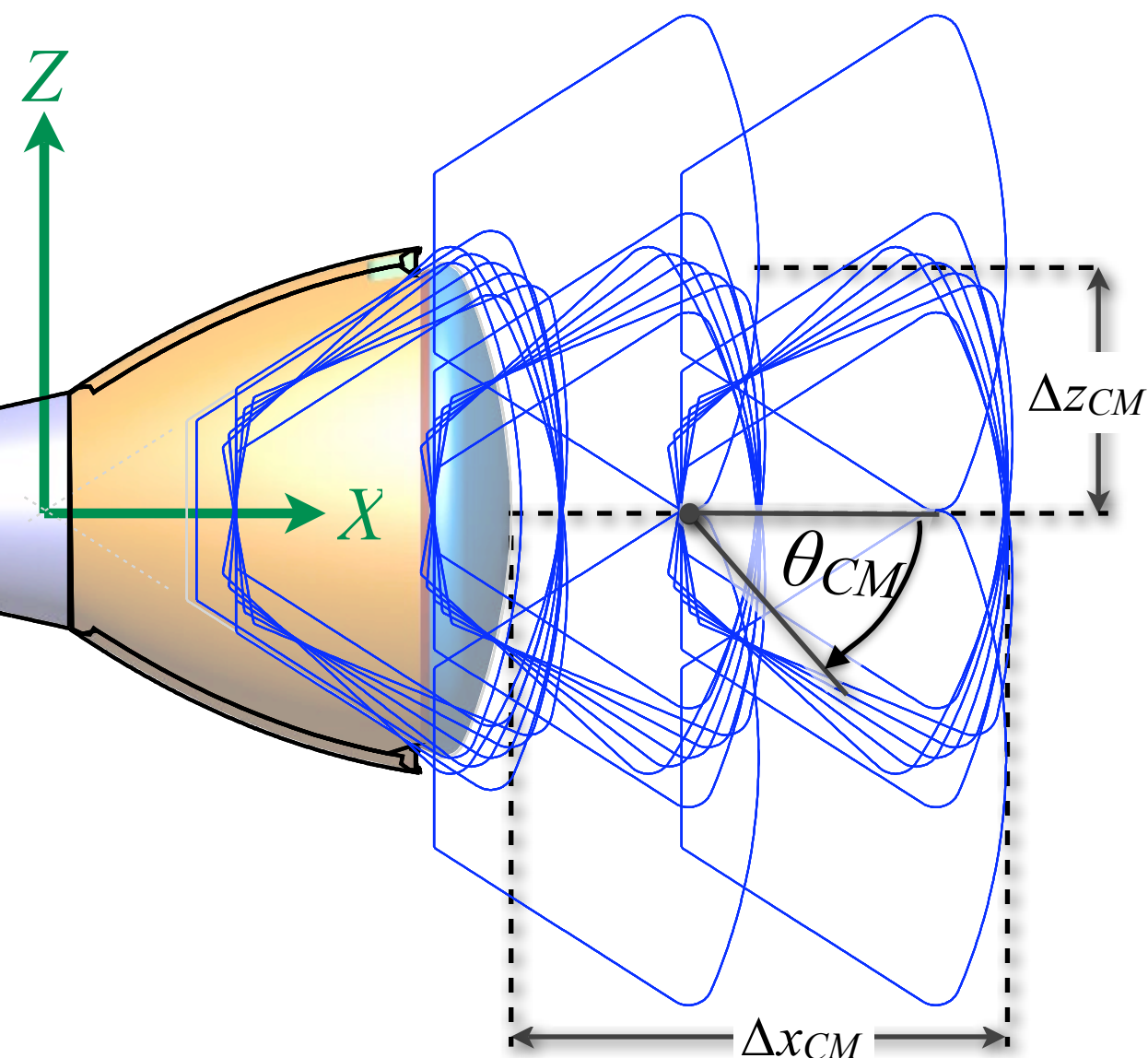
- Objective: Analyze aerodynamic forces and moments during LAS tower jettison
- Include effects of jettison motor firing with translation and rotation of the Crew Module (CM) relative to the Launch Abort Module





Geometry Configuration Space

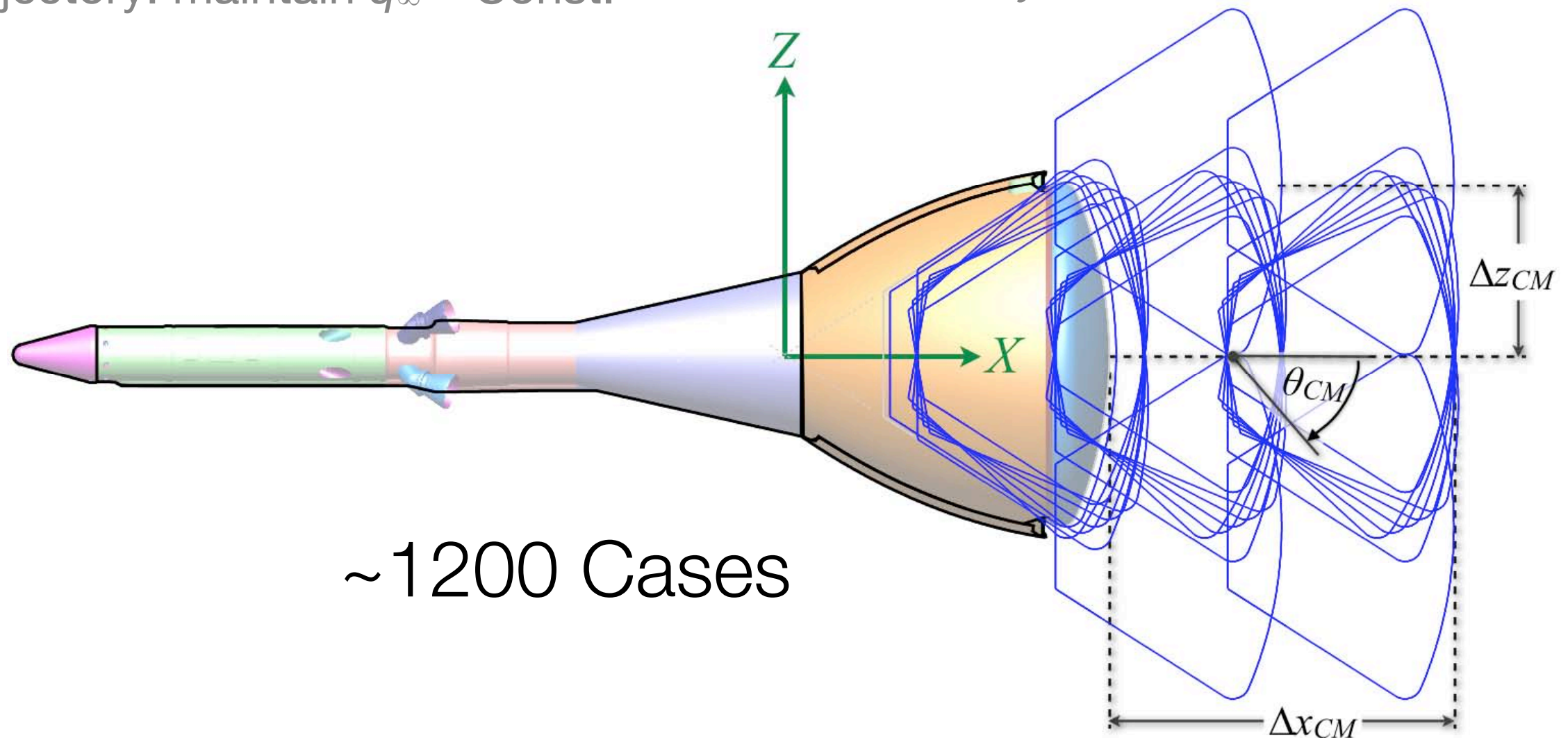
- Four configuration parameters for CM position and orientation:
 Δx , Δy , Δz , θ



Database Cases

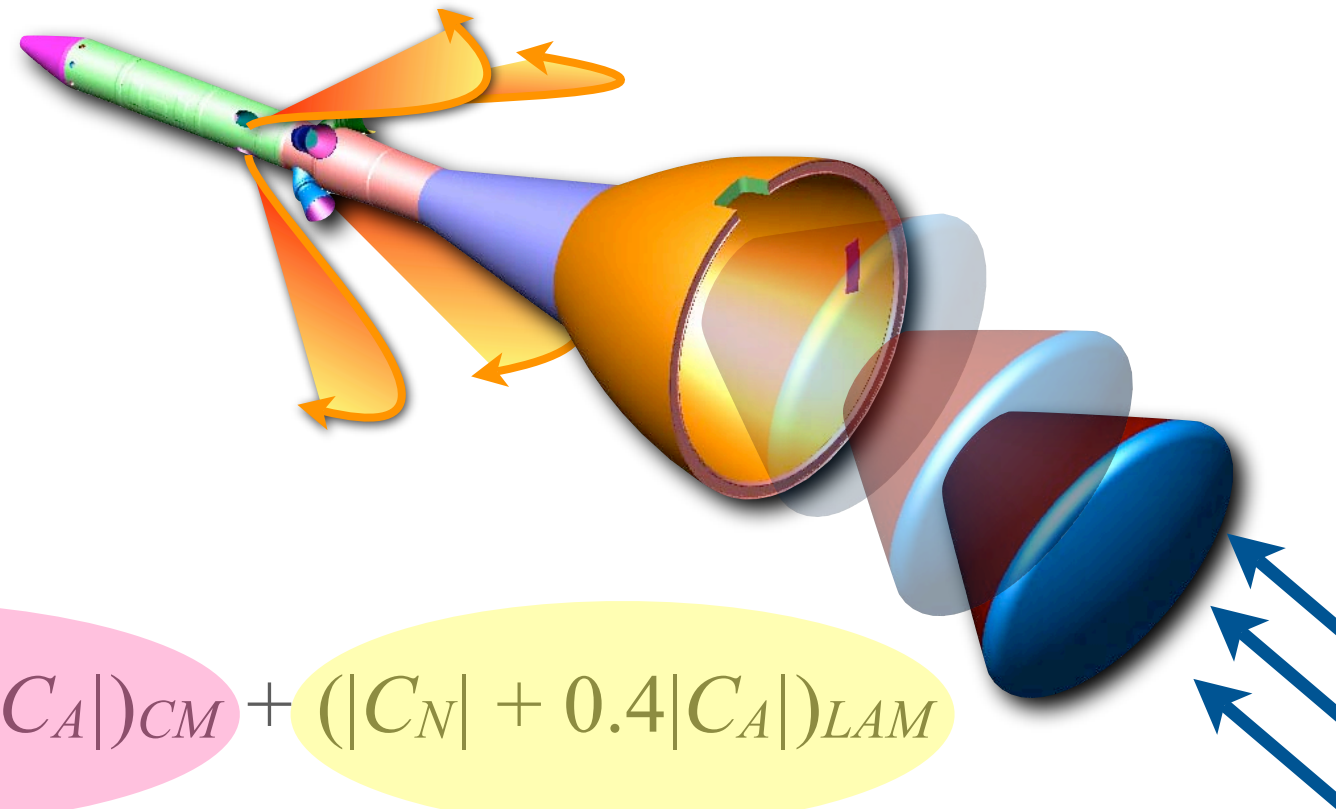
- Jettison Motor Plume Conditions:
 - JM on and JM off
 - Scale thrust for altitude
- Trajectory: maintain $q_\infty \approx \text{Const.}$

- Run Conditions:
 - $M_\infty = \{0.5, 0.7, 0.9, 1.1, 1.3, 1.6\}$
 - $\alpha = \{155^\circ, 160^\circ, 165^\circ, 170^\circ, 175^\circ, 180^\circ\}$
 - $\beta = \{0^\circ, 5^\circ\}$
 - $CM\Delta x, CM\Delta y, CM\Delta z, CM\Delta\theta$



Functional and Adaptation Strategy

- Challenging simulations
 - ▶ Complex, detailed geometry
 - ▶ Bodies in close proximity
 - ▶ Strong *upstream-firing* jets
 - ▶ Shocks and wakes



- Output functional: $J = (0.8|C_N| + 0.2|C_A|)_{CM} + (|C_N| + 0.4|C_A|)_{LAM}$

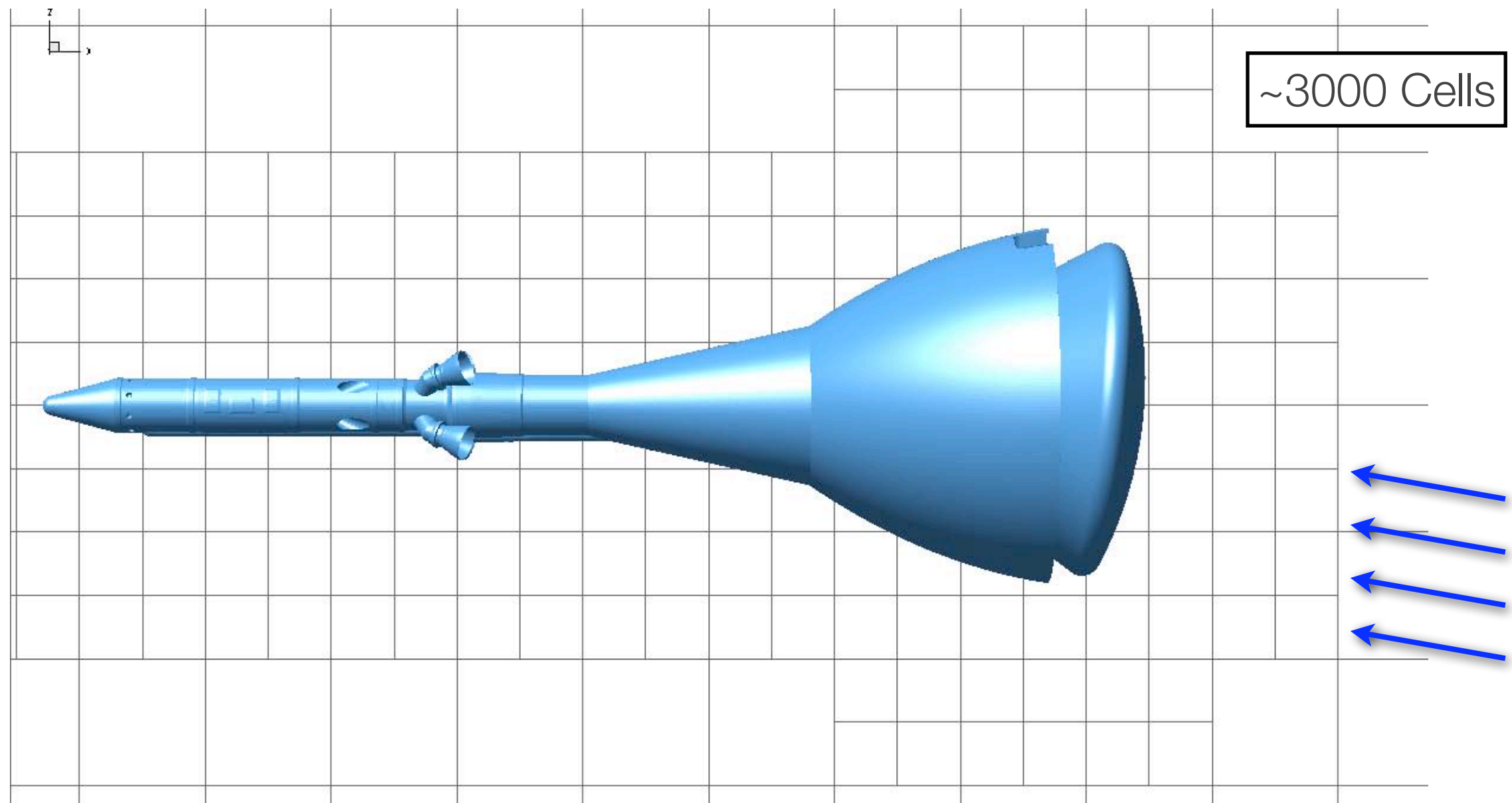
Capture forces on CM

Capture forces on tower

- Solution technique is a compromise since most of these cases are unsteady, and need high resolution
 - ▶ Want the best answer as cheaply as possible
- Adaptation follows “worst-things-first” strategy (AIAA 2008-0725)
 - ▶ Refine largest contributors to output error first

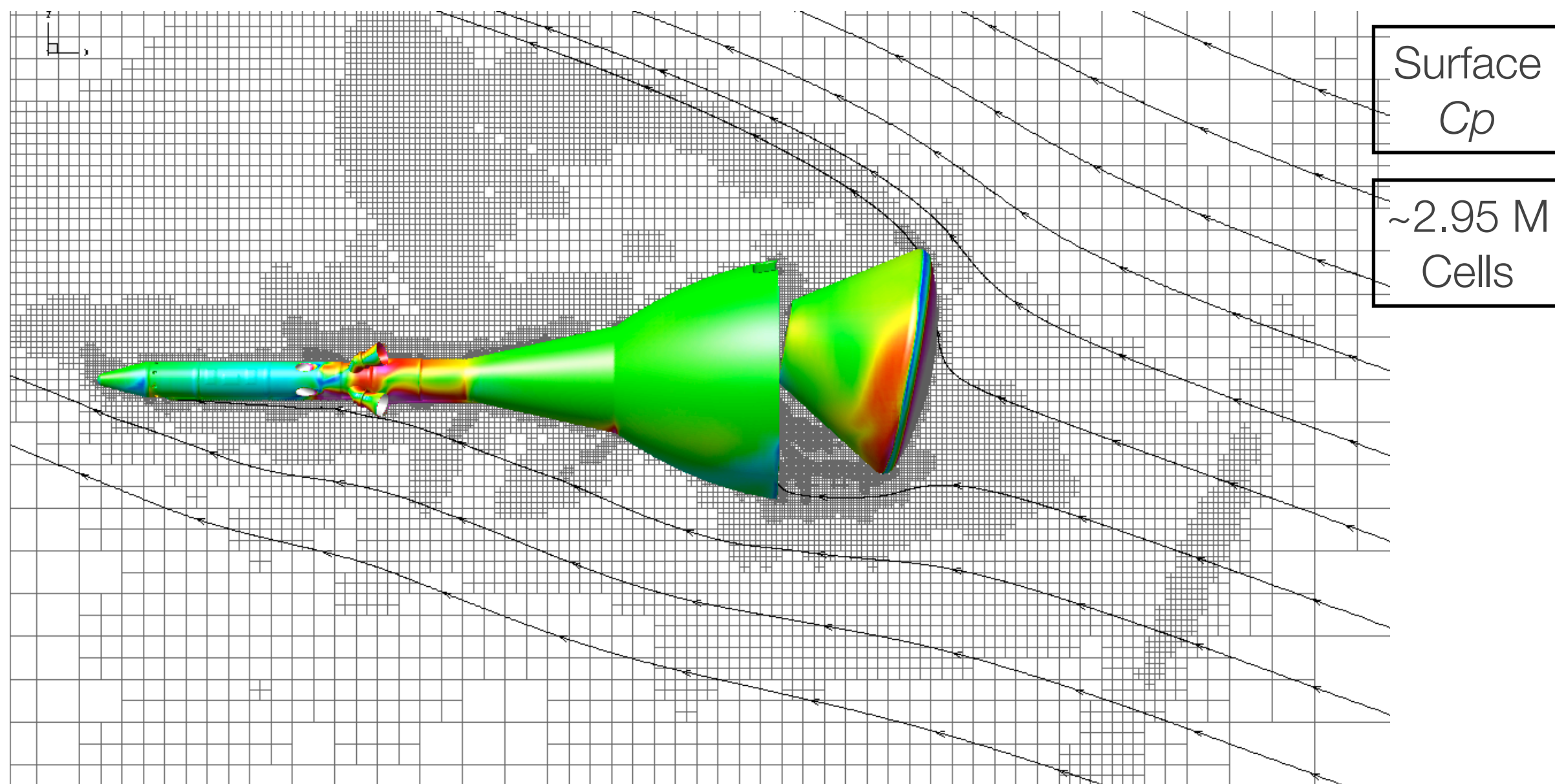
Initial Mesh

- Background mesh essentially symmetric and coarse to avoid biasing solution



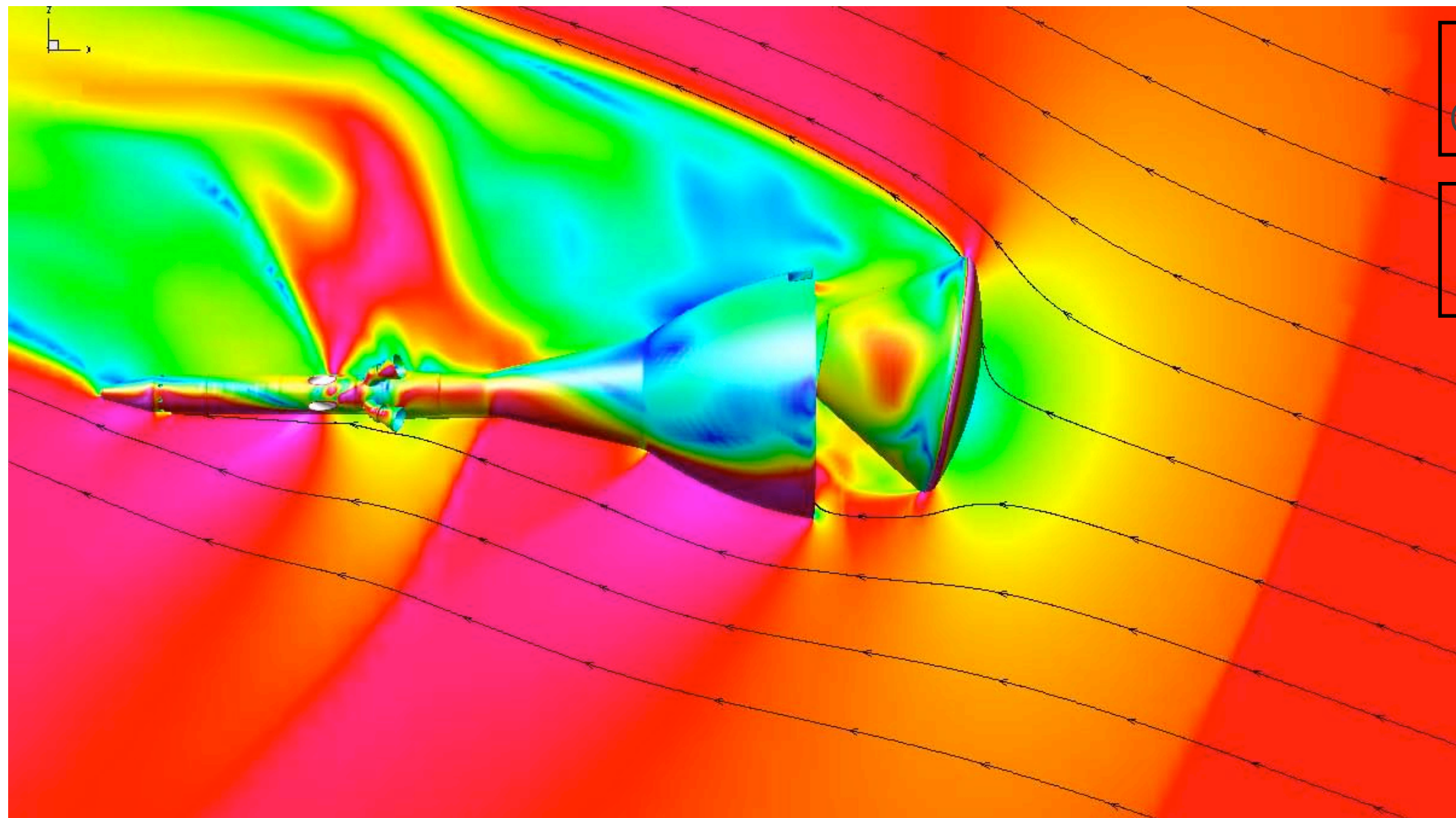
Example Final Mesh (10 Adapt Cycles)

- Output functional: $J = (0.8|C_N| + 0.2|C_A|)_{CM} + (|C_N| + 0.4|C_A|)_{LAM}$
- $M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$



Example Final Solution (10 Adapt Cycles)

- Output functional: $J = (0.8|C_N| + 0.2|C_A|)_{CM} + (|C_N| + 0.4|C_A|)_{LAM}$
- $M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$



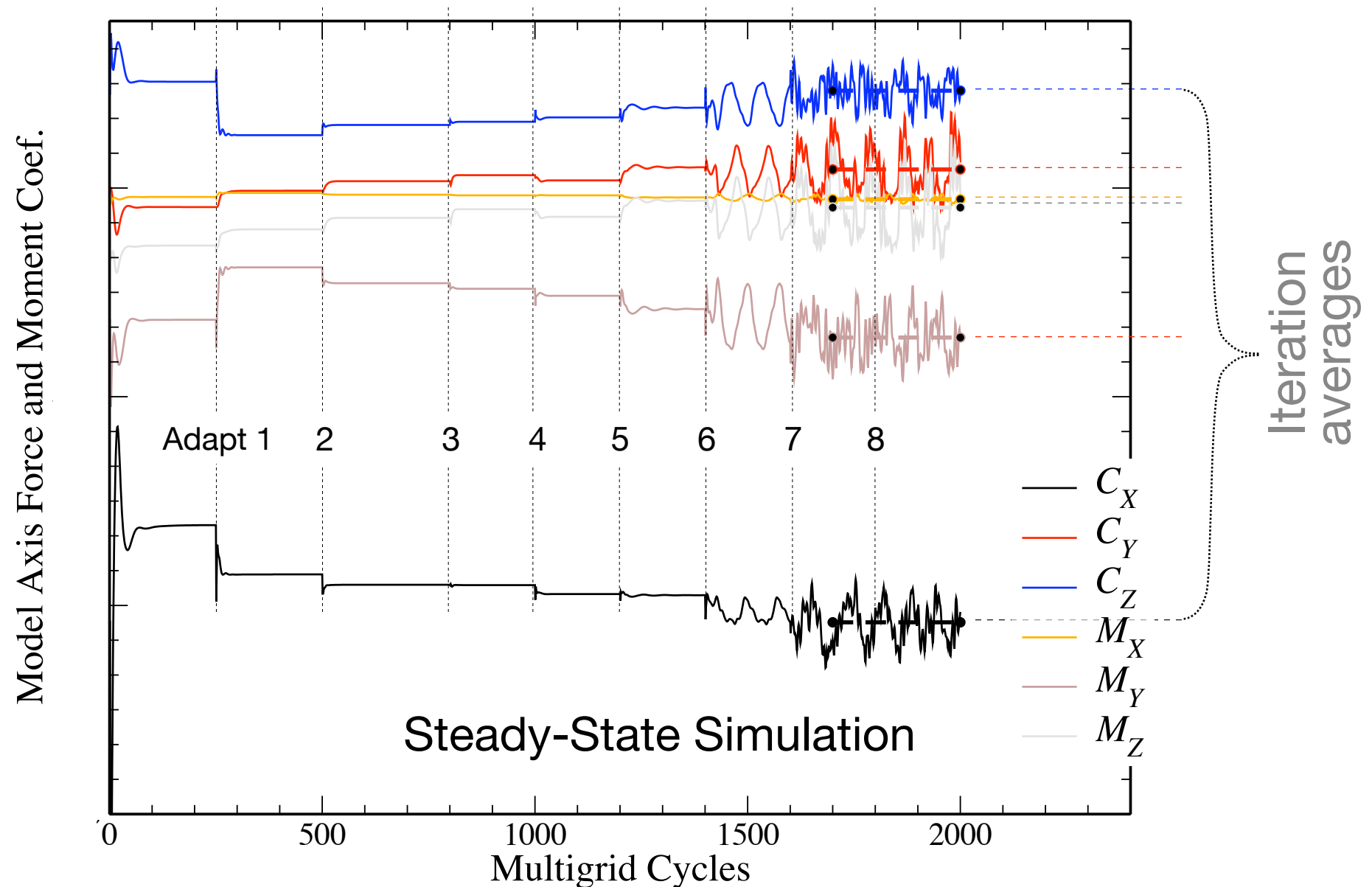
Mach
Contours

~2.95 M
Cells



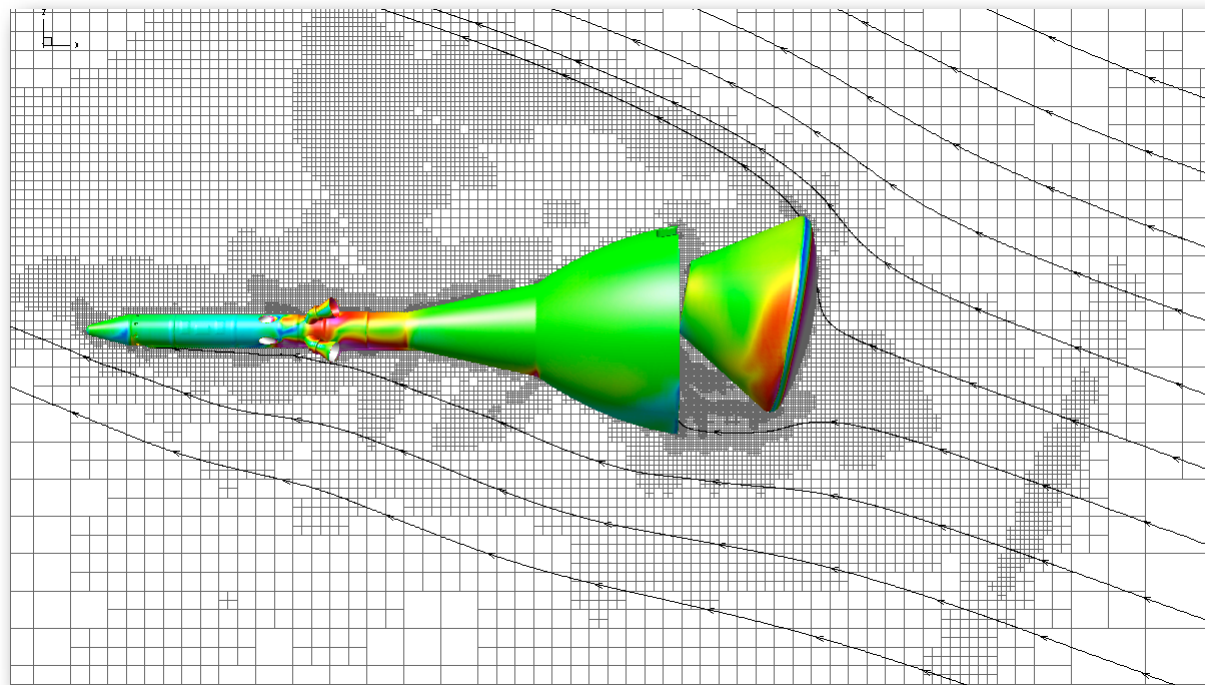
Convergence of Aerodynamic Coefficients

- Output functional: $J = (0.8|C_N| + 0.2|C_A|)_{CM} + (|C_N| + 0.4|C_A|)_{LAM}$
- $M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$
- Convergence of forces and moms. on CM with mesh refinement

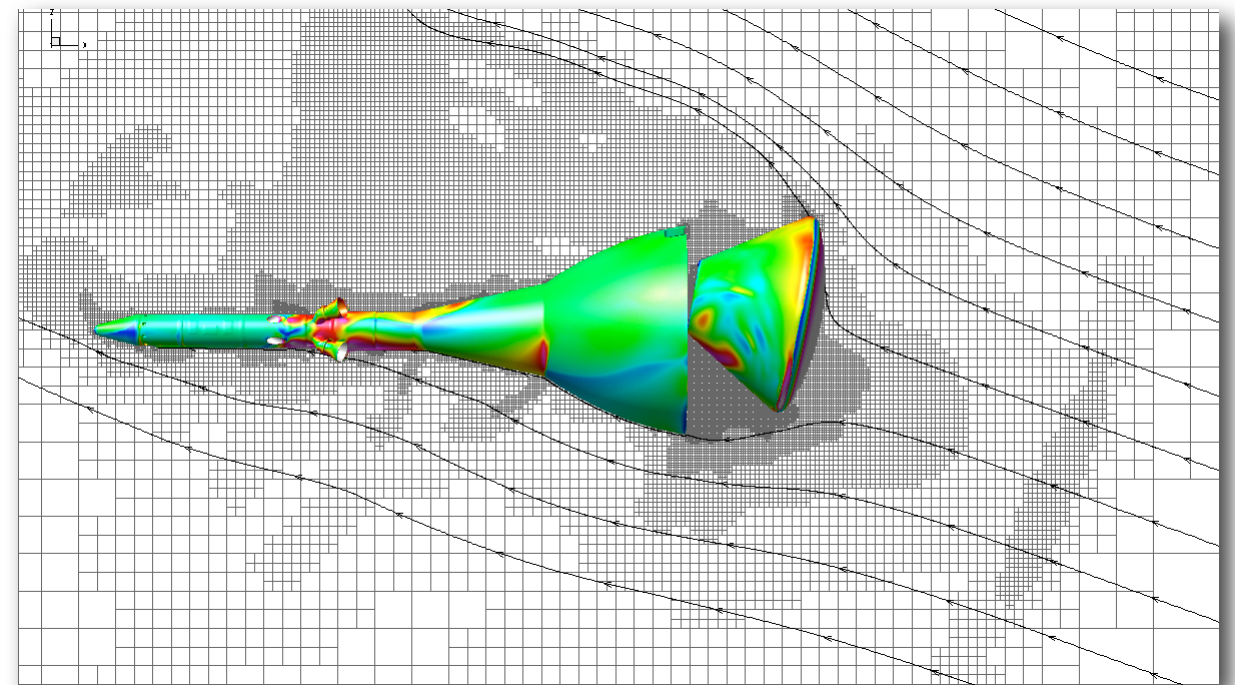


Comparison with Unsteady Simulation

- How do these iteration averages compare with unsteady simulation?
- Performed comparisons at Mach 0.7, & 1.1
- “Best unsteady mesh” generated by 1 additional refinement of steady mesh, using low threshold to “fill out” adaptation regions
- Example case: $M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$



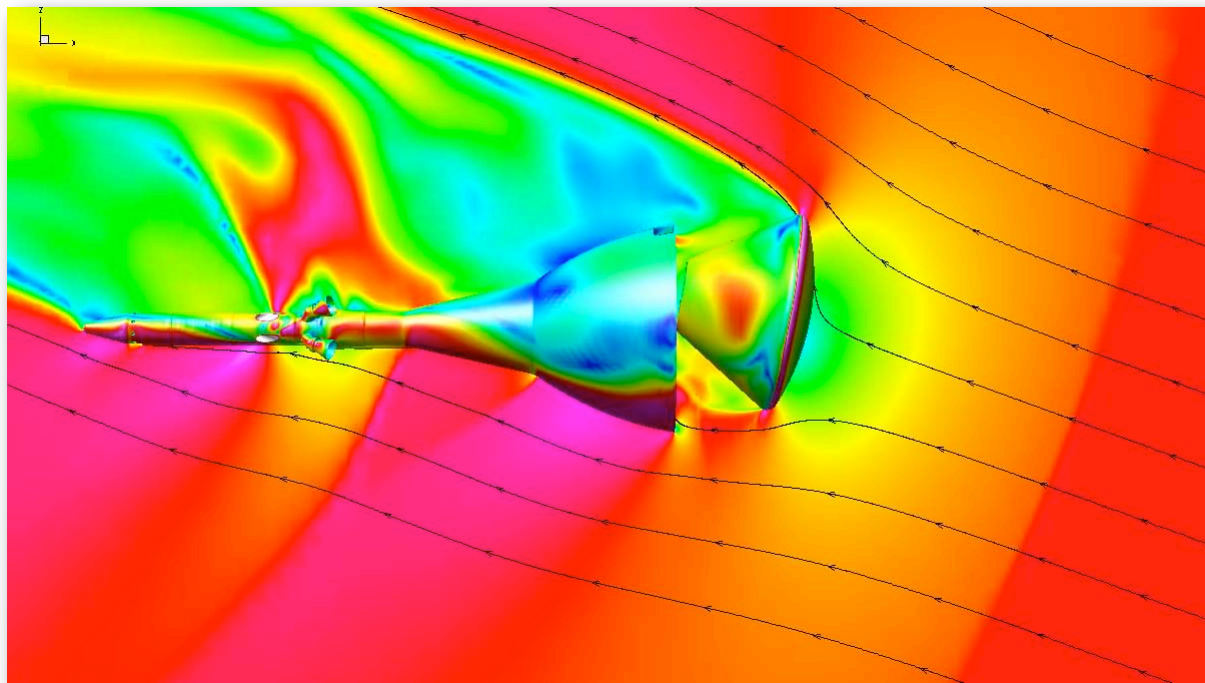
Steady mesh & C_p , ~2.95 M Cells



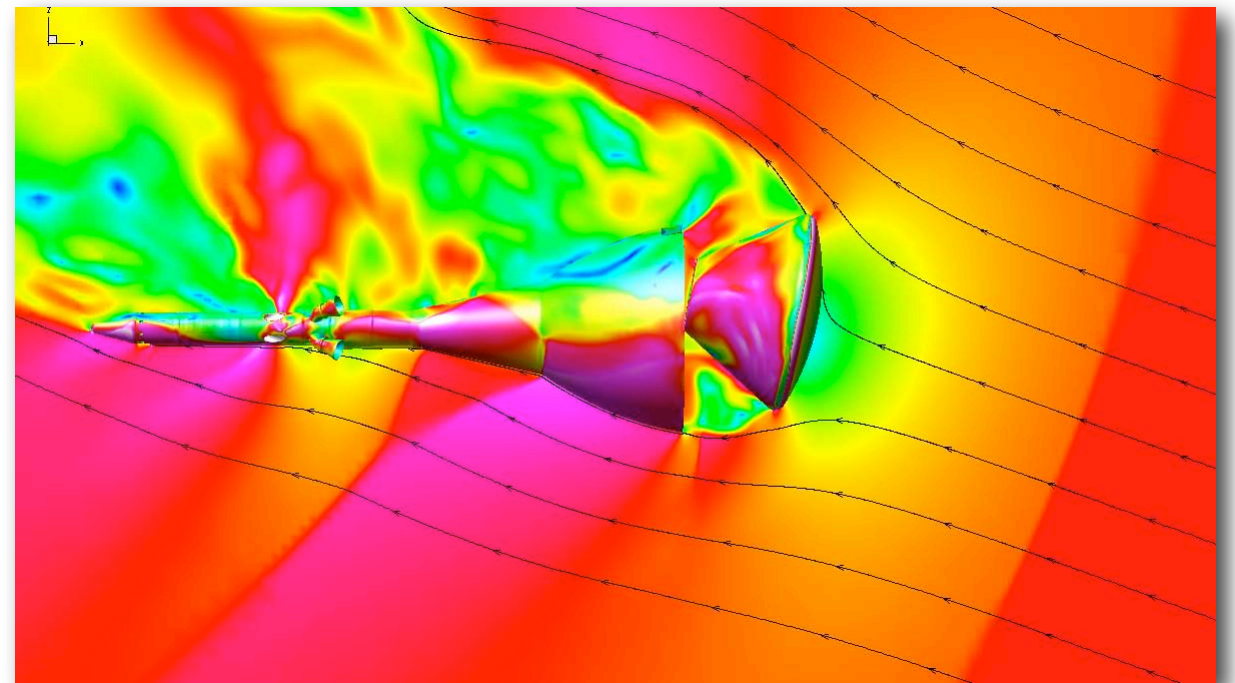
Unsteady mesh & C_p , ~5.2 M Cells

Comparison with Unsteady Simulation

- How do these iteration averages compare with unsteady simulation?
- Performed comparisons at Mach 0.7, & 1.1
- “Best unsteady mesh” generated by 1 additional refinement of steady mesh, using low threshold to “fill out” adaptation regions
- Example case: $M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$



Steady mesh iso-Mach, ~2.95 M Cells

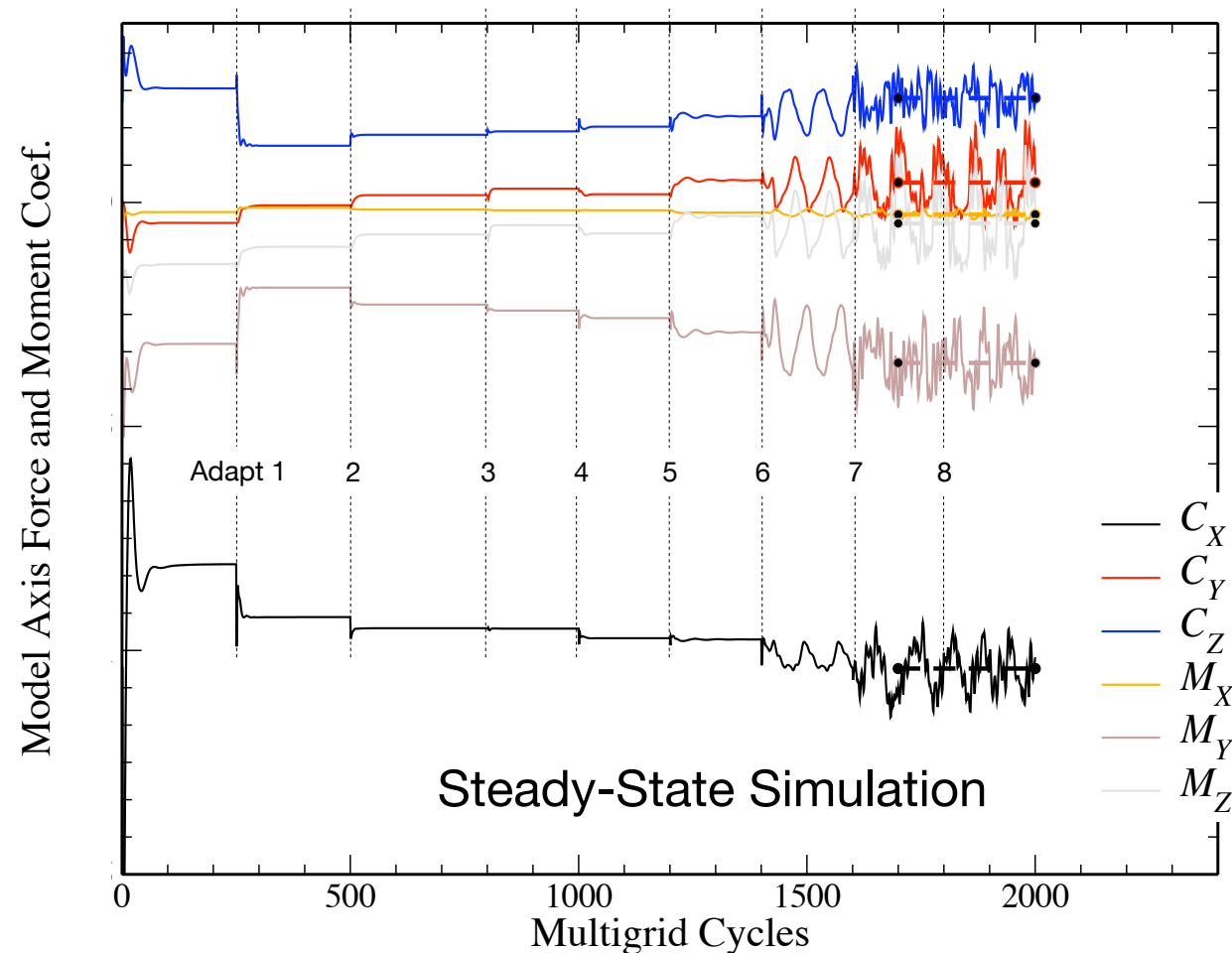


Unsteady mesh iso-Mach, ~5.2 M Cells

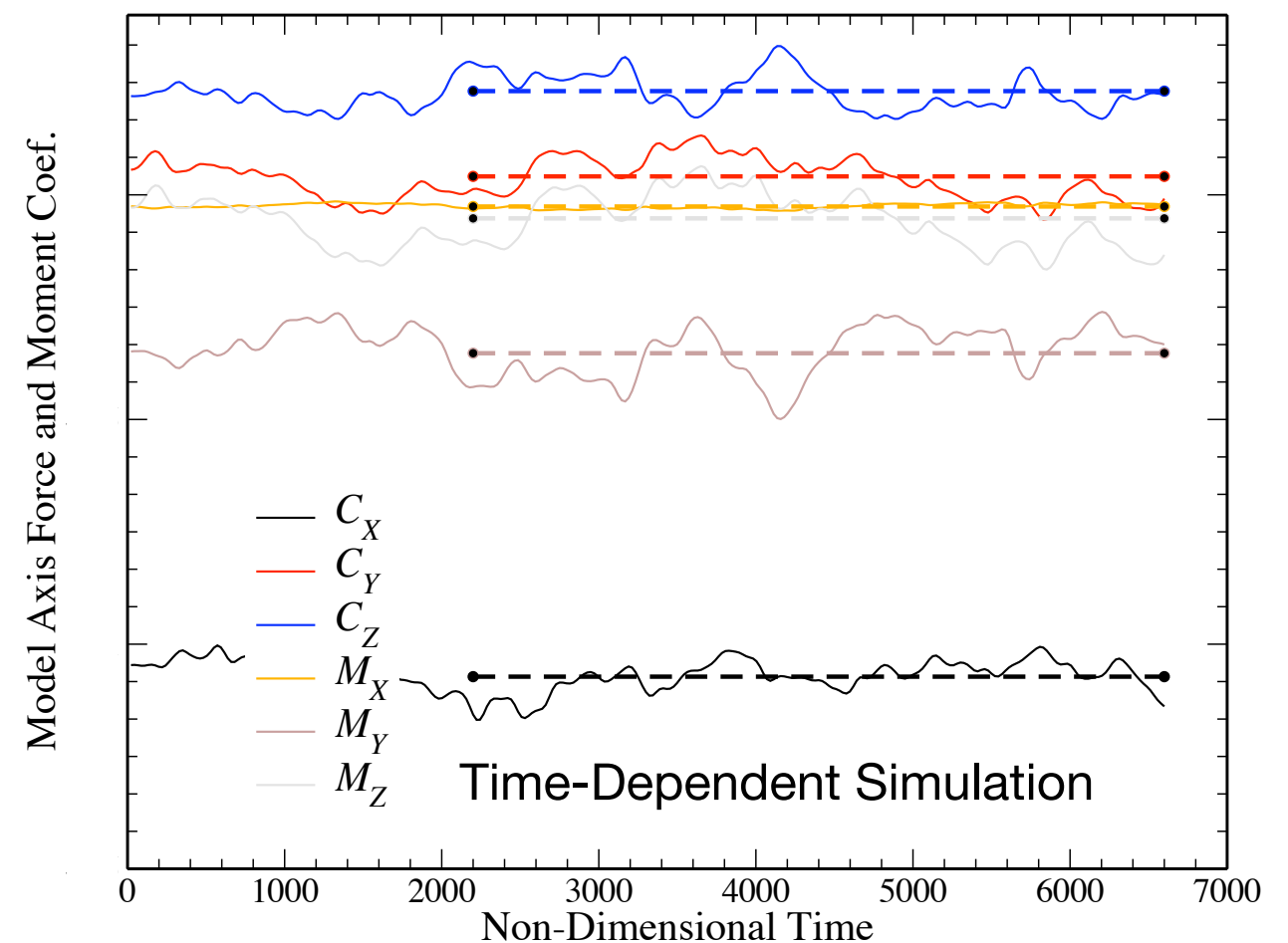
Comparison with Unsteady Simulation

$M_\infty = 1.1$, $\alpha = 160^\circ$ with the CM @ $(\Delta x, \Delta y, \Delta z, 10^\circ)$

Steady, ~2.95M Cells



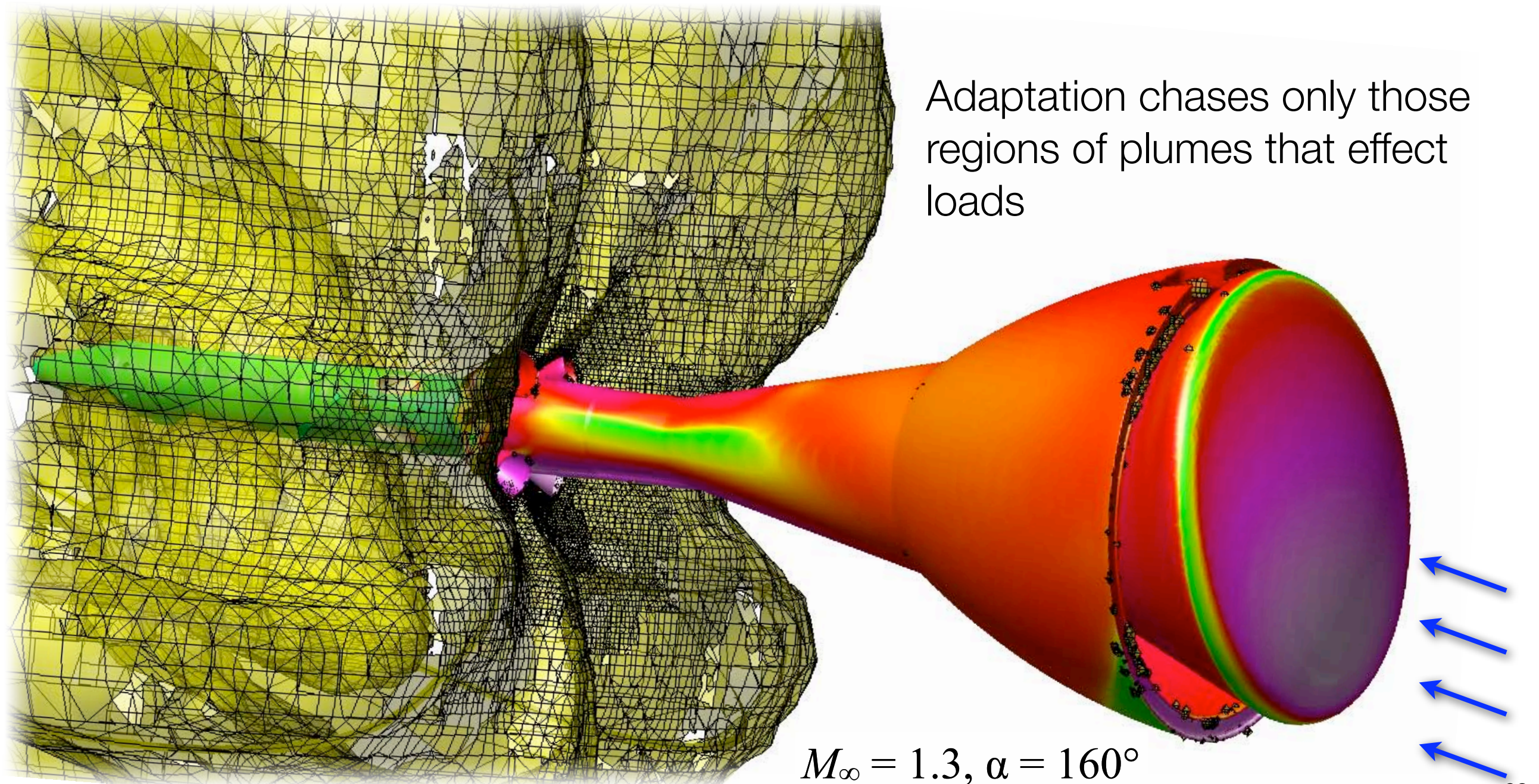
Unsteady, ~5.2M Cells



- Agreement to third significant digit
- Differences in averages are same size as differences due to averaging window
- Similar results for other components at both Mach 0.7 & Mach 1.1

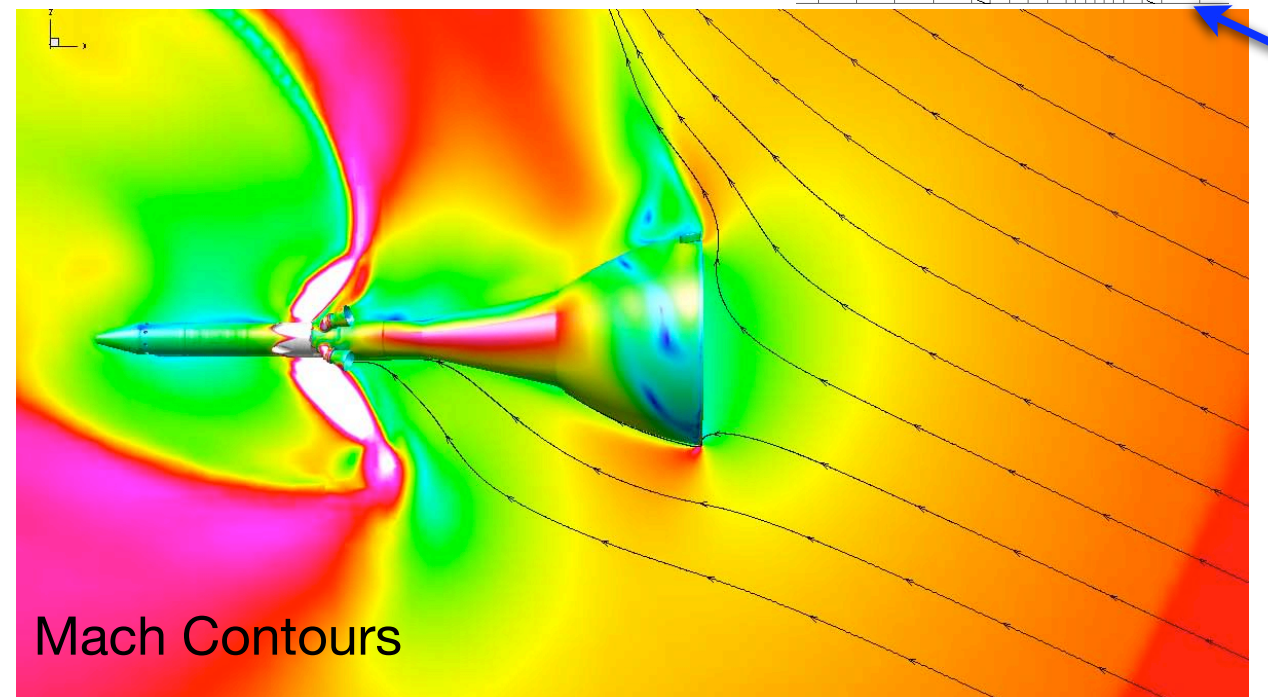
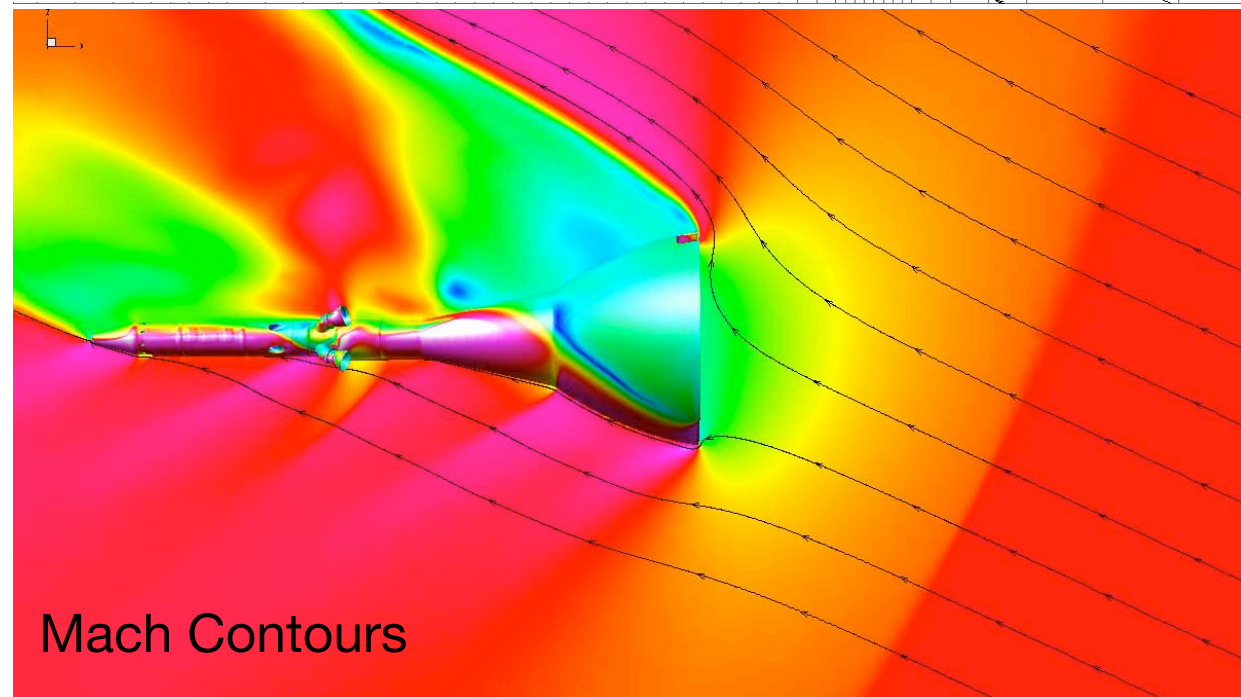
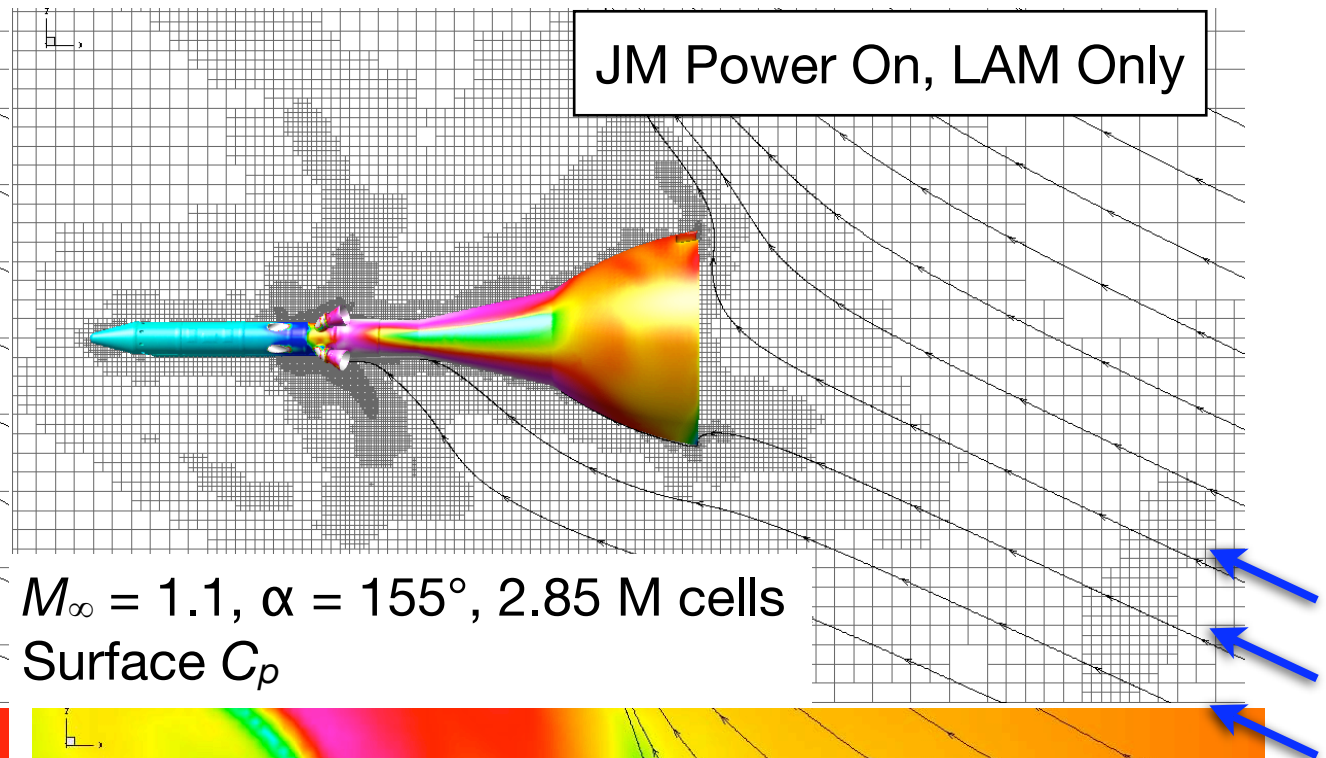
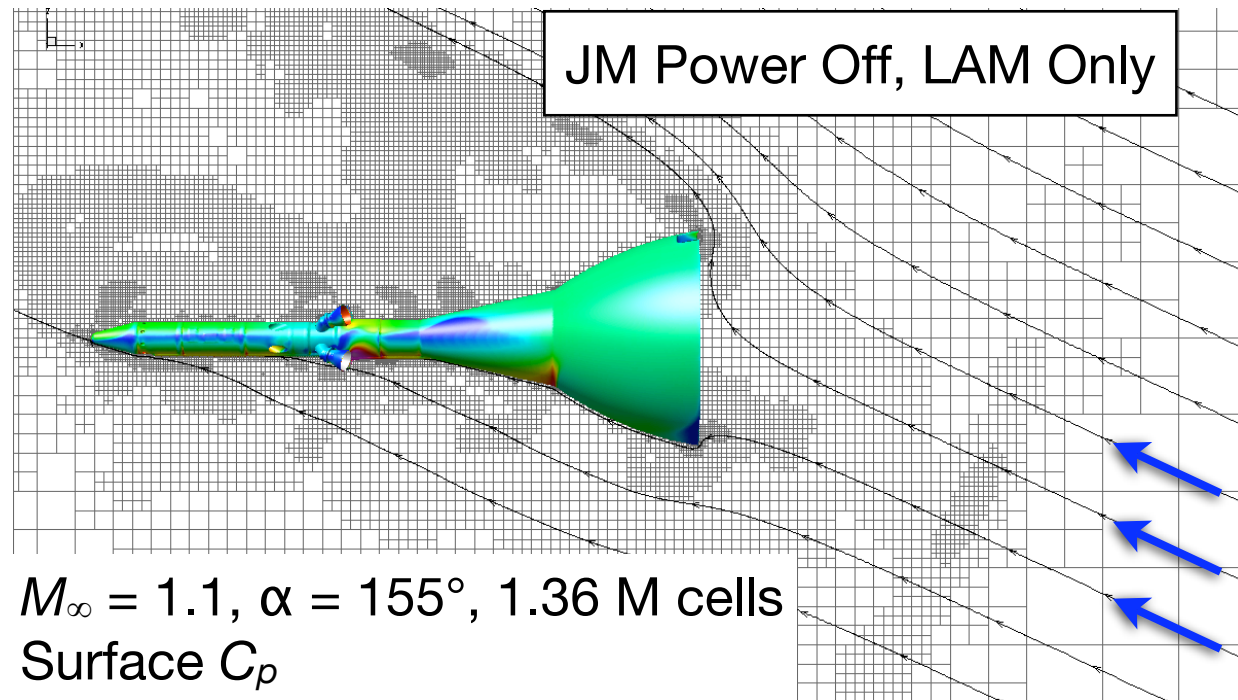
Plume Shape

T_o iso-surface showing approximate plume shape





Comparison of JM On and Off Flowfields



JM plumes move bow shock ~18 ft upstream

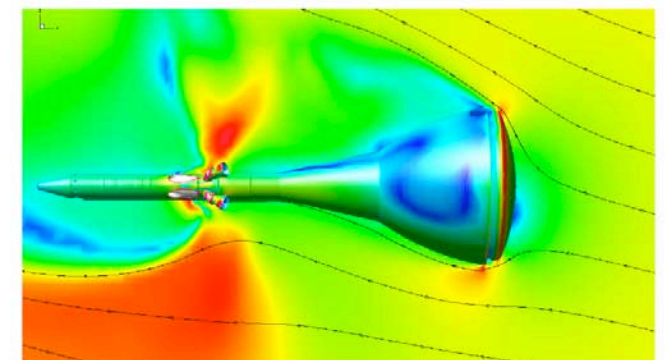
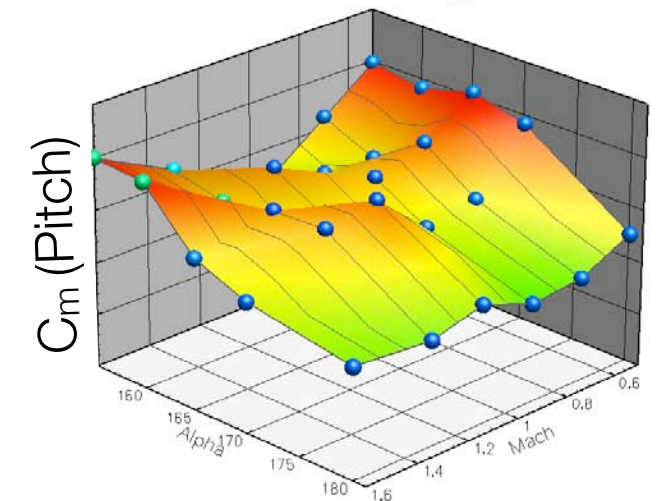
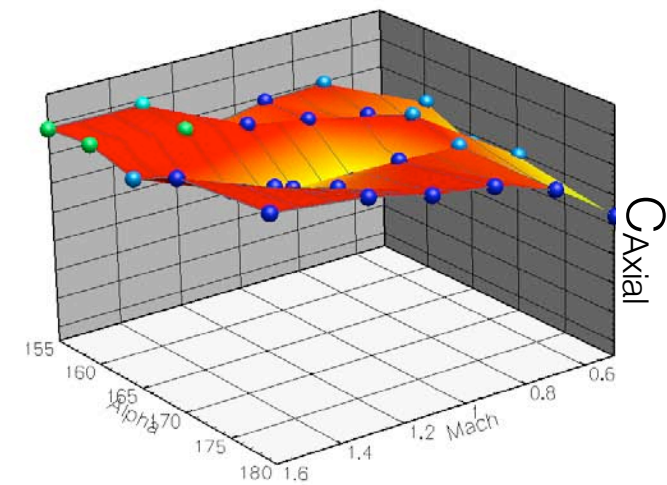
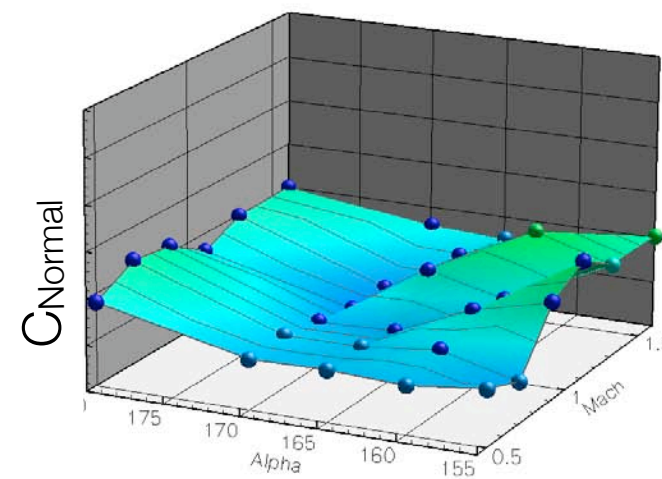
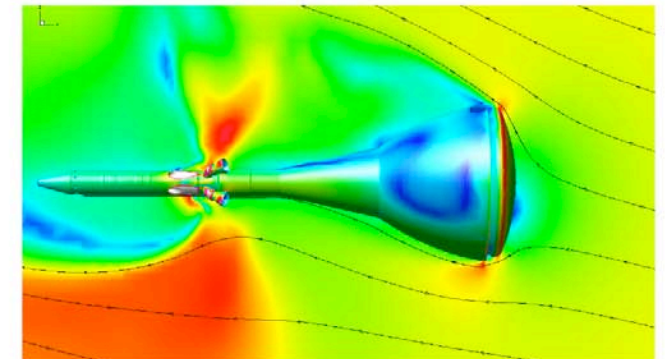
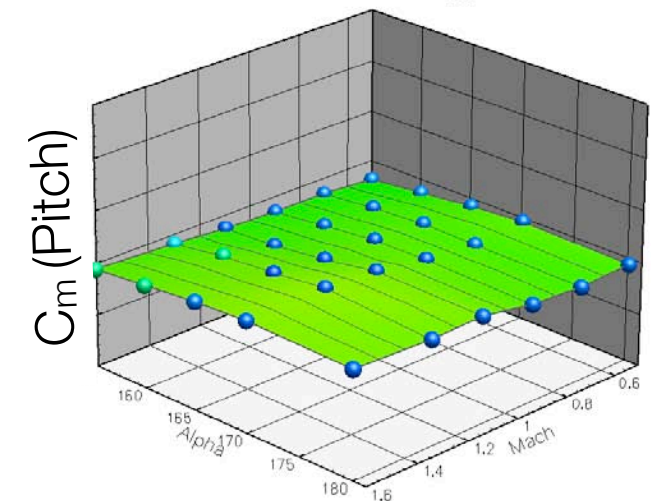
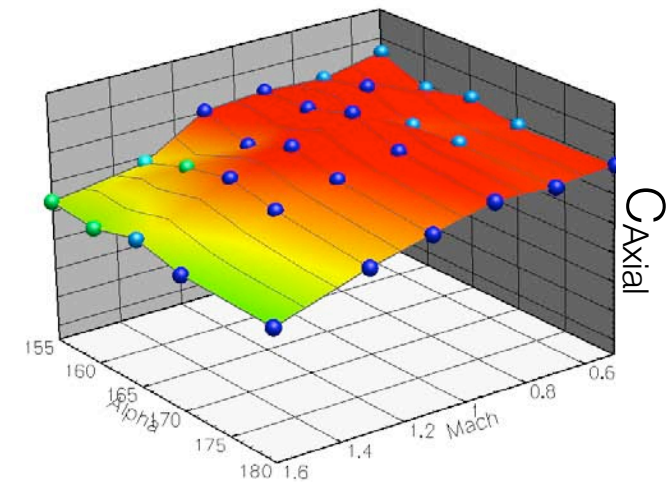
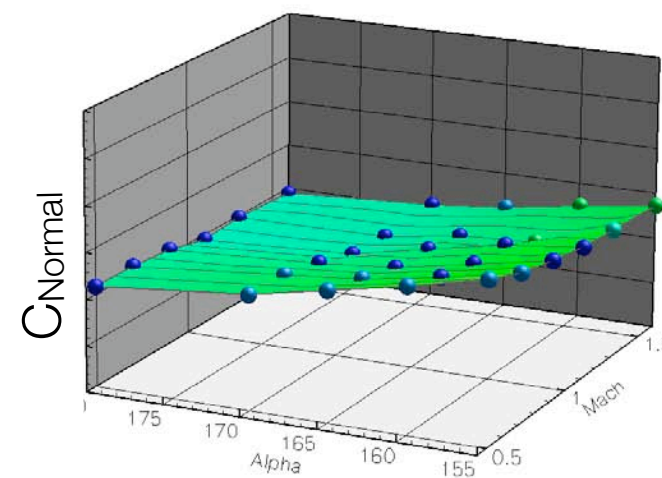
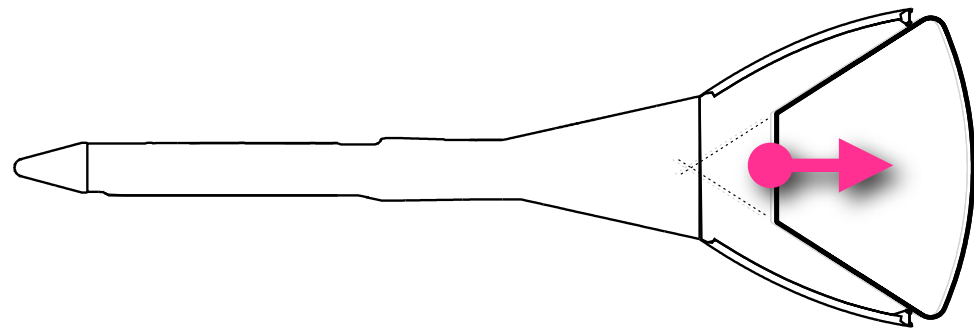
Database Samples

Loads on CM and LAM in proximity

$(\Delta x, 0.0, 0.0, 0^\circ)$

Loads on CM

Loads on LAM



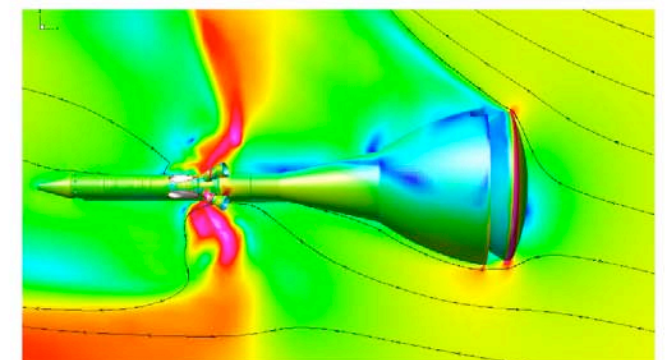
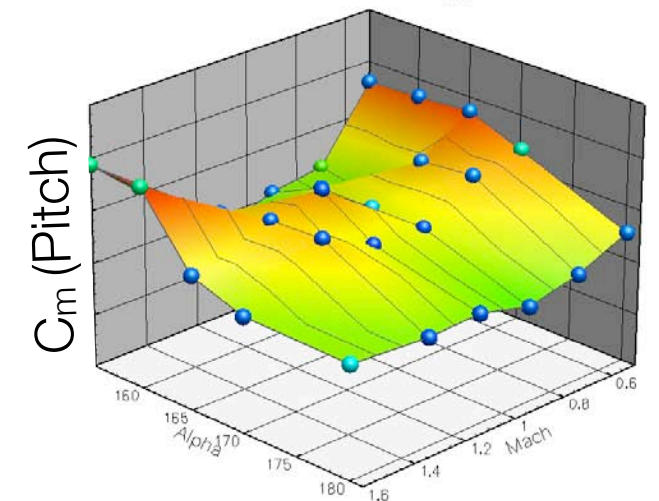
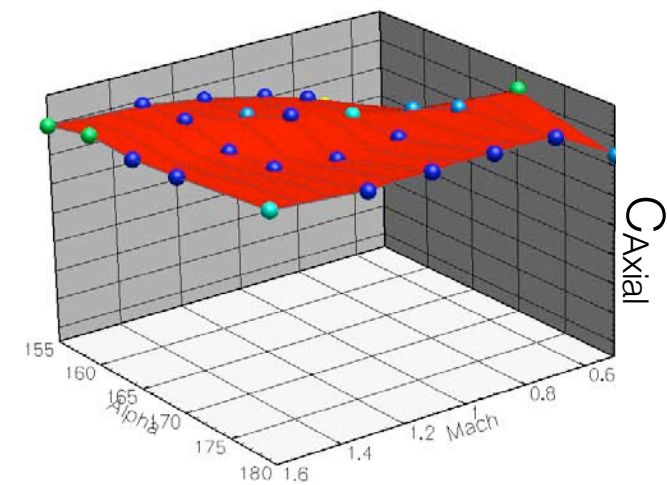
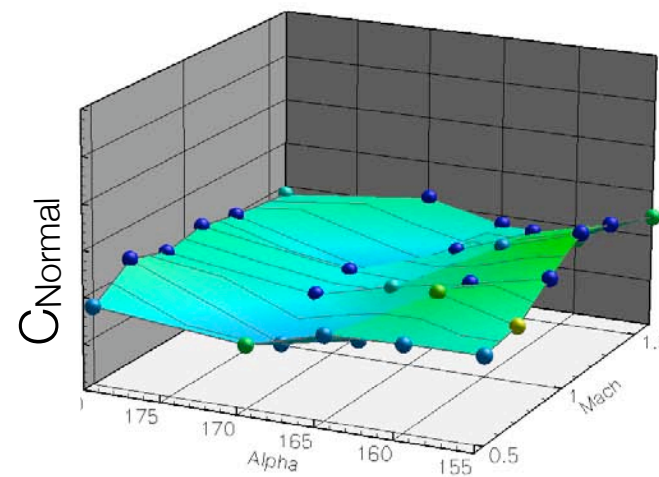
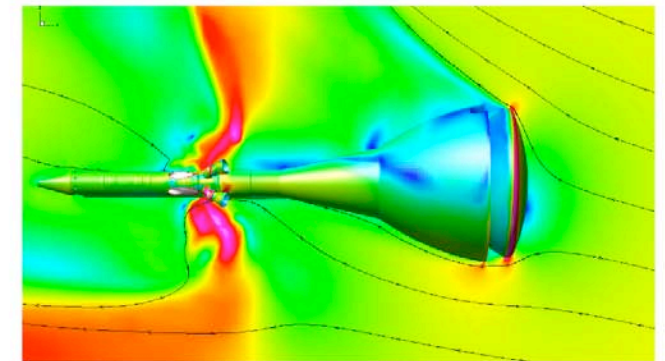
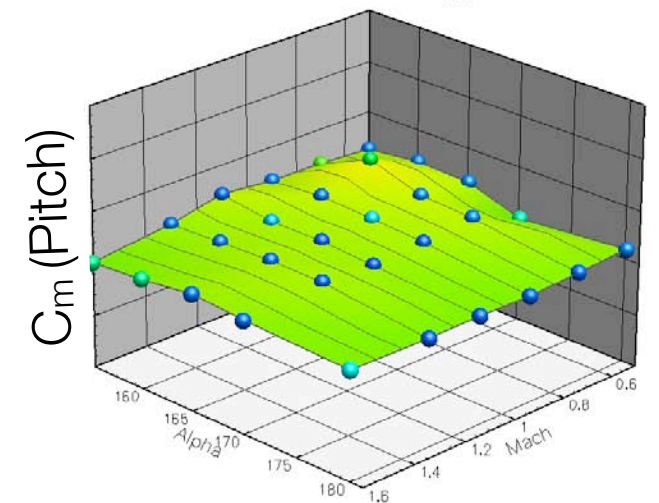
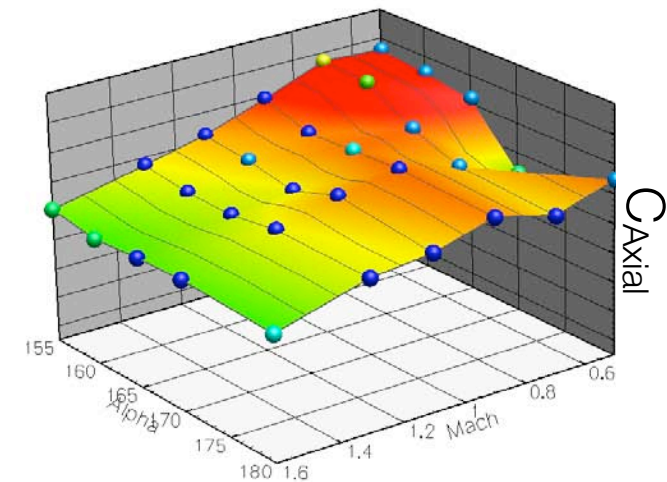
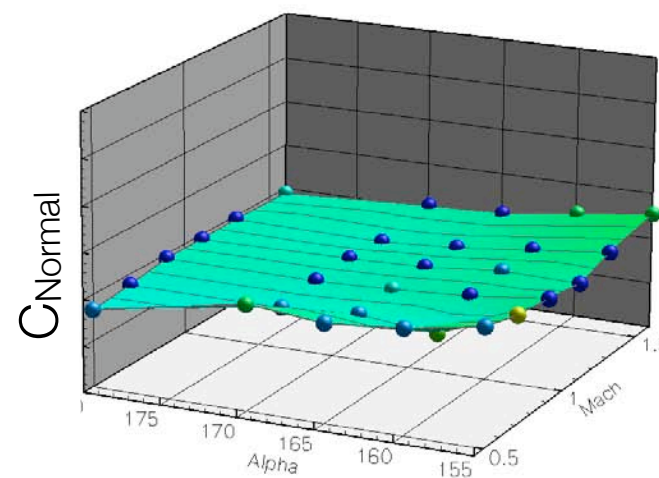
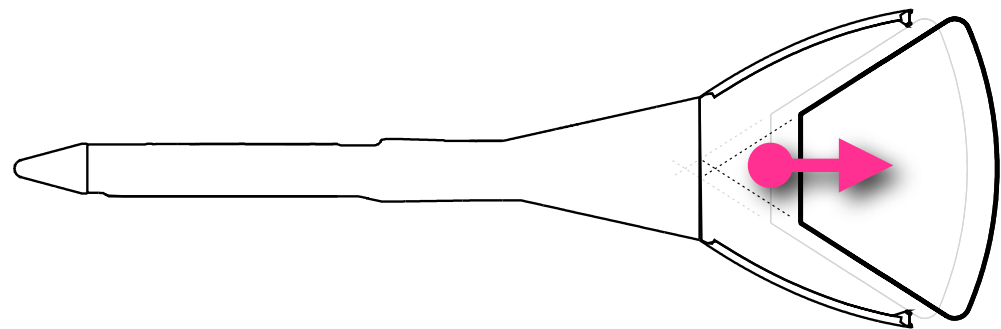
Database Samples

Loads on CM and LAM in proximity

$(\Delta x, 0.0, 0.0, 0^\circ)$

Loads on CM

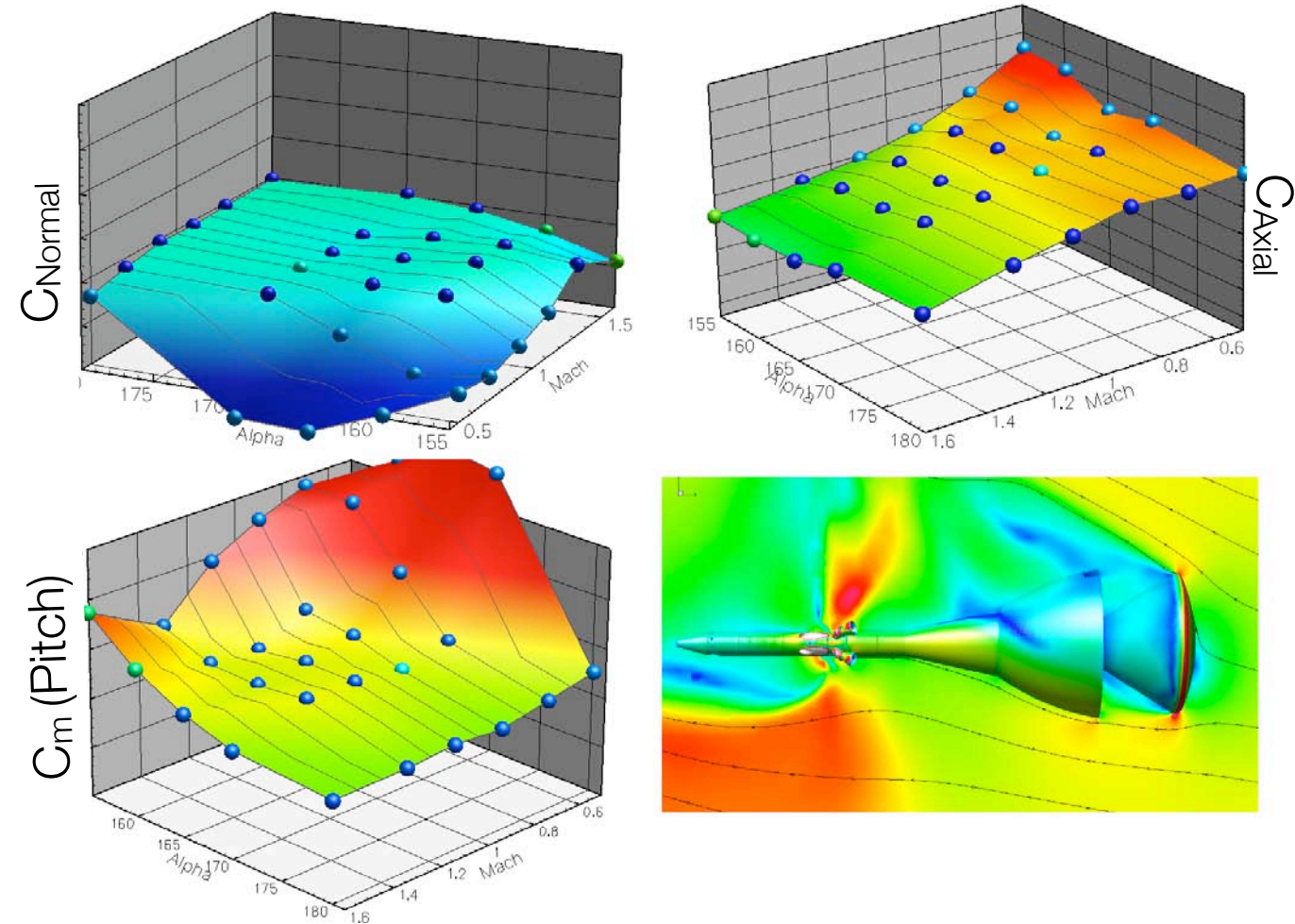
Loads on LAM



Database Samples

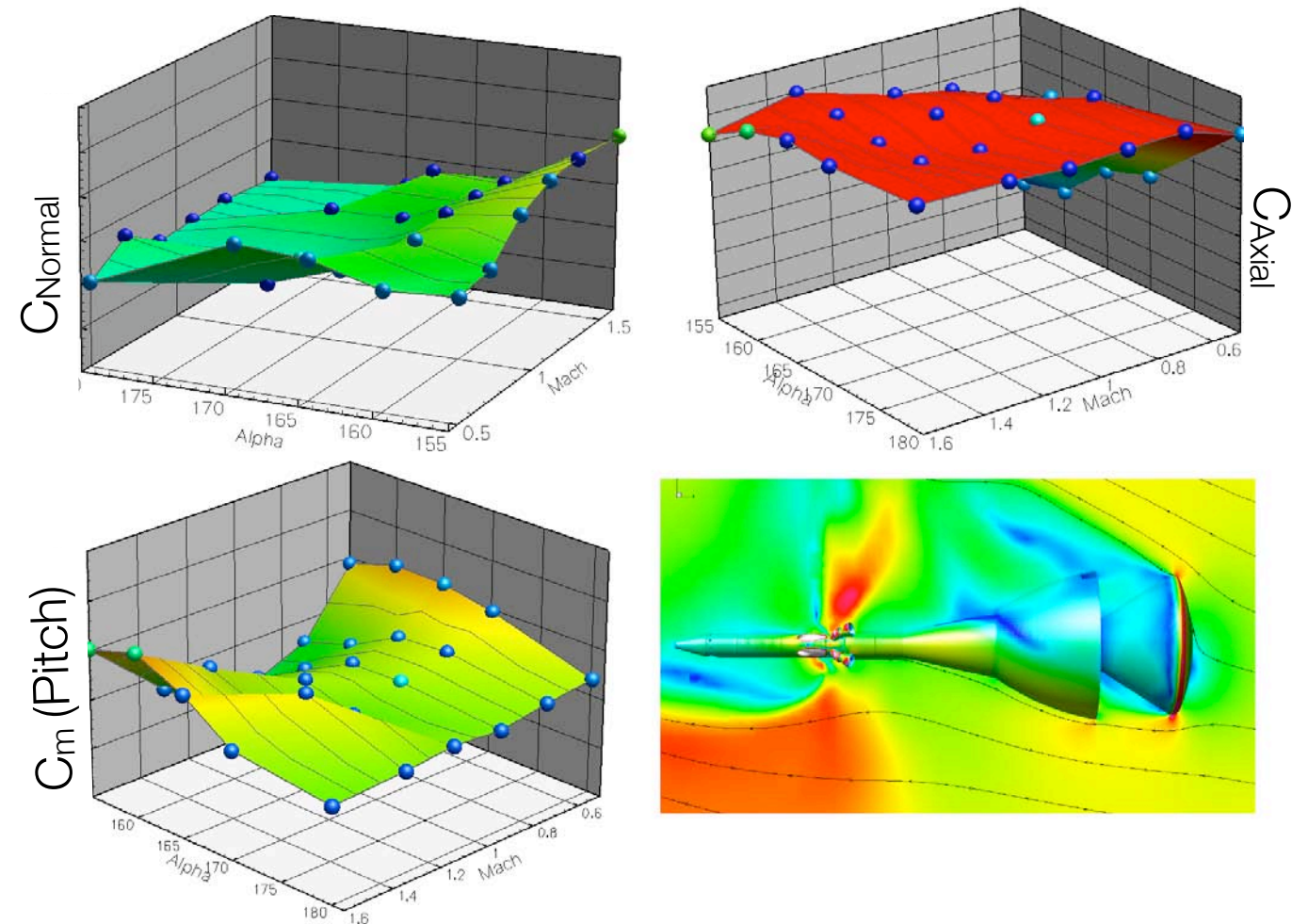
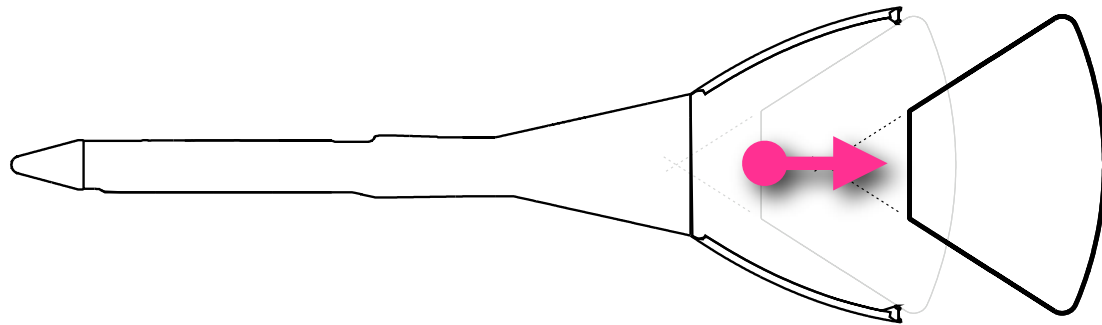
Loads on CM and LAM in proximity

(Δx , 0.0, 0.0, 0°)



Loads on CM

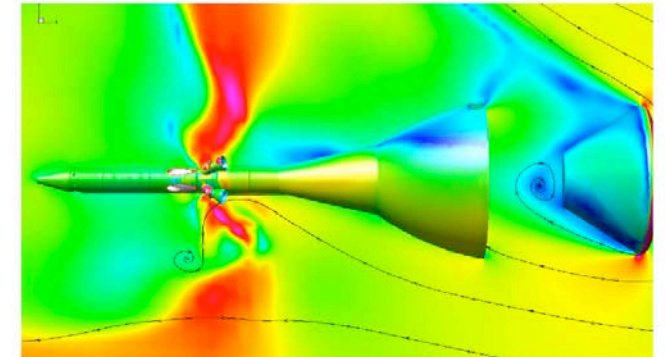
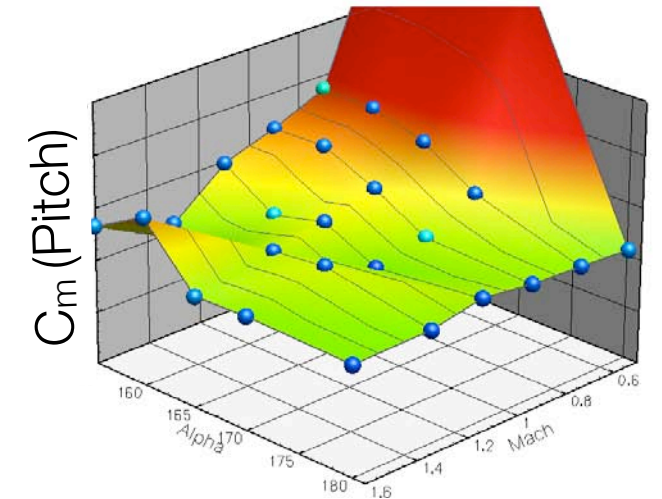
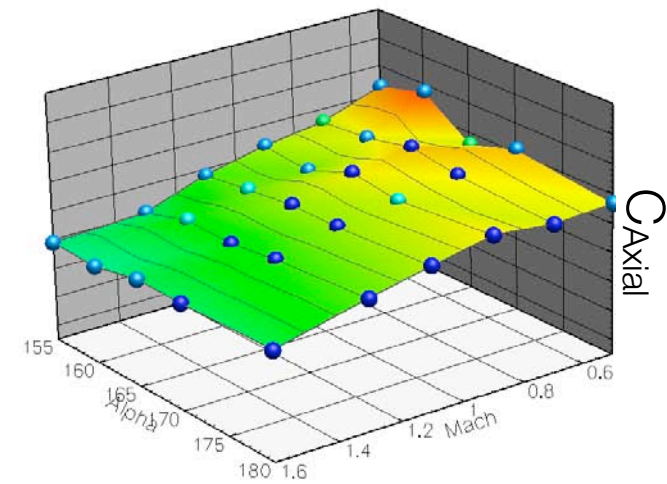
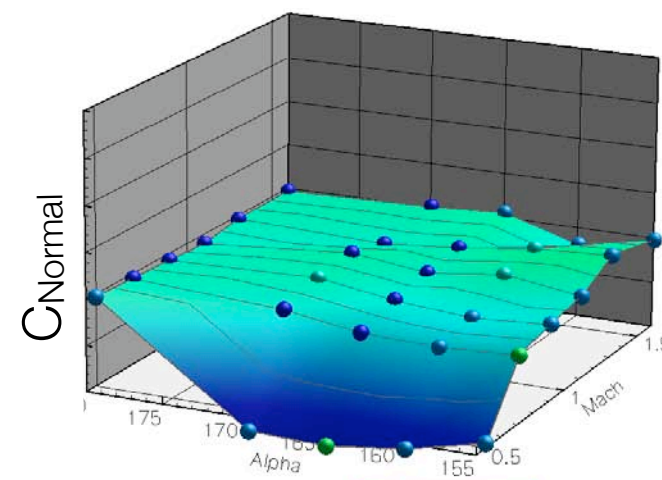
Loads on LAM



Database Samples

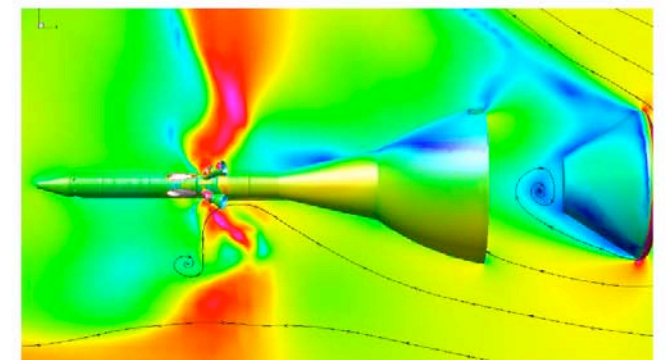
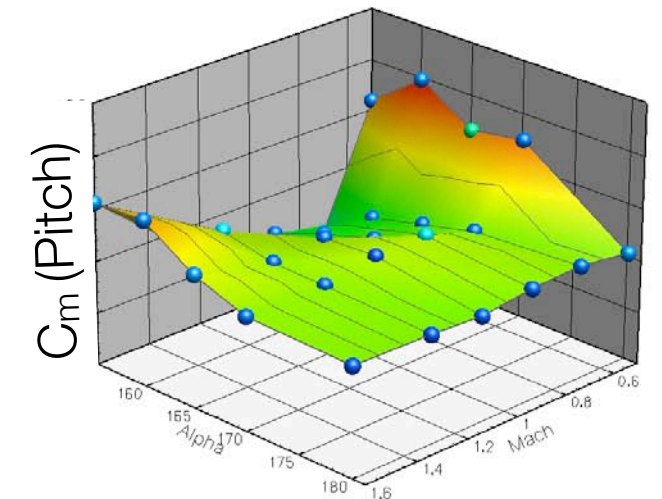
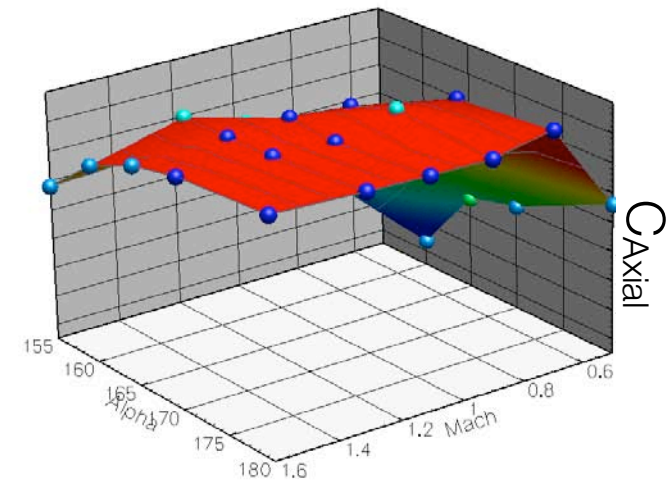
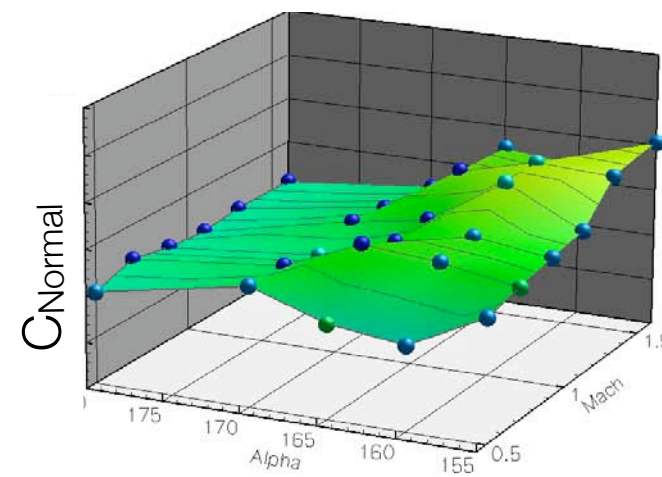
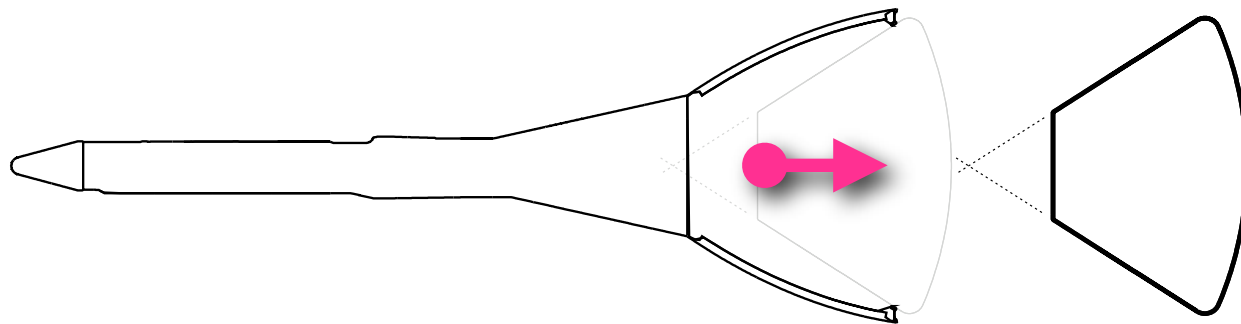
Loads on CM and LAM in proximity

($\Delta x, 0.0, 0.0, 0^\circ$)



Loads on CM

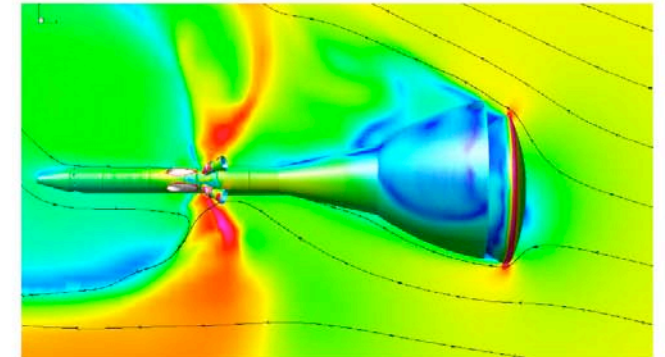
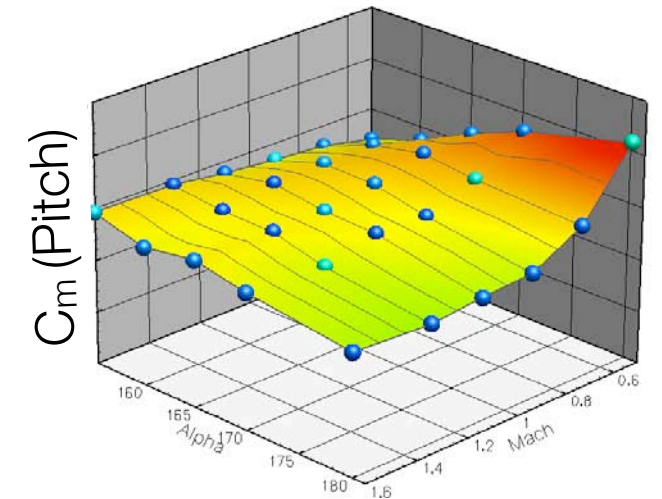
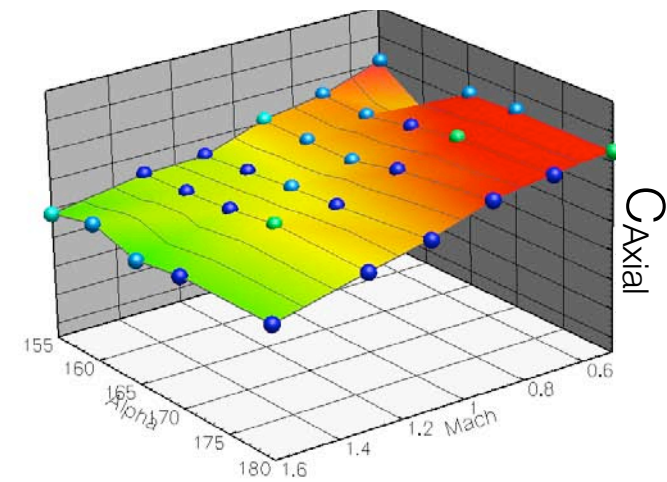
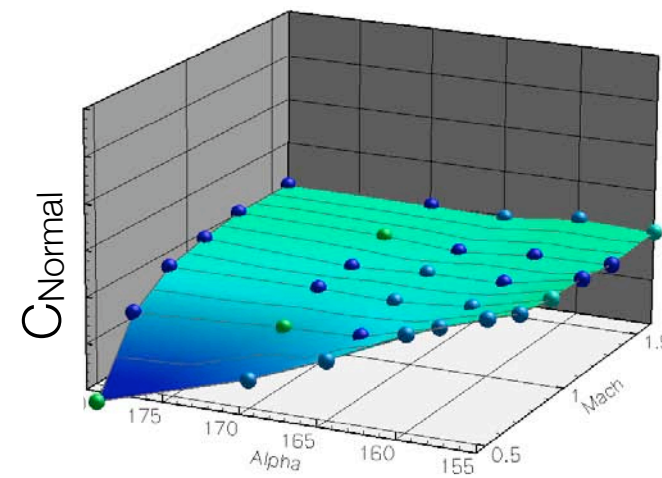
Loads on LAM



Database Samples

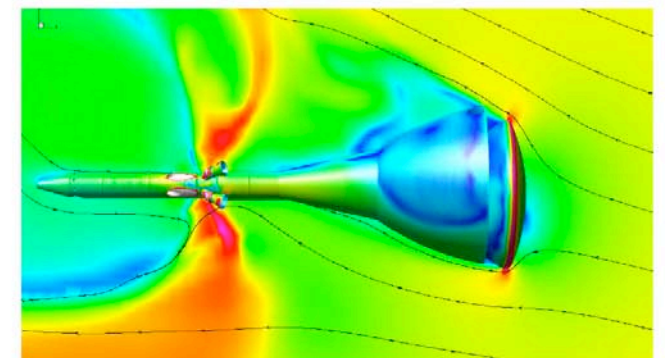
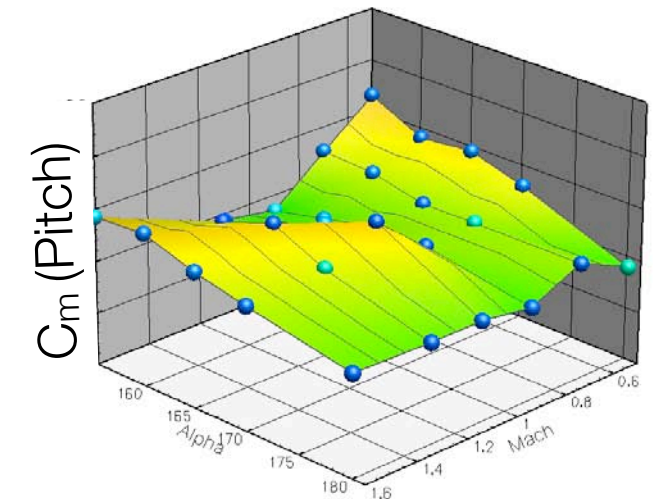
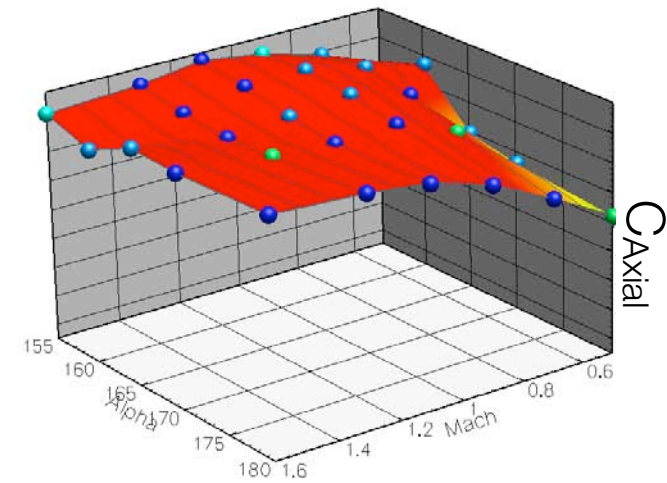
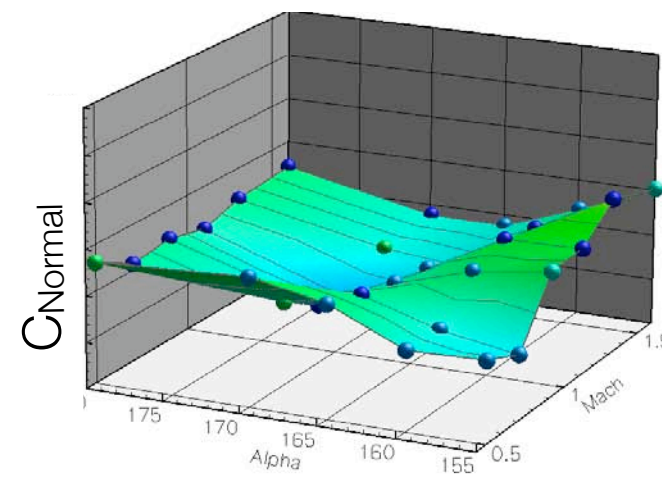
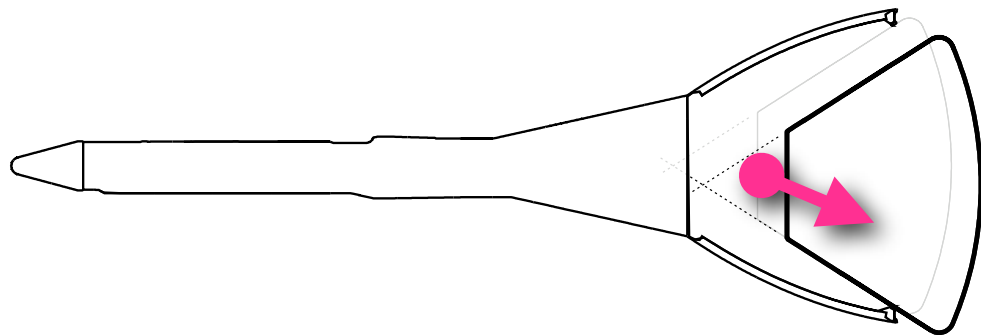
Loads on CM and LAM in proximity

$(\Delta x, 0.0, -\Delta z, 0^\circ)$



Loads on CM

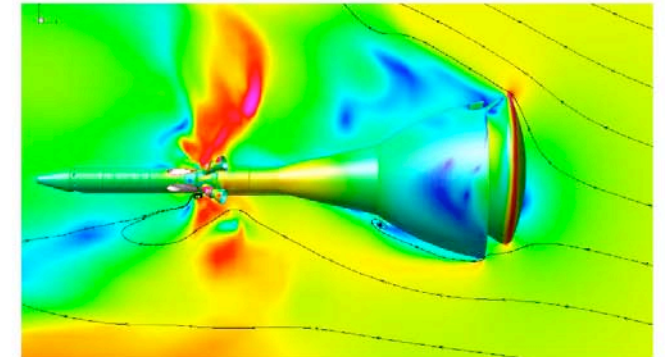
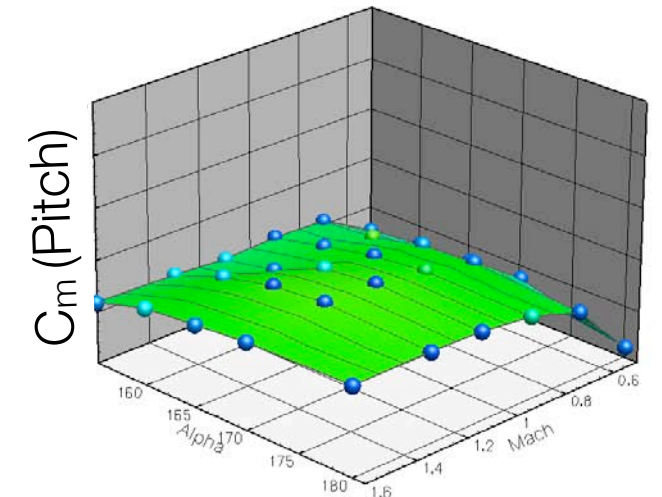
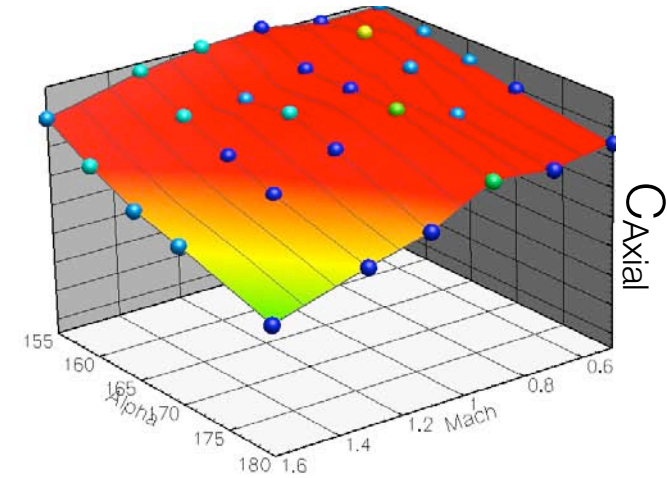
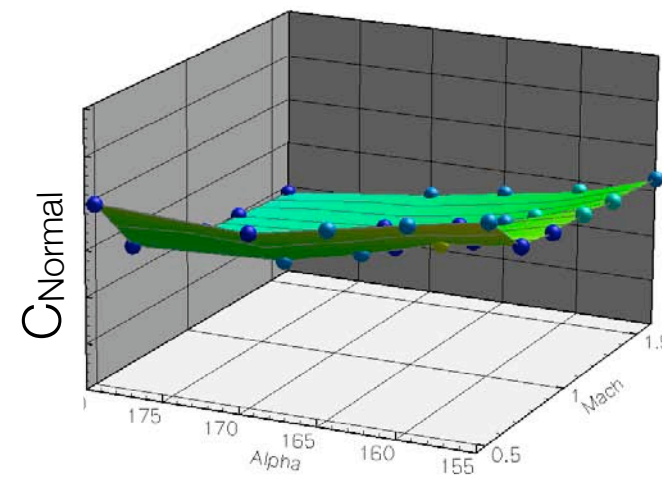
Loads on LAM



Database Samples

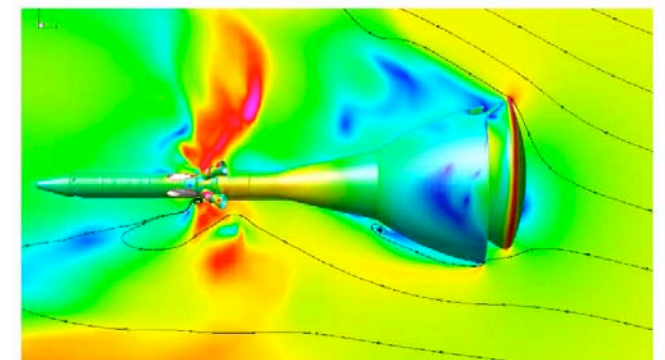
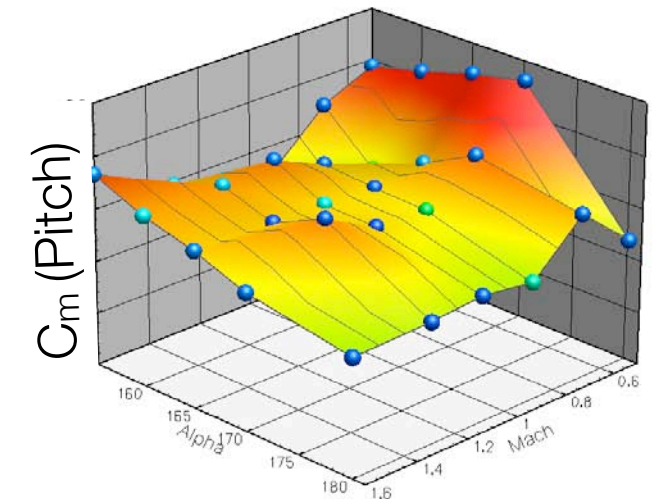
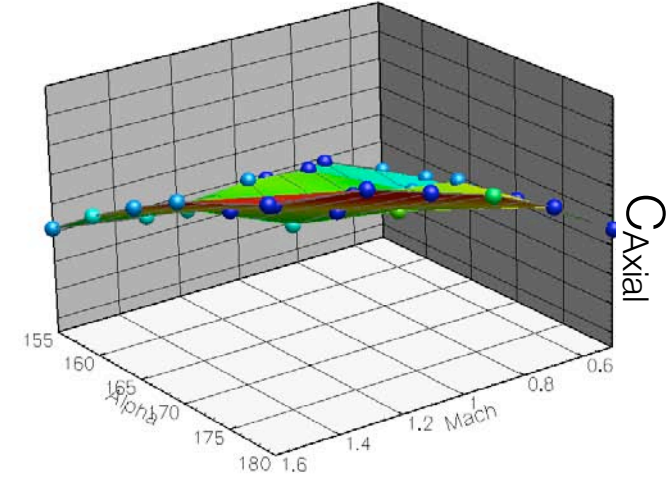
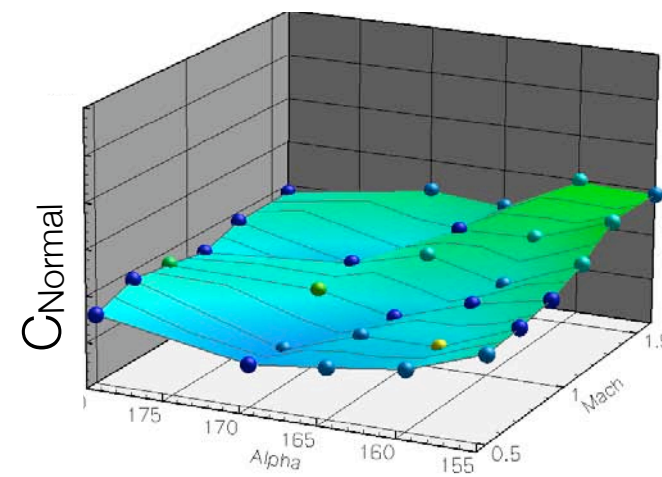
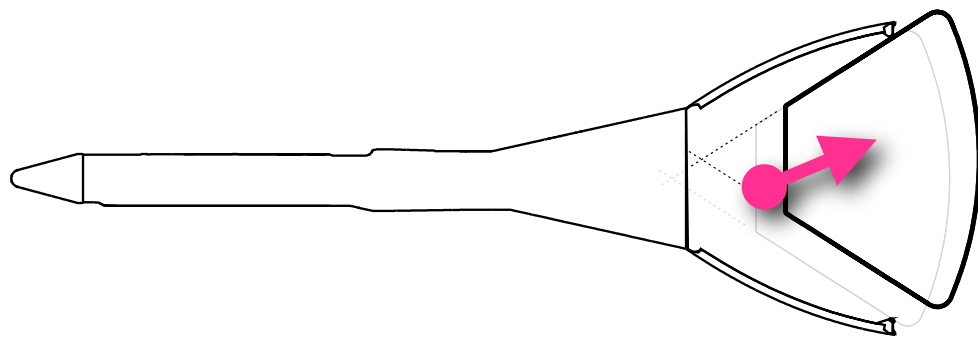
Loads on CM and LAM in proximity

$(\Delta x, 0.0, \Delta z, 0^\circ)$



Loads on CM

Loads on LAM





Summary

Presented a reliable and efficient approach for error estimates and mesh refinement of complex geometry problems

1. Handles complex geometry problems in an automatic fashion
2. Tolerant of coarse initial meshes
3. Behavior of functional, correction, and error estimate provide an indication of errors due to lack-of-convergence in steady simulations

- ➔ **It is our best mesh generator ... refinement complements and surpasses expert knowledge**
- ➔ **Allows users to focus on data validation and analysis instead of mesh generation**



Present and Future Work

- Sonic-boom applications (Mathias Winzter, AIAA 2008-6593)
- Address unsteadiness issues in difficult cases
 - Affordable mesh refinement and error bound for “mildly” unsteady flow
 - Formal unsteady adjoint development
- Control accuracy of objective functions in optimization studies

Acknowledgments

- Marsha Berger, NYU
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